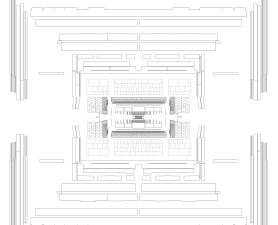
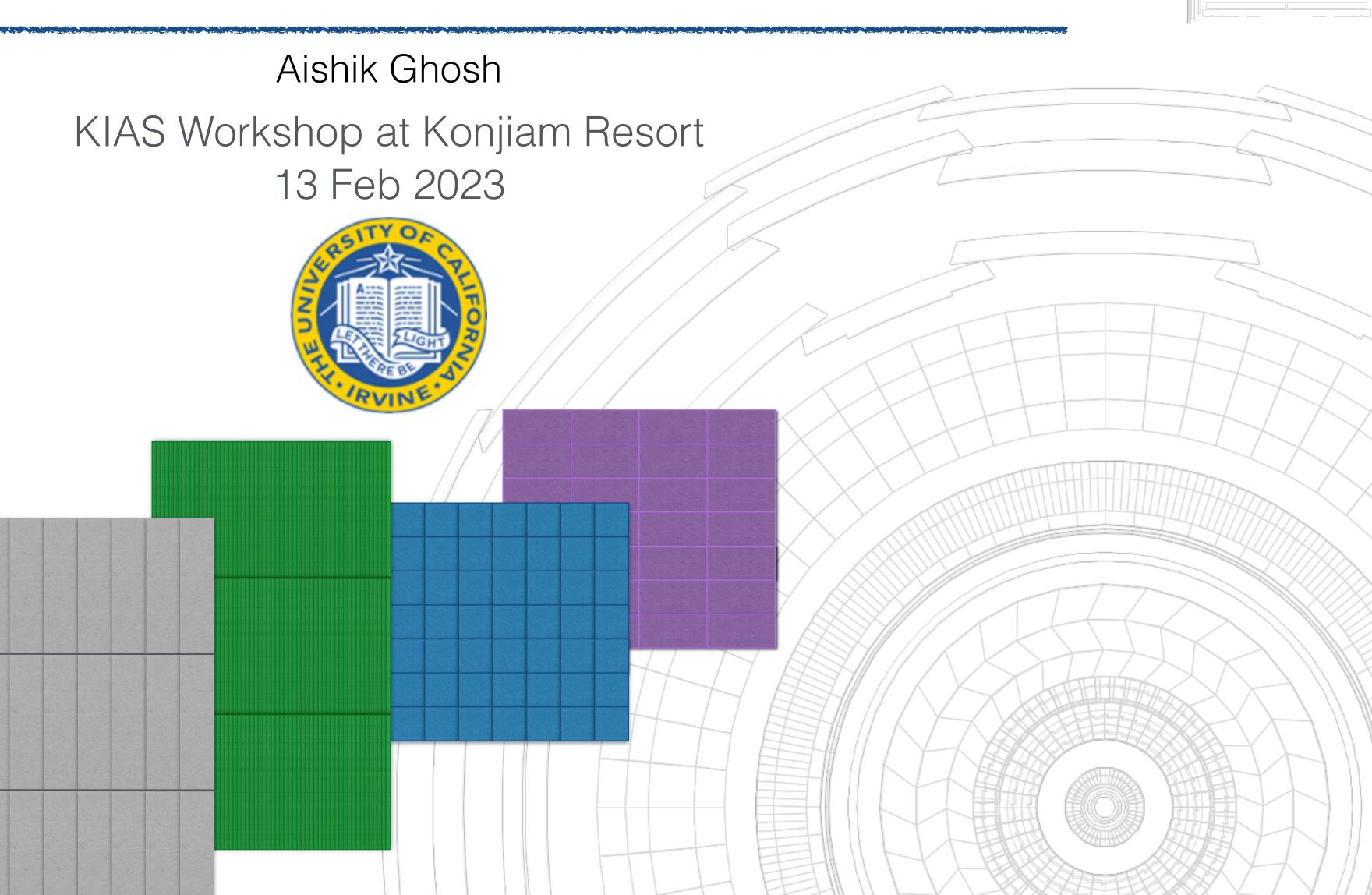
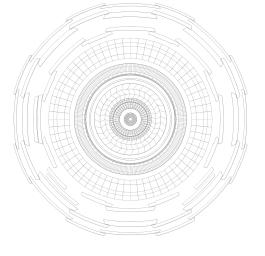


Uncertainties in the era of ML



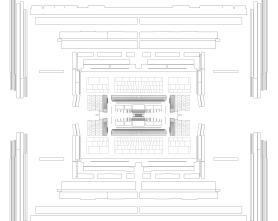




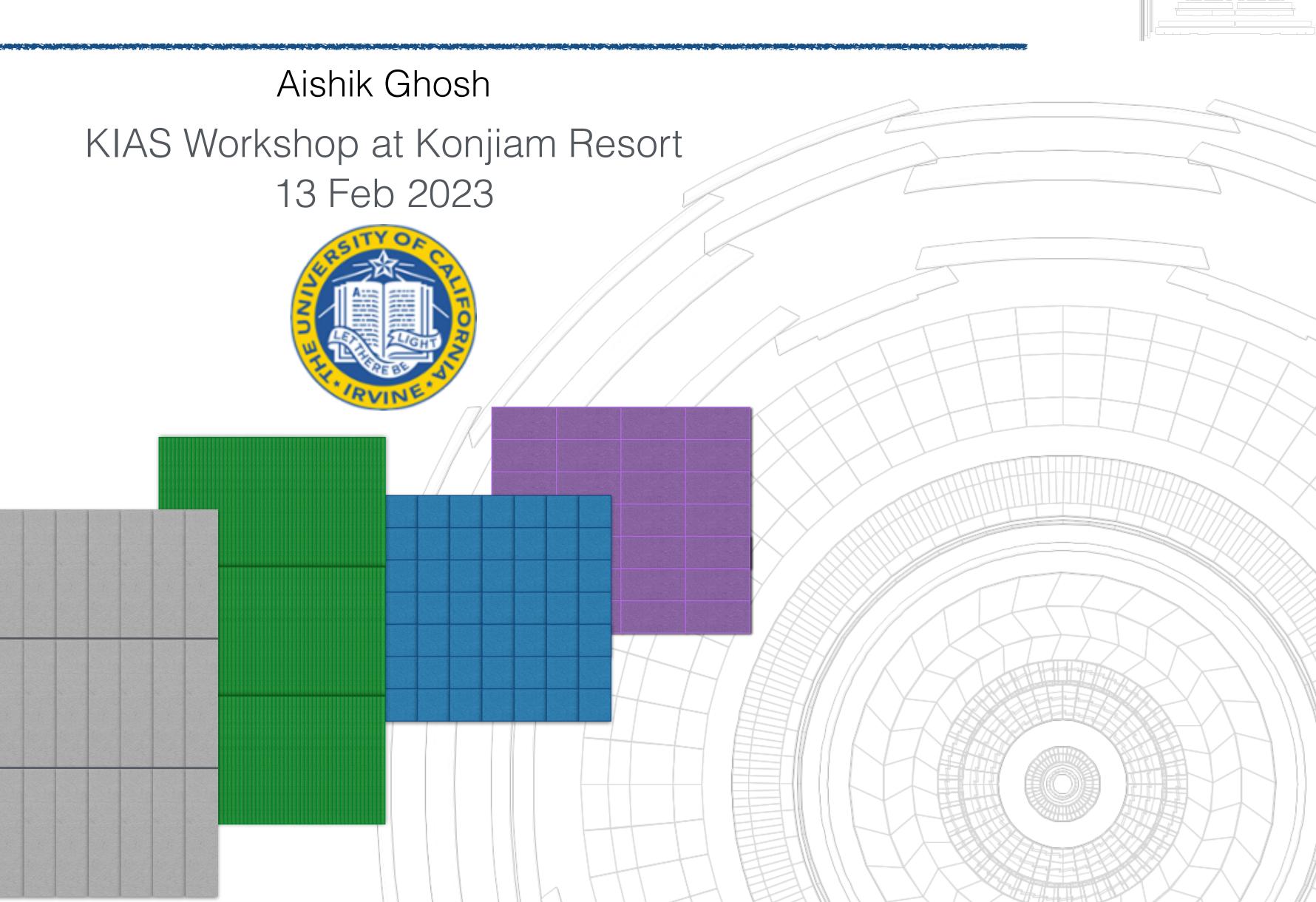


Polarising topic, expect spicy debate..

Uncertainties in the era of ML







$$mH = 125.25 \pm 0.17 \text{ GeV}$$

$$mH = 125.25 \pm 0.17 \,\text{GeV}$$

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How sure am I? How can I reduce my uncertainty?

$$mH = 125.25 \pm 0.17 \, GeV$$



How sure am I? How can I reduce my uncertainty?

Systematic Uncertainties: What if all my measurements are biased in the same way !?

$$mH = 125.25 \pm 0.17 \,\text{GeV}$$

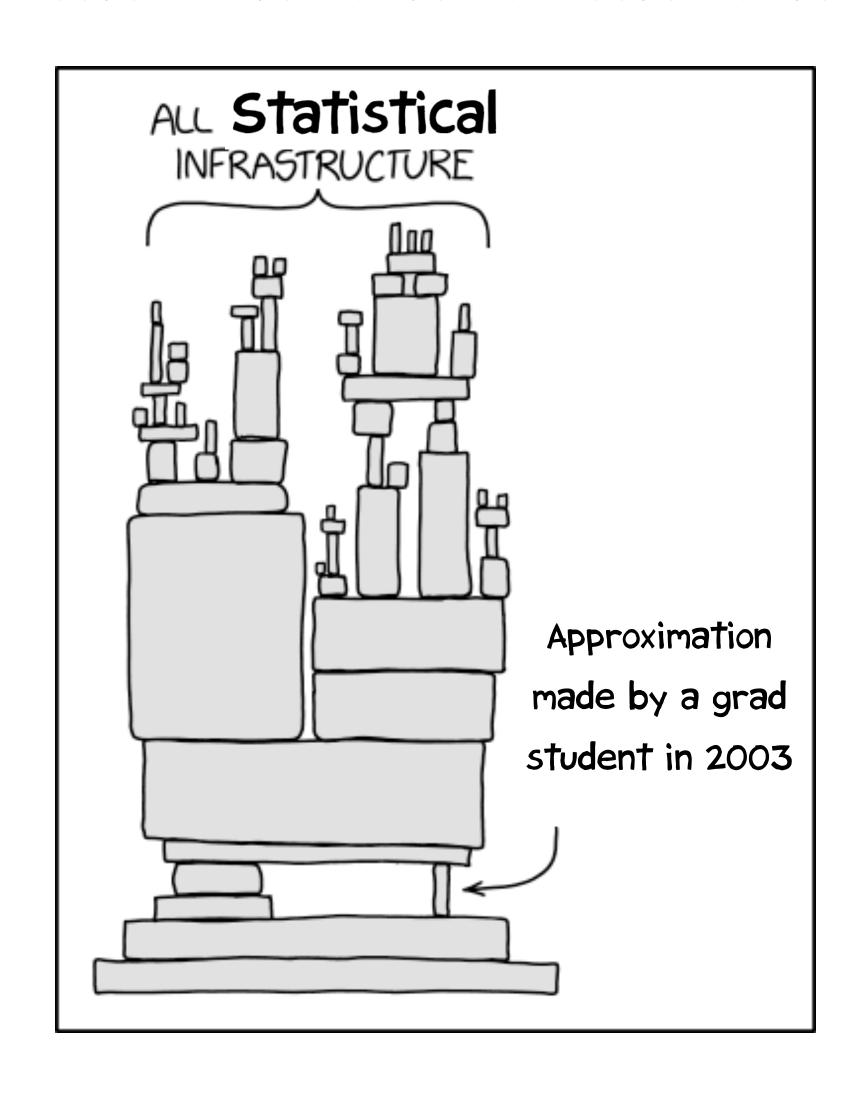
{statistical, detector systematic, theory systematic, epistemic,}



How sure am I? How can I reduce my uncertainty?

Systematic Uncertainties: What if all my measurements are biased in the same way !?

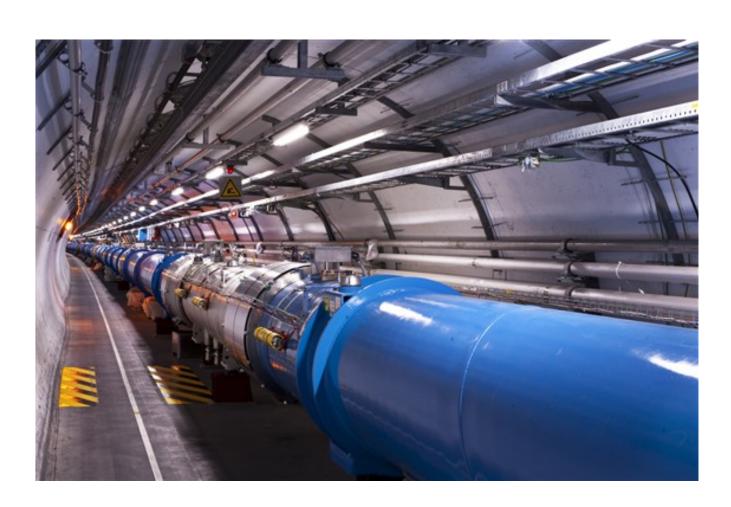
Nuisance Parameter Infrastructure



Time to re-examine some of the underlying pieces

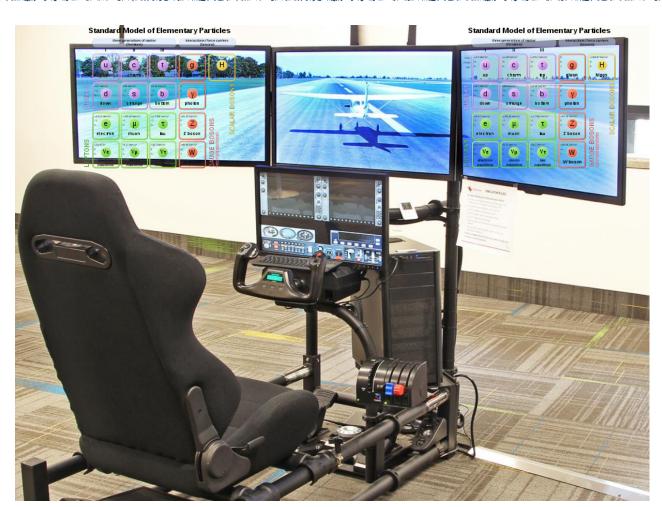
Are they up to the task of the precision era?

Simulation Based Inference at LHC



Unlabelled data from LHC

Compare to find New Physics



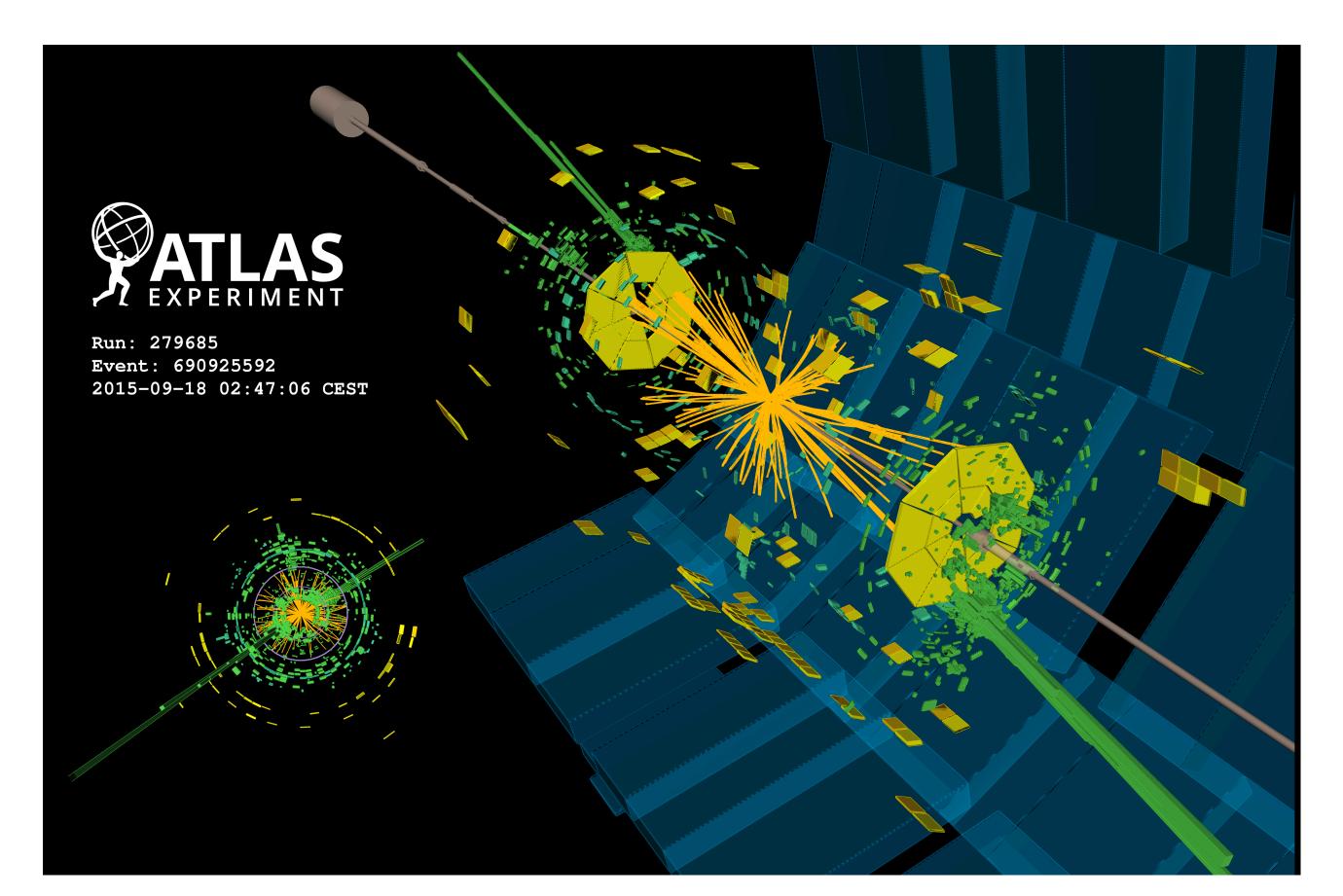
Simulation using Standard Model of particle physics

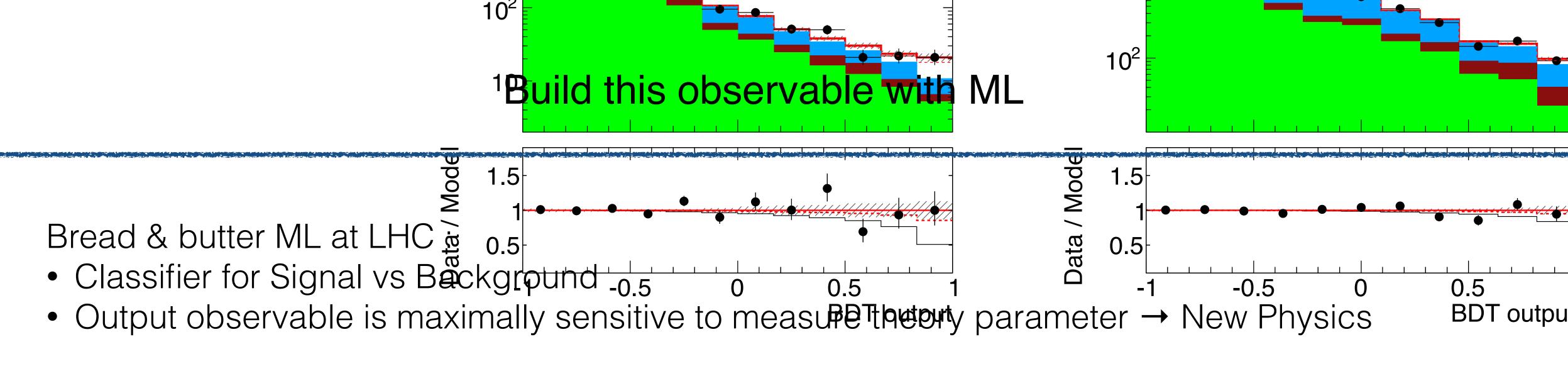
High dimensional data

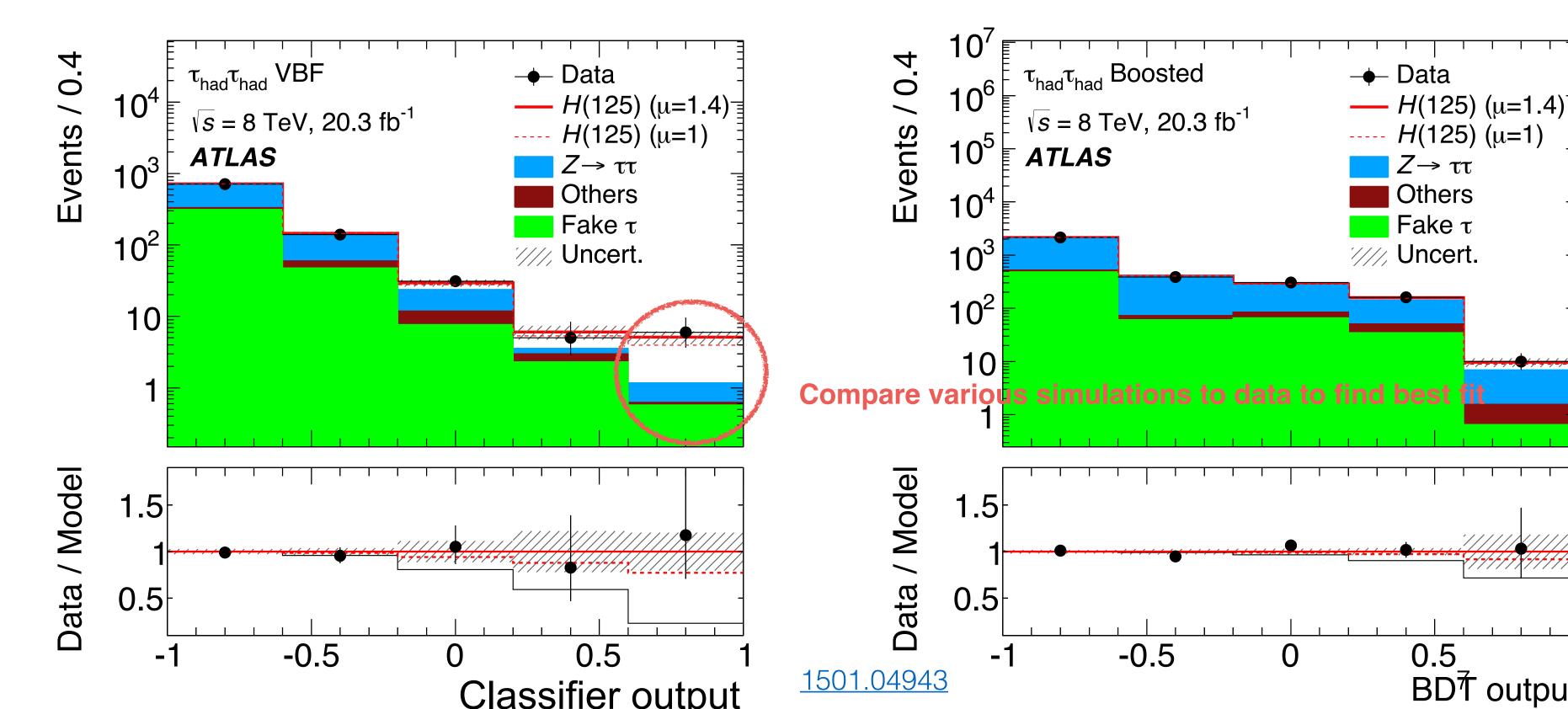
Detector has ~100 million sensors

→ Combine information into 1 powerful variable

Look at histogram of this variable







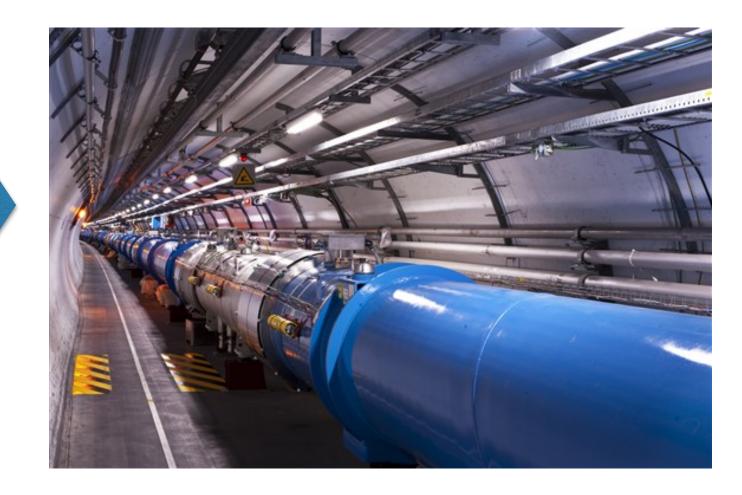
Known unknowns

Simulation using Standard Model of particle physics



Train ML models on simulation, apply on data

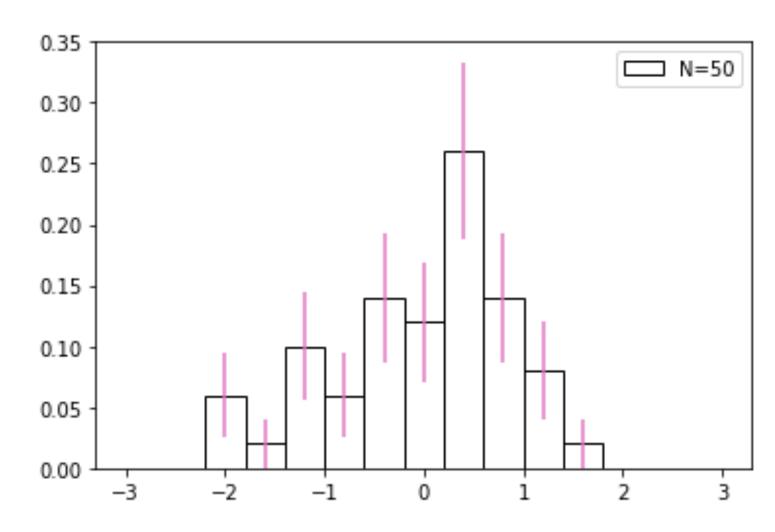
Unlabelled data from LHC



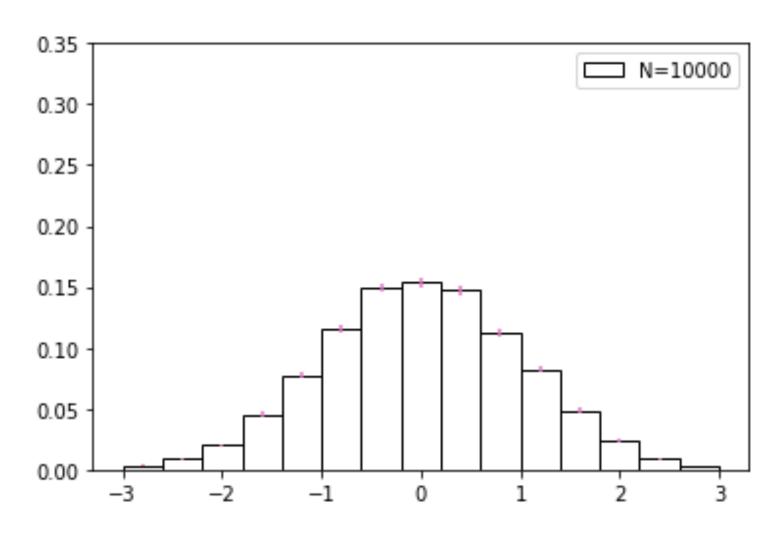
Simulate using best guess: Z=1

Detector state Z = ? in data

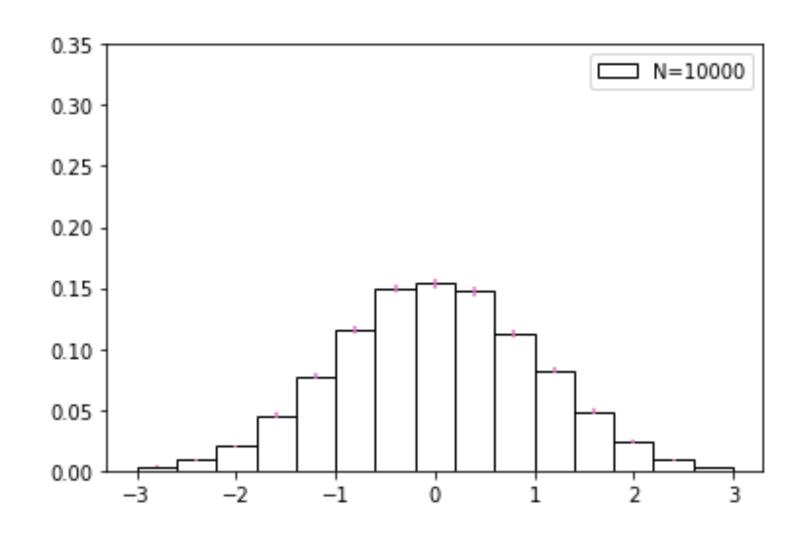
Statistical Uncertainty



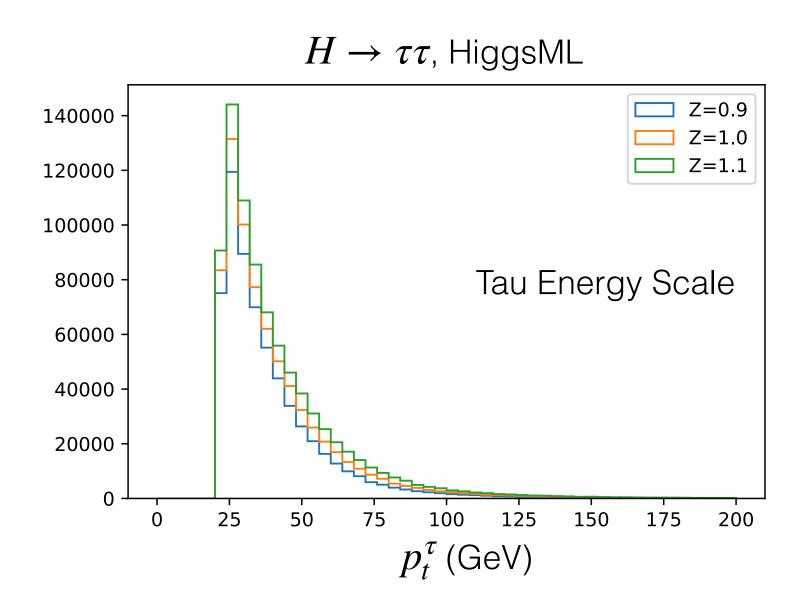
Statistical Uncertainty



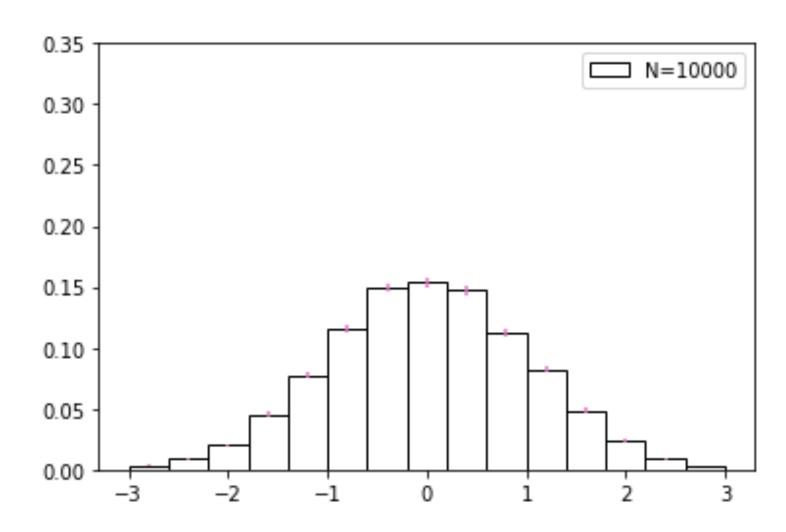
Statistical Uncertainty



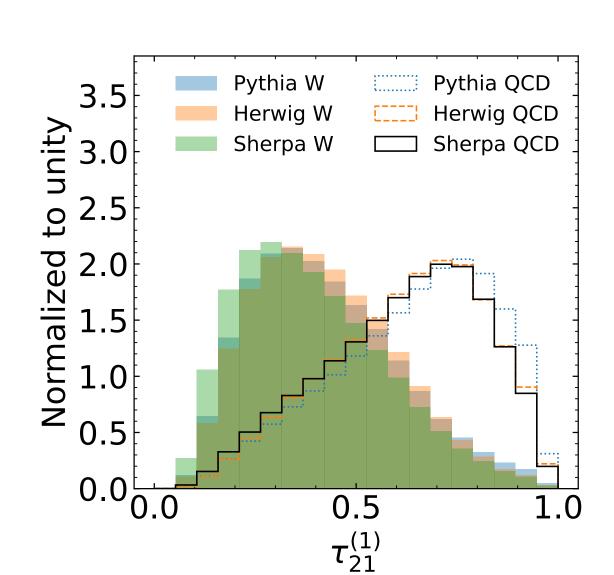
Systematic Experimental Uncertainty



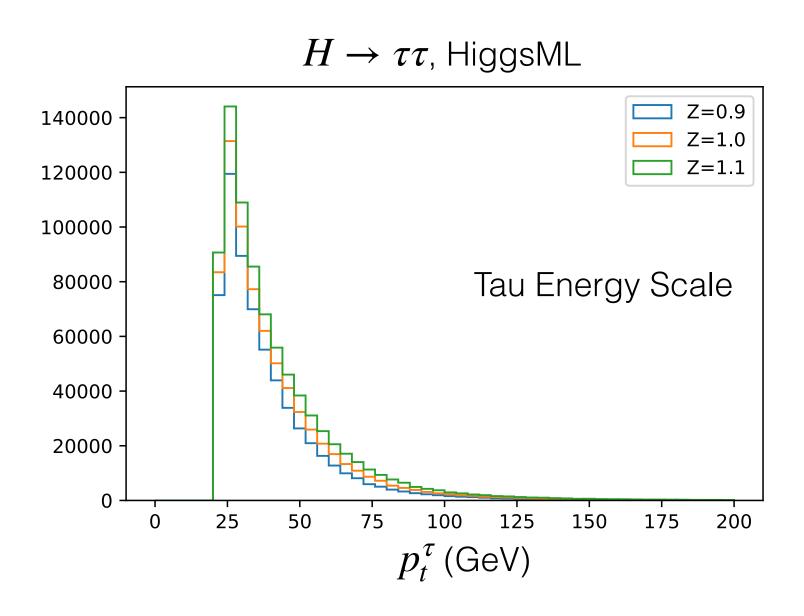
Statistical Uncertainty



Systematic Theory Uncertainty



Systematic Experimental Uncertainty



Aleatoric Uncertainty



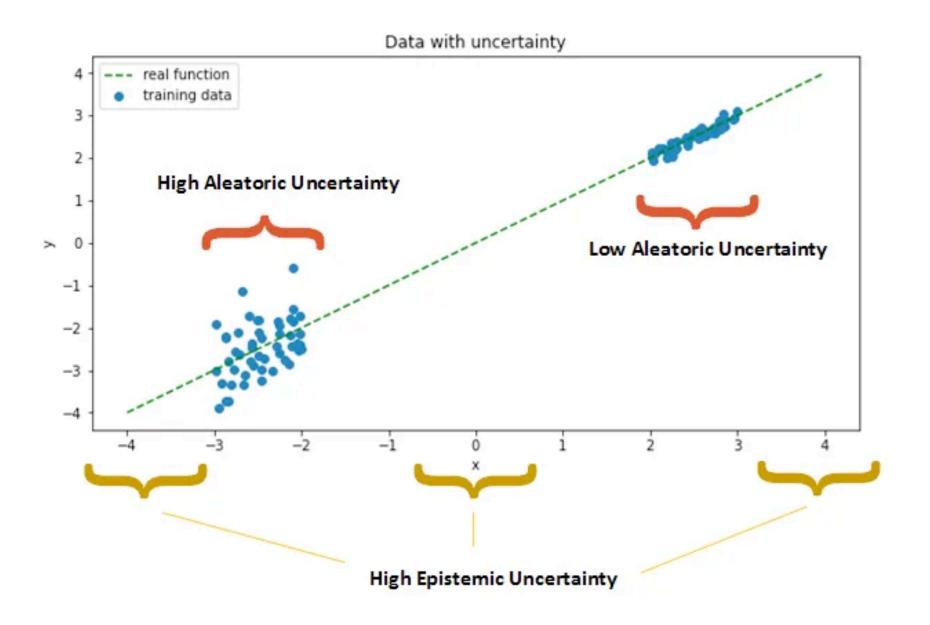
Inherent in data / experiment Irreducible

Aleatoric Uncertainty



Inherent in data / experiment Irreducible

Epistemic Uncertainty



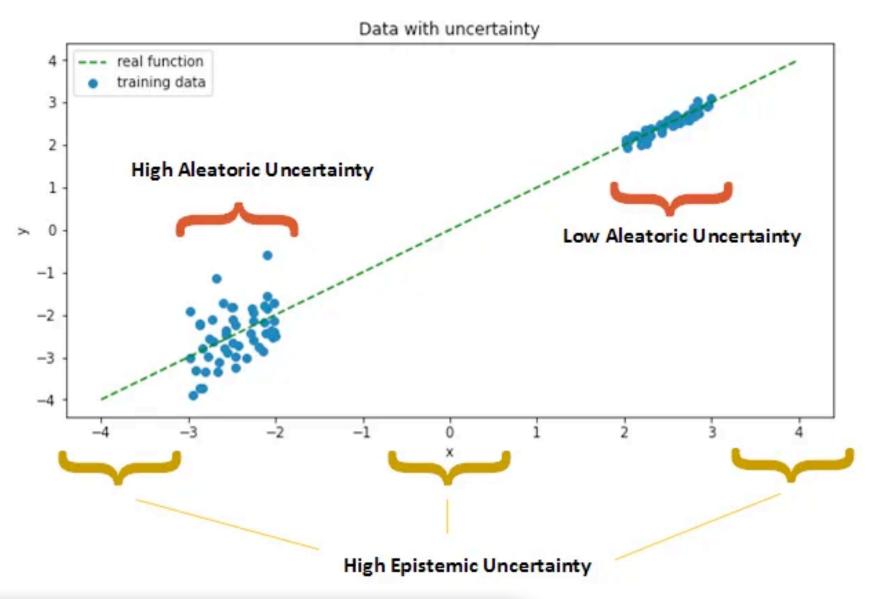
Could reduce by gathering more data

https://towardsdatascience.com/my-deep-learning-model-says-sorry-i-dont-know-the-answer-that-s-absolutely-ok-50ffa562cb0b

Aleatoric Uncertainty



Epistemic Uncertainty



Irreducible



Snowmass 2021: Advocate to build common language

Outline

- Experimental Uncertainties
- Theory Uncertainties
- Performance Quantification Metrics for Generative Models

Experimental Uncertainties

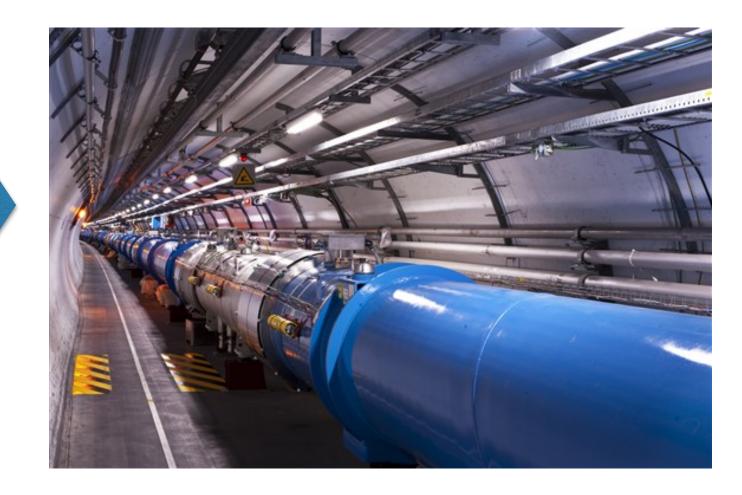
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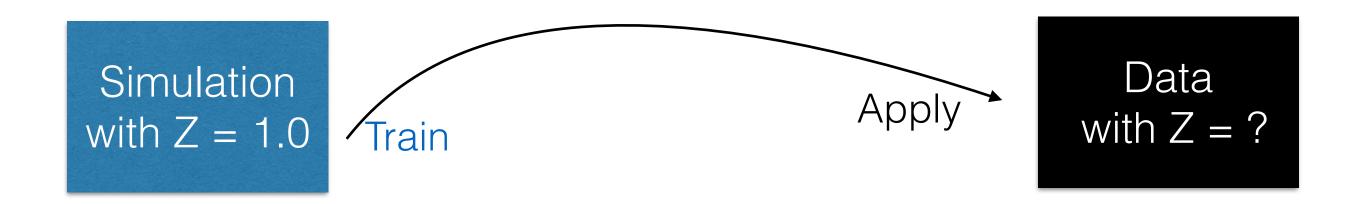


Simulate using best guess: Z=1

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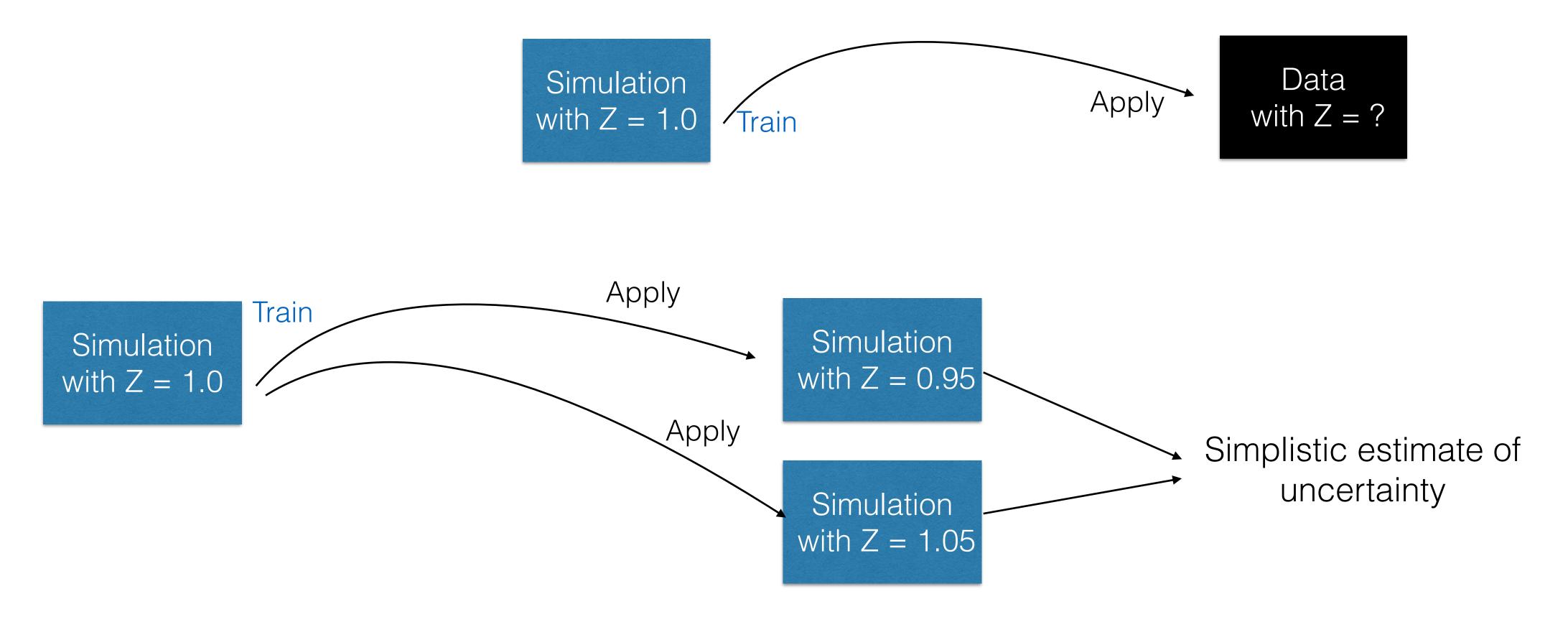
Baseline Approach to Uncertainty Quantification

Train AI classifier on nominal data (assume detector state Z=1) and estimate uncertainties using alternate simulations



Baseline Approach to Uncertainty Quantification

Train AI classifier on nominal data (assume detector state Z=1) and estimate uncertainties using alternate simulations



Full statistical treatment → Expensive 'Profile Likelihood'

Similar ideas: <u>1905.10384</u>, <u>1305.7248</u>

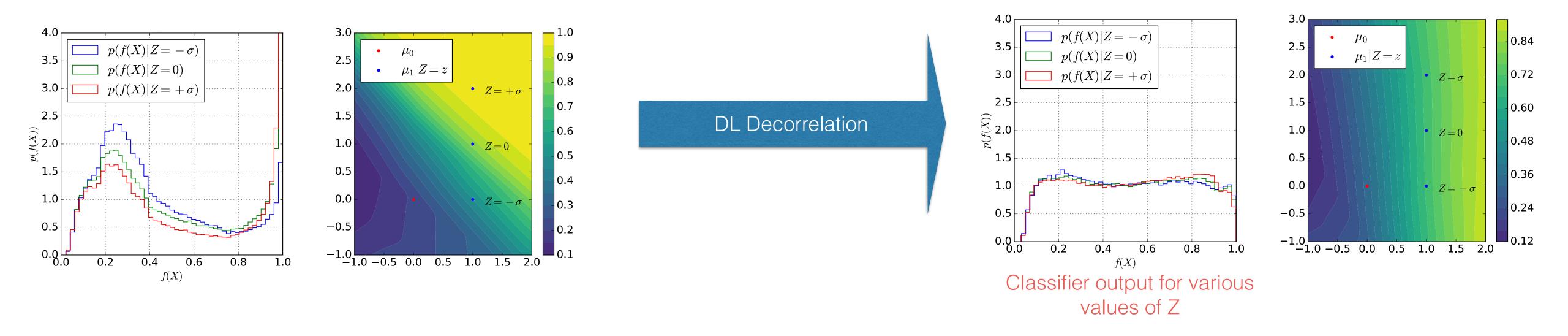
1907.11674

epjconf_chep2018_06024

Lots of innovation towards decorrelated classifiers

Ideas from AI fairness: Make the classifier make the same response regardless of race / gender

Imported to physics: Make classifier robust to changes in Z (invariant to impact of nuisance parameters)

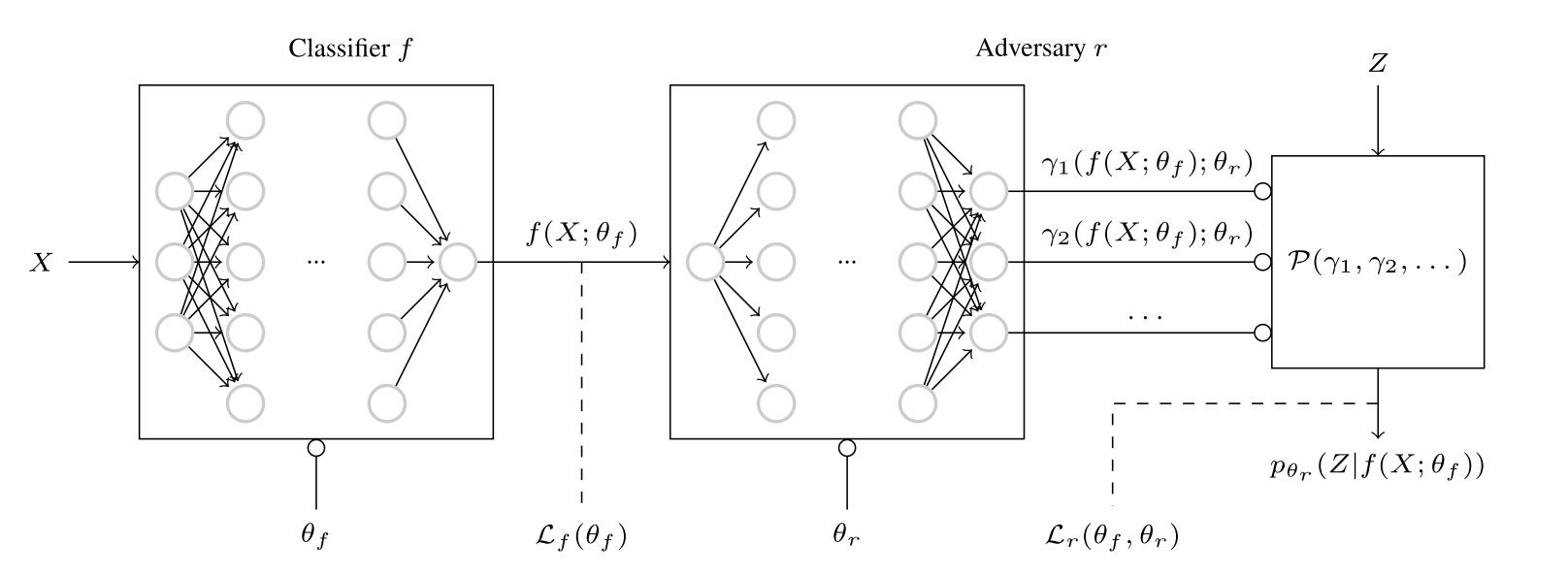


Similar ideas: <u>1905.10384</u>, <u>1305.7248</u>,

<u>1907.11674</u>,

epjconf_chep2018_06024

Adversarial decorrelation



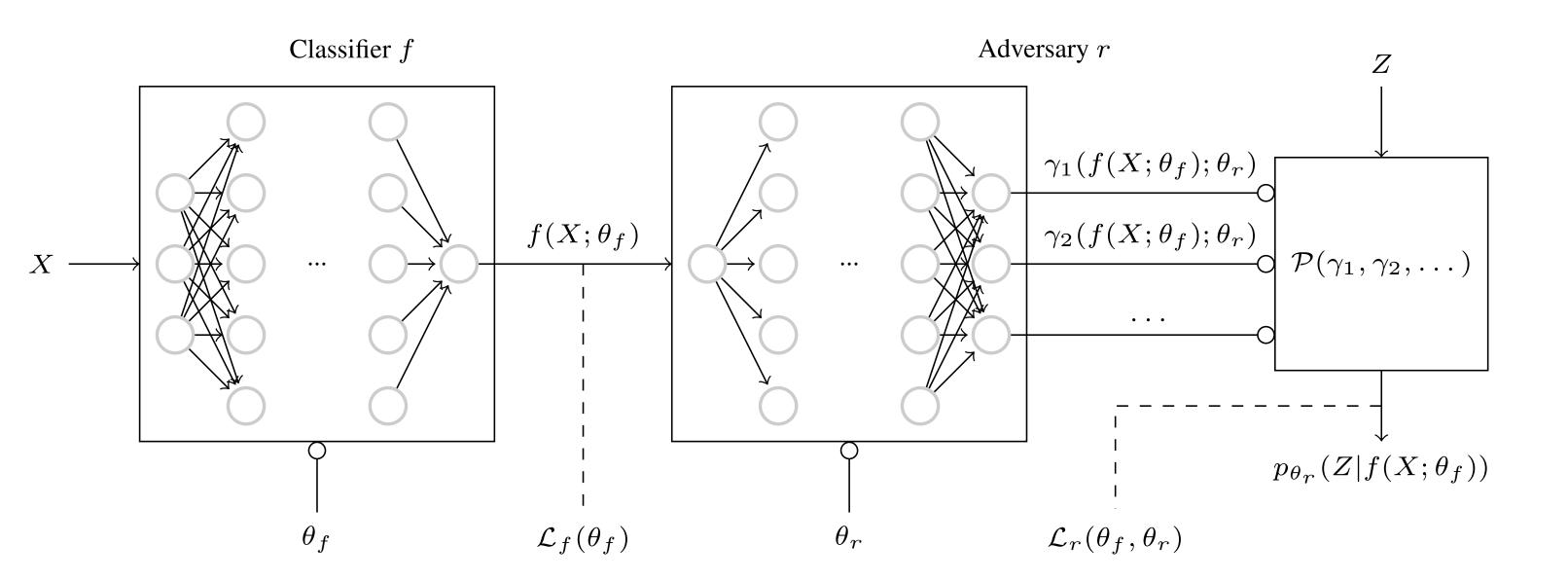
$$L_{Classifier} = L_{Classification} - \lambda \cdot L_{Adversary}$$

Similar ideas: <u>1905.10384</u>, <u>1305.7248</u>,

<u>1907.11674</u>,

epjconf_chep2018_06024

Adversarial decorrelation

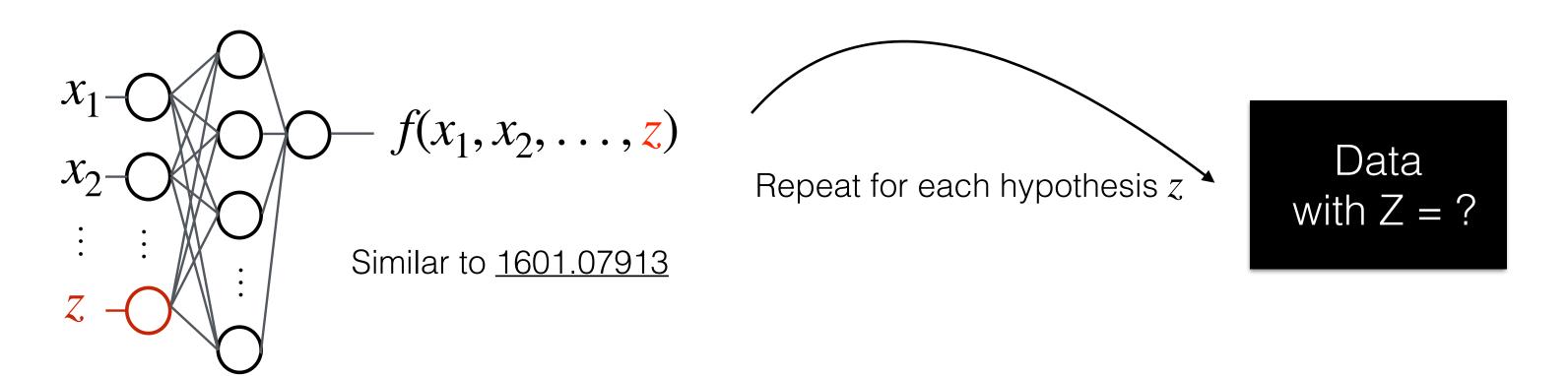


To fool the adversary, classifier output should be decorrelated to Z

$$L_{Classifier} = L_{Classification} - \lambda \cdot L_{Adversary}$$

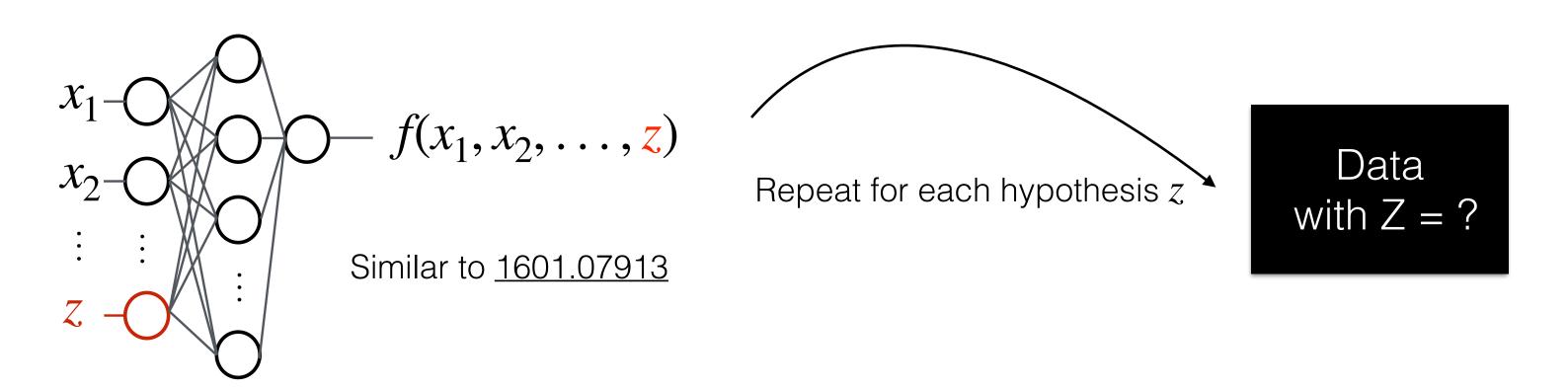
Advocated for the opposite of decorrelation

• Fully parameterise the classifier on Z in a "uncertainty aware" way



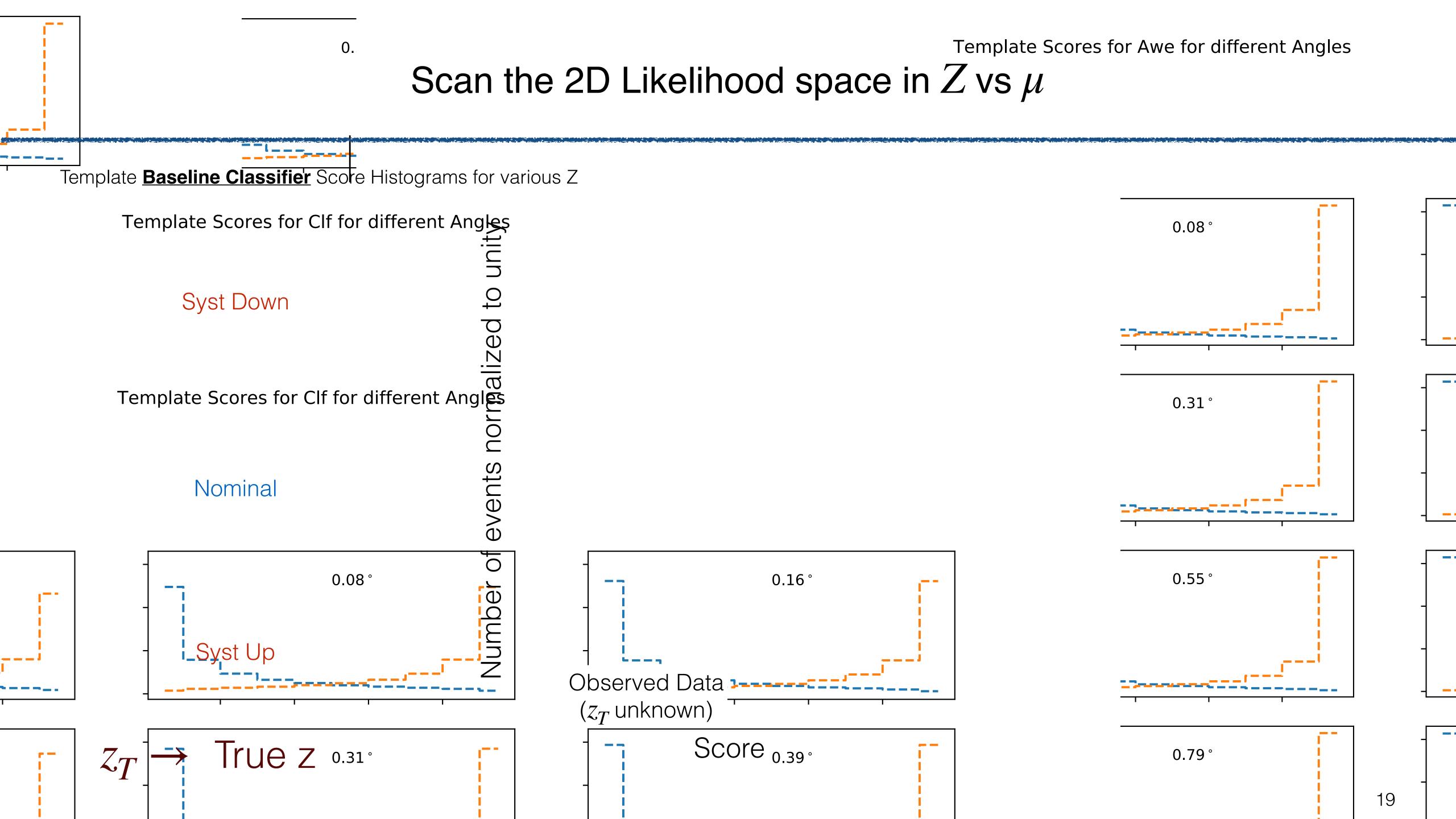
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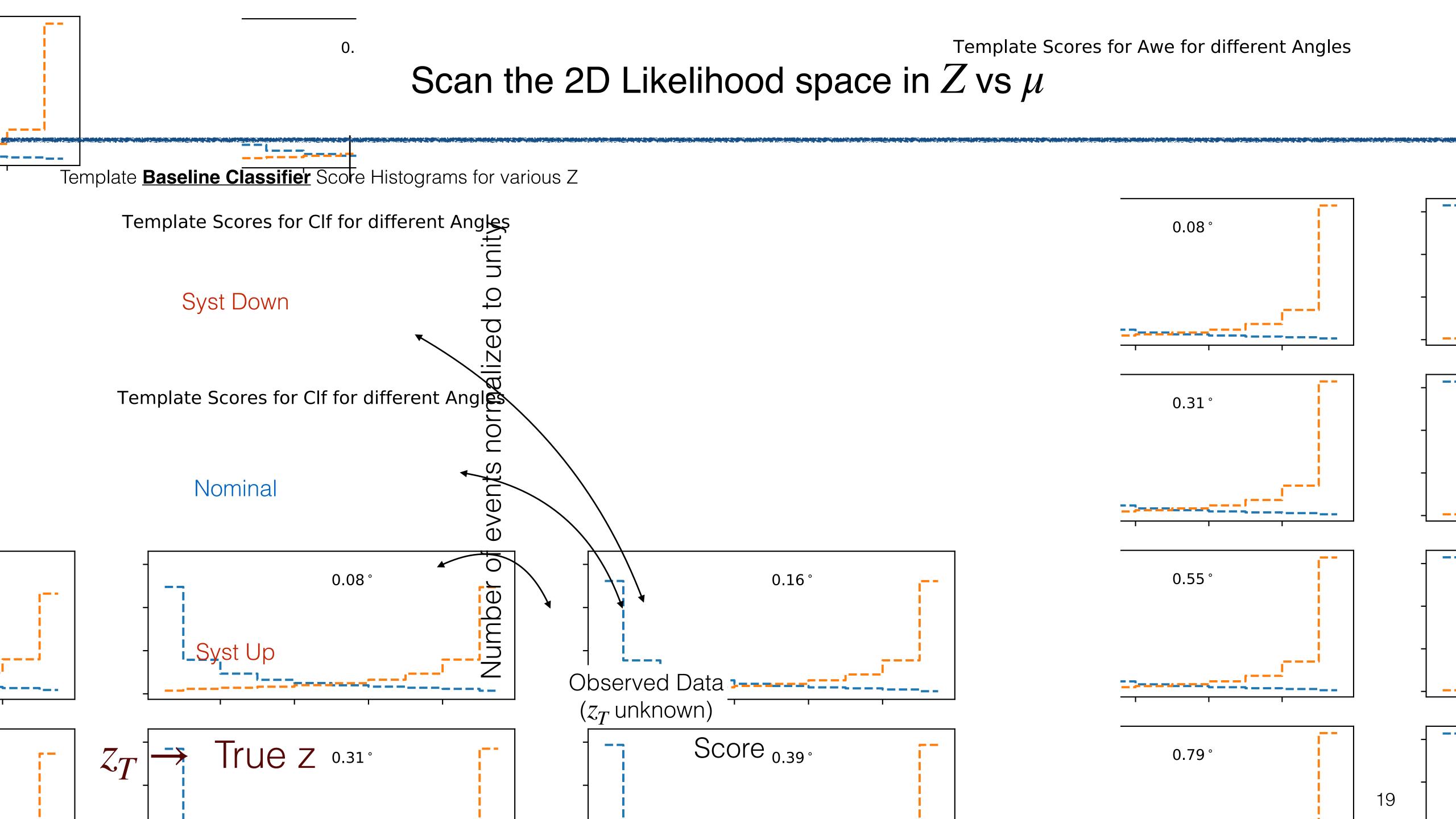
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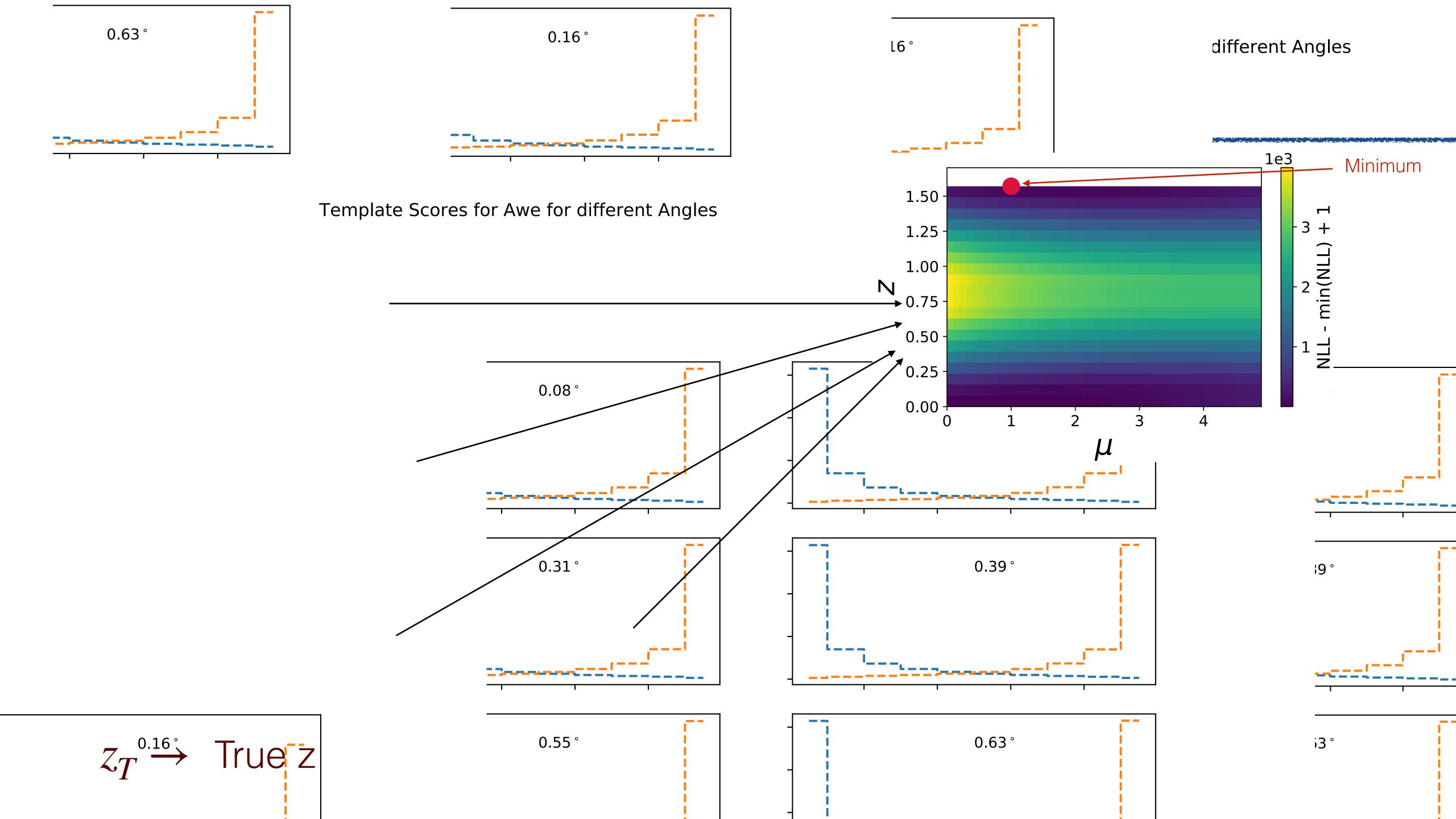


- Intuition: Allow the analysis technique to vary with Z
 You always get the best classifier for each value of Z
- Constrain nuisance parameters (NP) from data + incorporate prior
- Evaluation: The actual profile likelihood

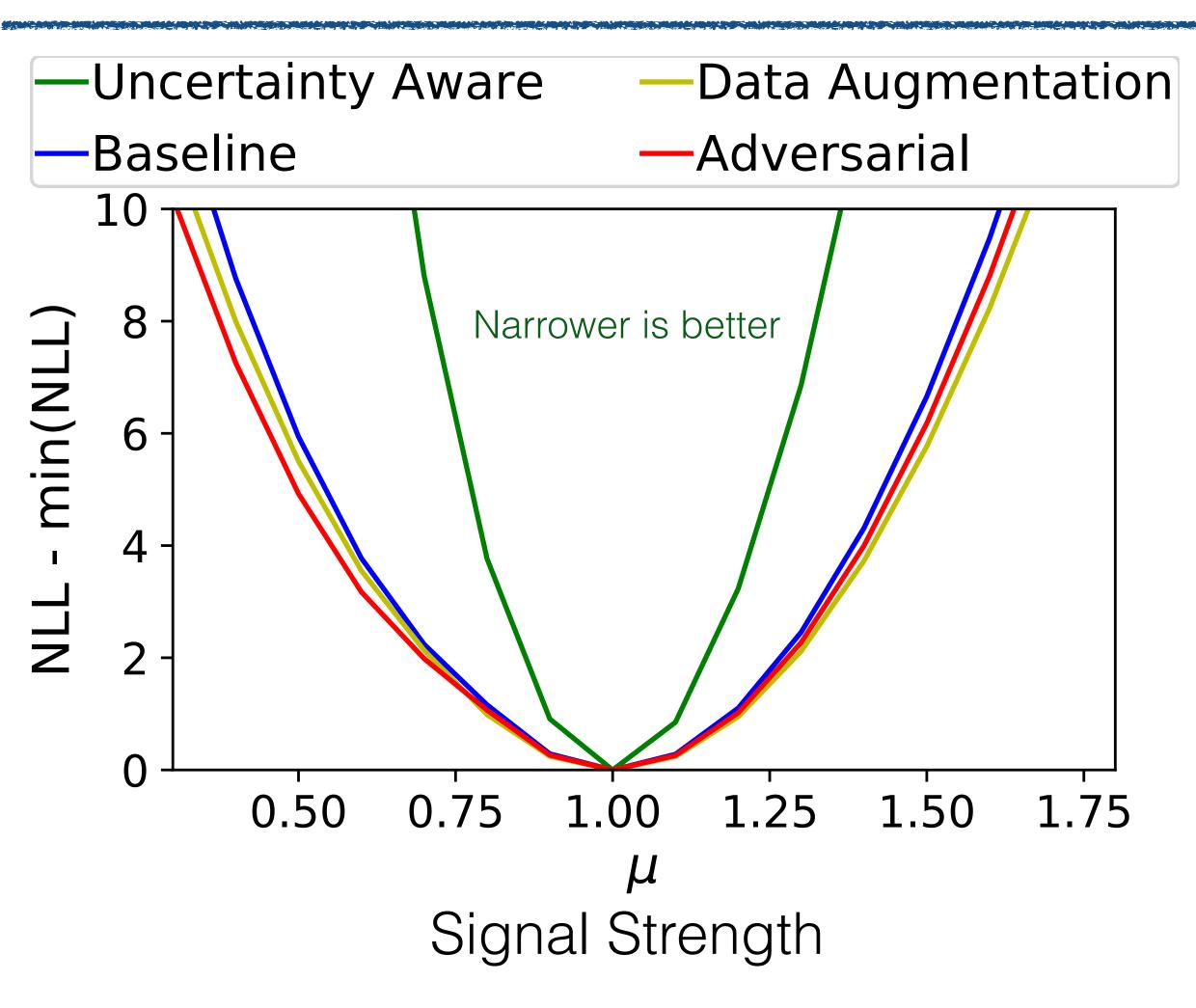
We don't know Z in collision data, what value do we use?







Profile away Z - Example at $(\mu, Z)_{True} = (1, 1.57)$



Narrower ⇒ Smaller [statistical + systematic] uncertainty on measurement

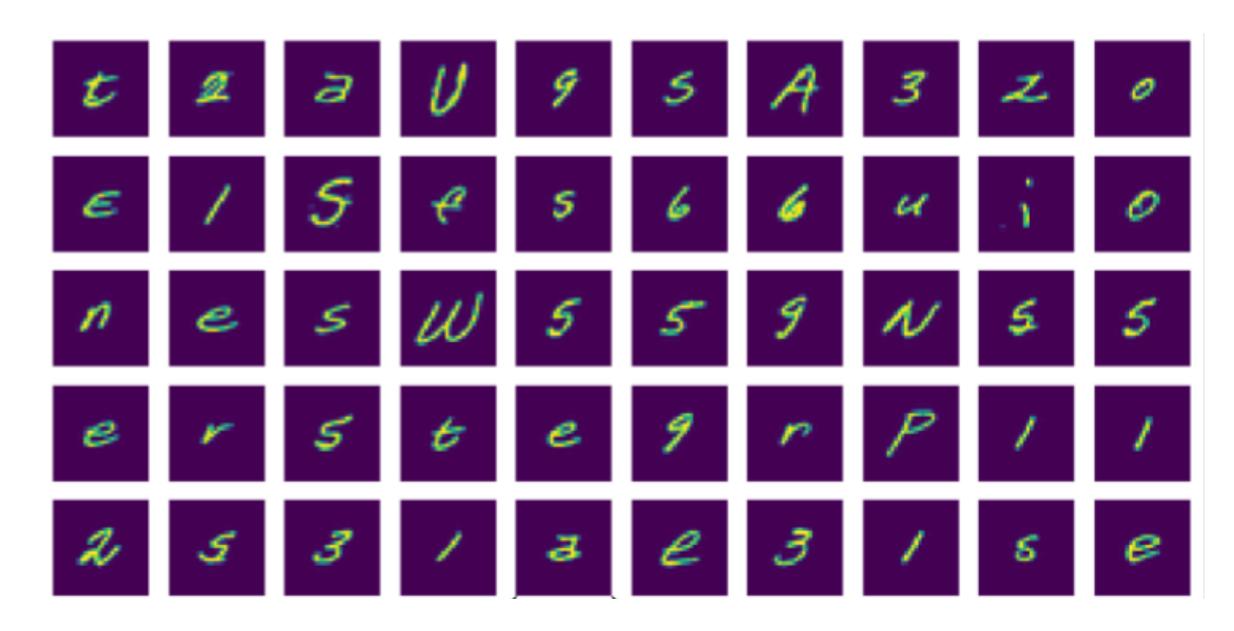
Narrower ⇒ We can exclude wrong values of µ with greater confidence

Practical for LHC analysis: Parameterise your main nuisance parameter but no need to train on all 100 NPs

- ML researchers assume i.i.d
- This technique exploits correlations between samples a different paradigm
- Interesting applications outside of physics

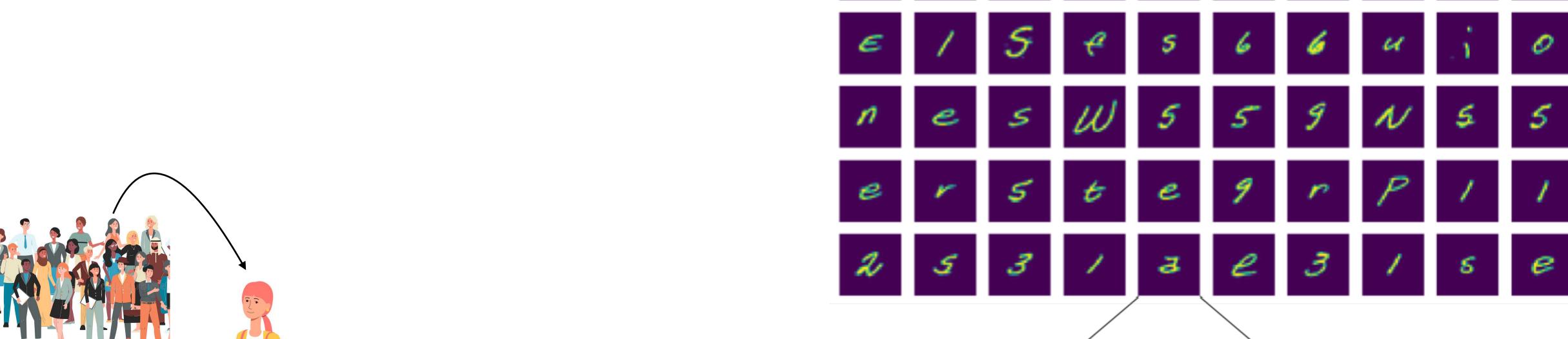
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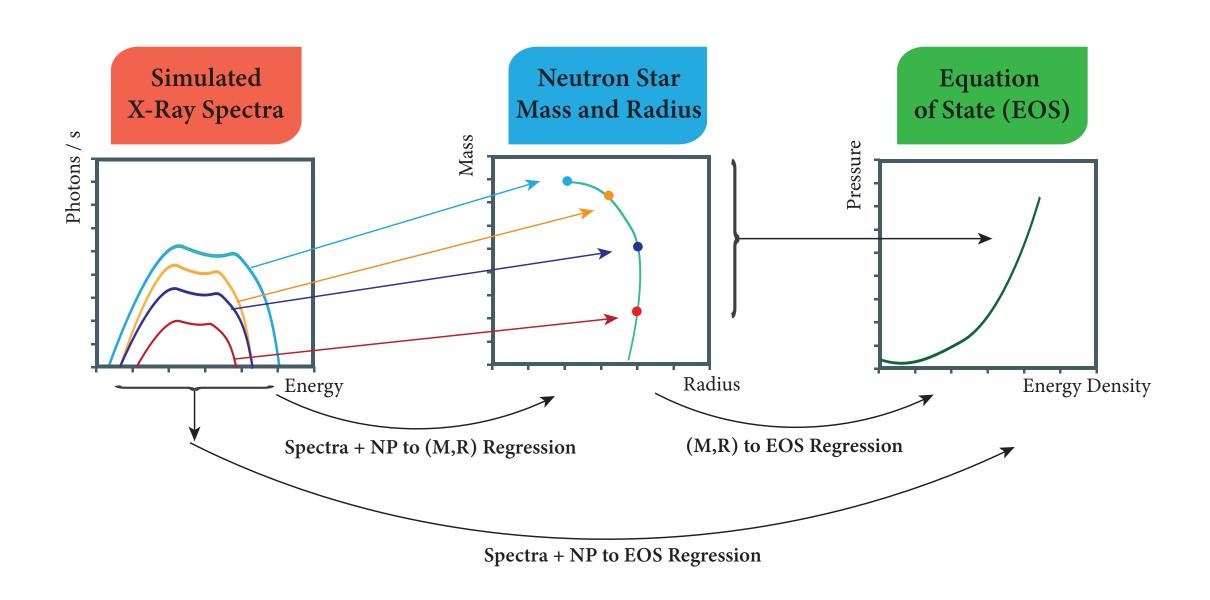
arXiv:2007.02931

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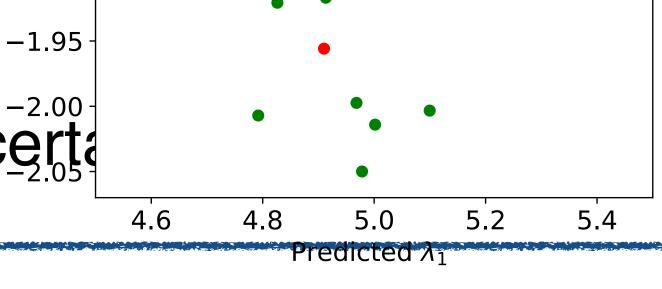
For my handwriting this is '2', for yours it might be 'a' ARM: Adapt to the individual + classify

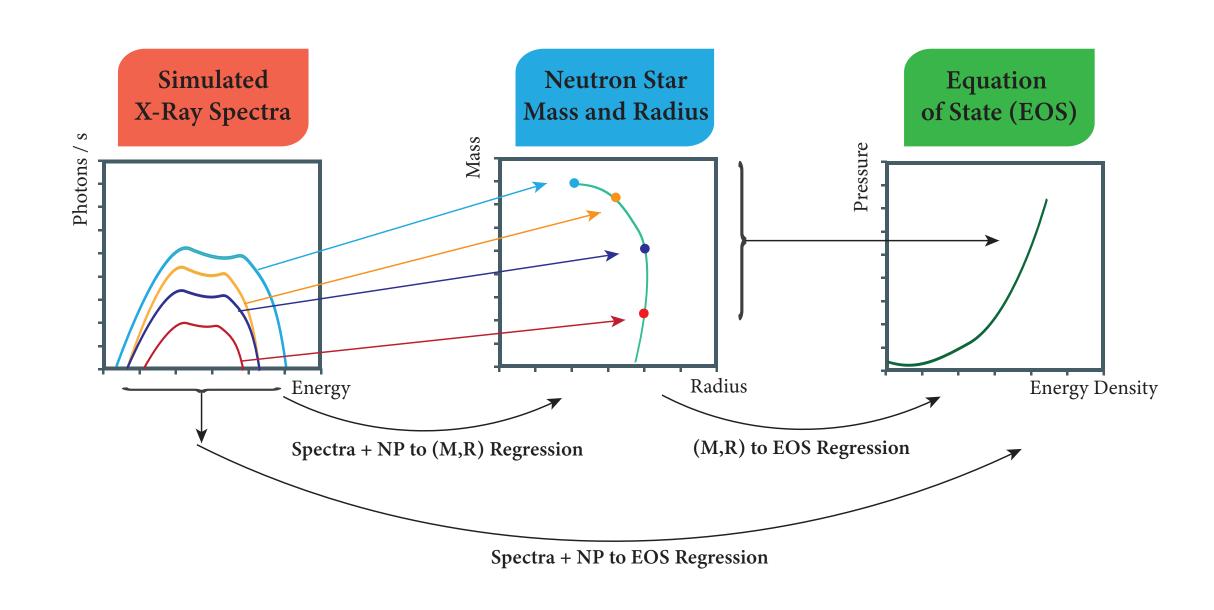
Application in Astrophysics: Propagate Uncertainties



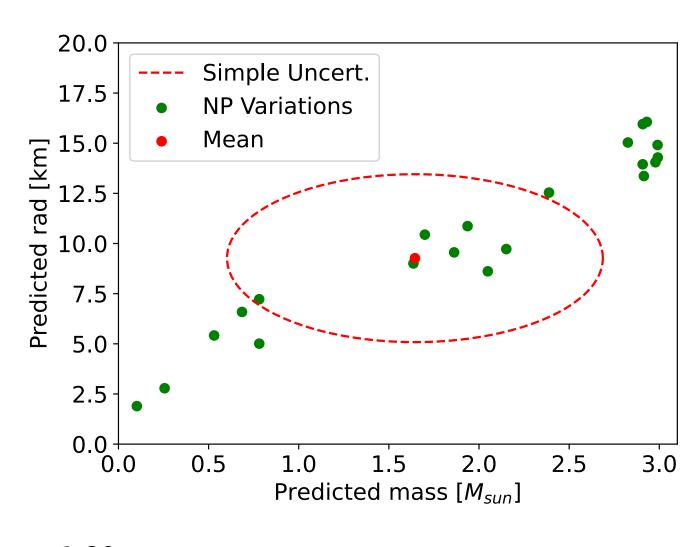
SOTA assumed uncorrelated Gaussian uncertainties

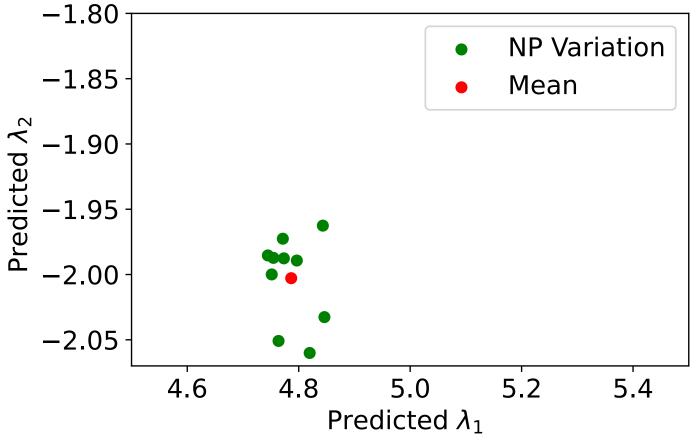
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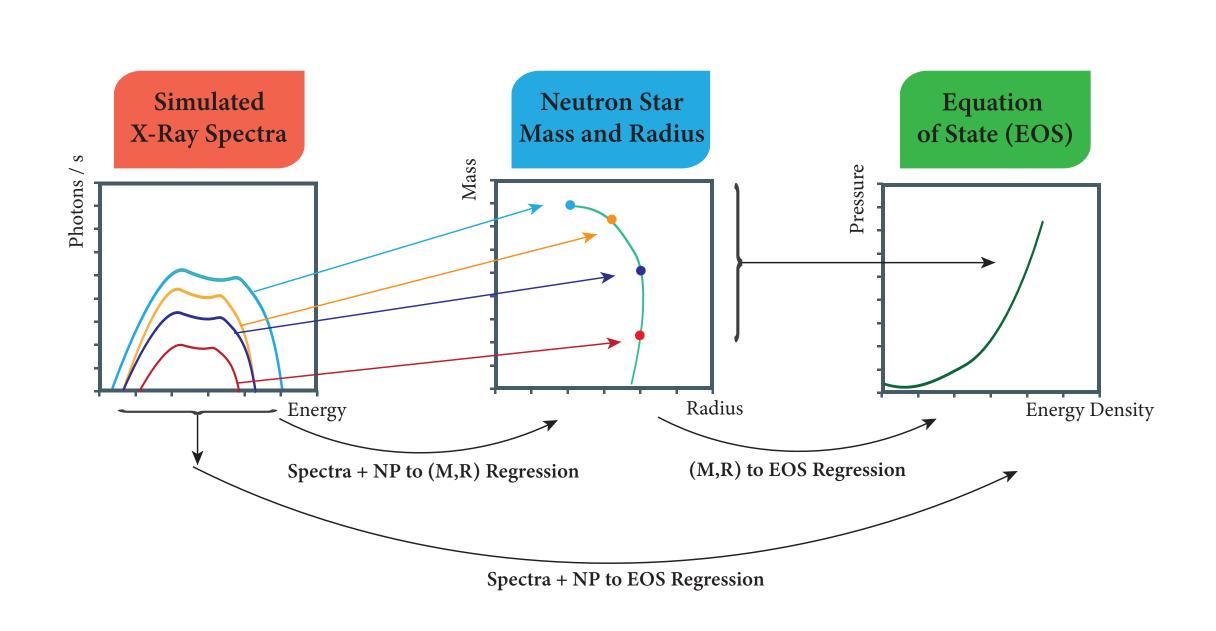


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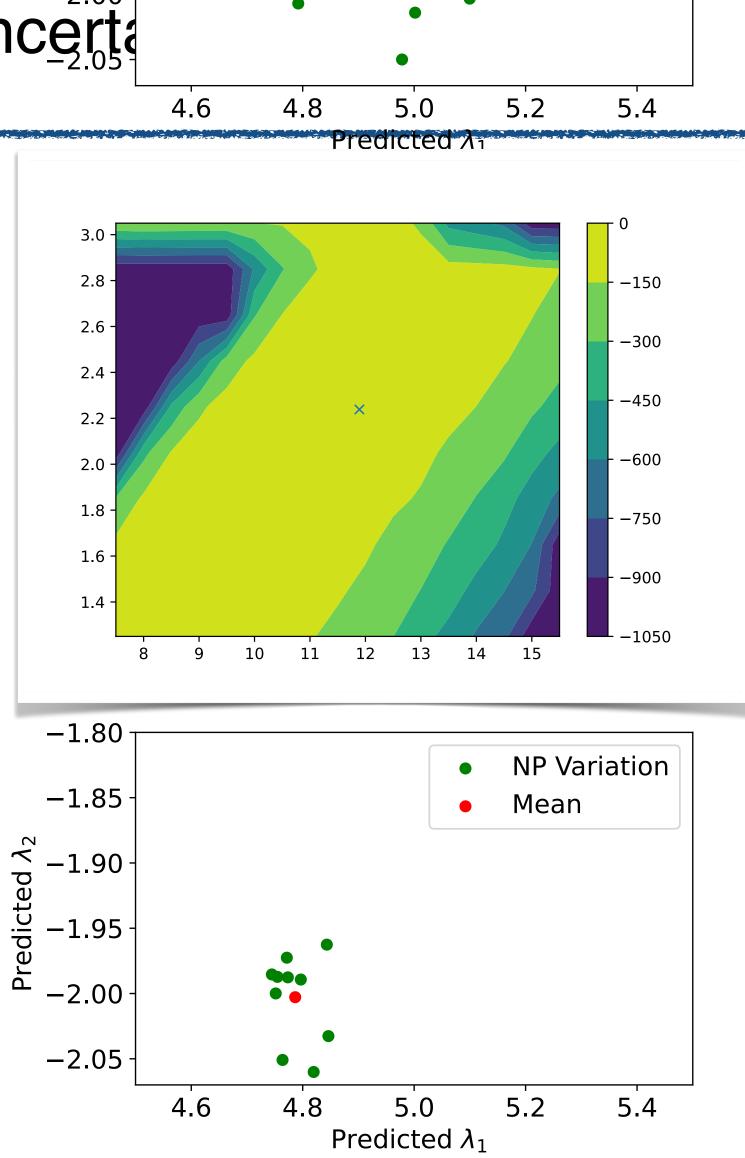




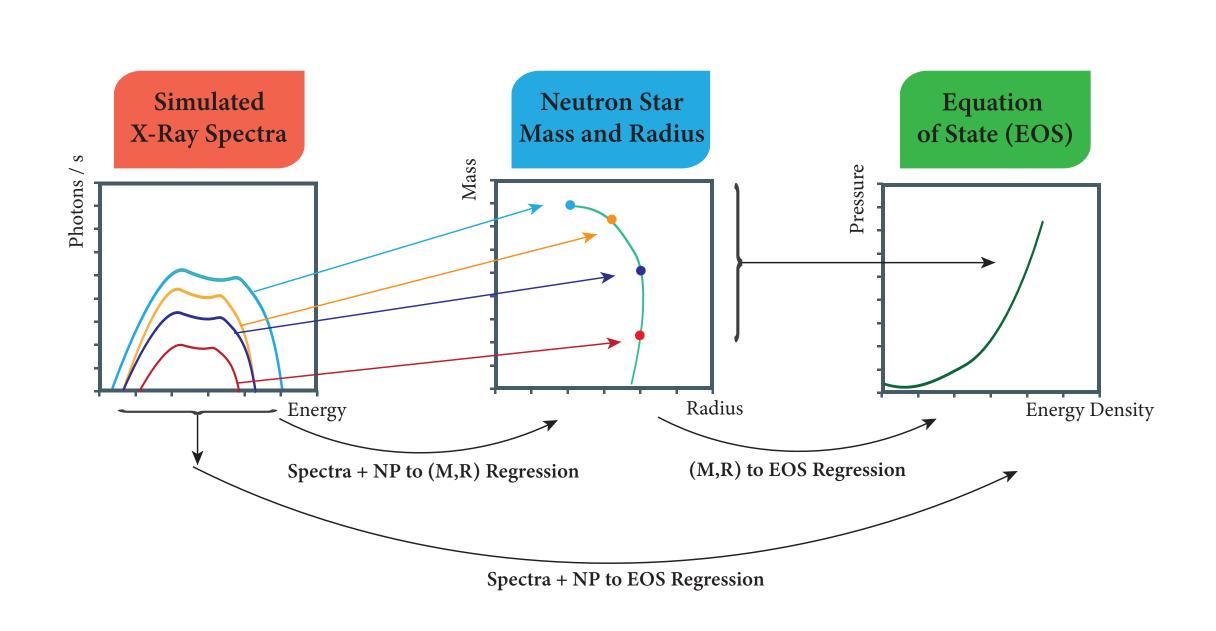
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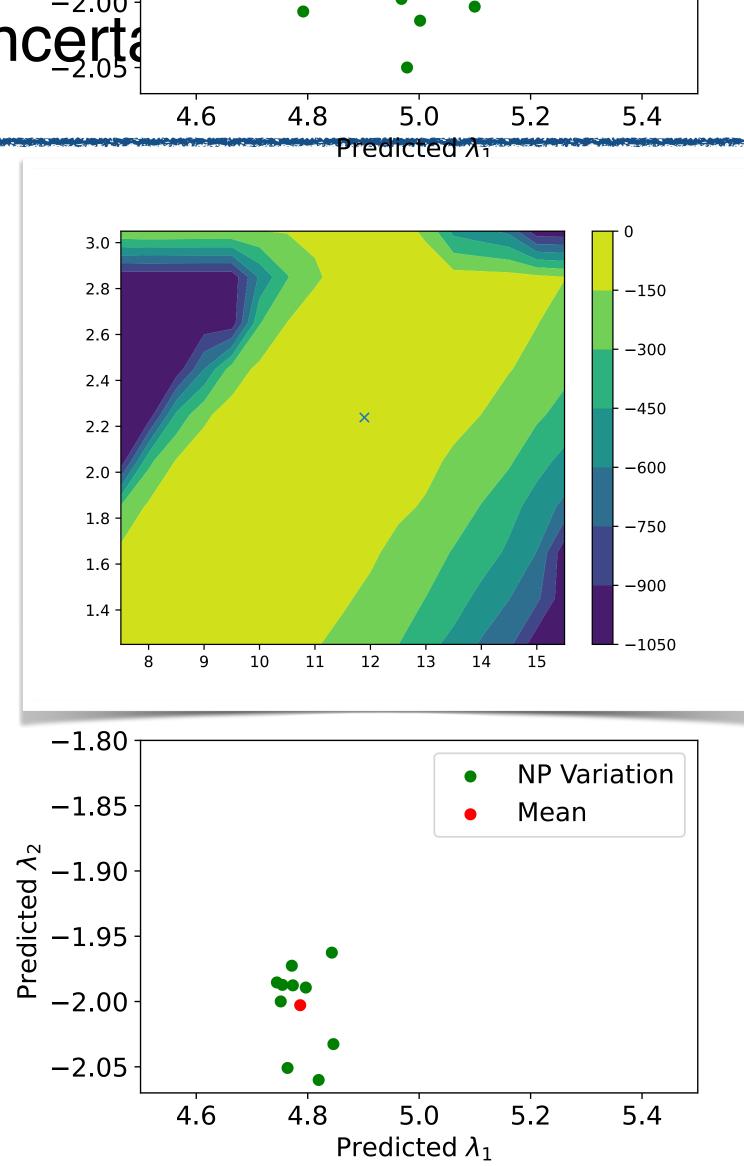


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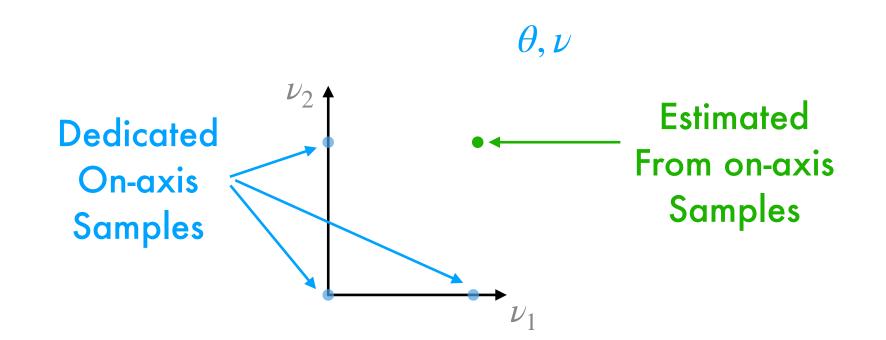
SOTA assumed uncorrelated Gaussian uncertainties

Challenge: Scan & profile over likelihood too expensive for 5×10 NPs



Challenges & Opportunities

- Train parameterised models on many NPs difficult: Need training data for full NP phase space
- Make it computationally feasible to scan & profile likelihood
- NP profiling for detector unfolding



Related ideas: arxiv:2110.00449 <u>21110.00449</u>

Estimated

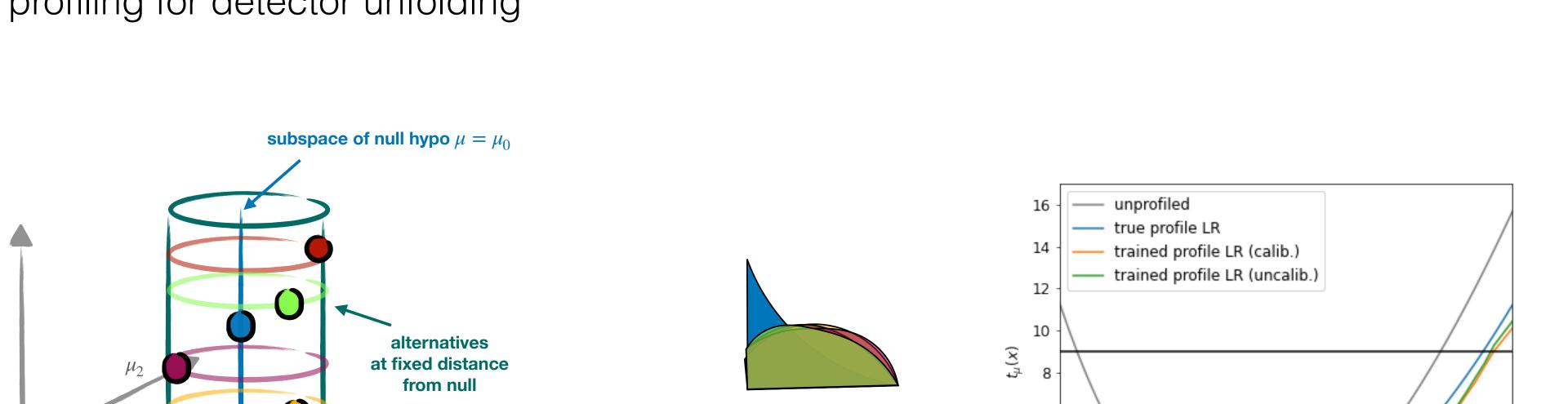
From on-axis

Samples

 θ, ν

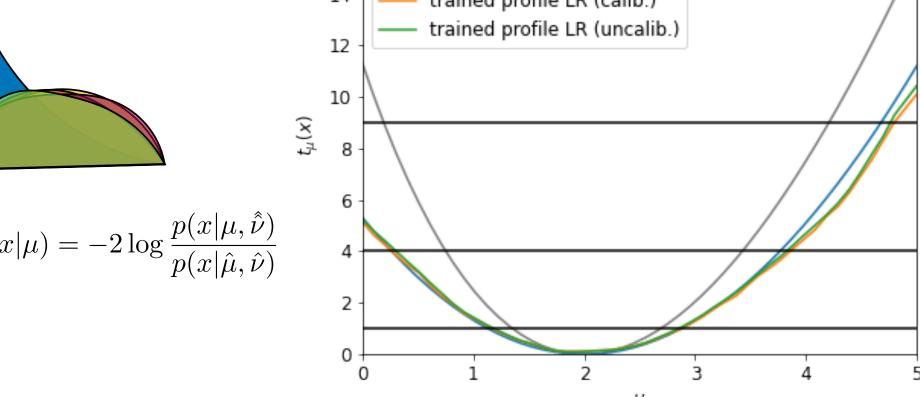
Challenges & Opportunities

- Train parameterised models on many NPs difficult: Need training data for full NP phase space
- Make it computationally feasible to scan & profile likelihood
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alternatives at fixed "radius" from the **null space**

2 POI, 1 NP



NN gives you profile likelihood directly?

Dedicated

On-axis

Samples

Challenges & Opportunities

- Train parameterised models on many NPs difficult: Need training data for full NP phase space
- Make it computationally feasible to scan & profile likelihood
- NP profiling for detector Unfolding

Fresh off the press! : Chan and Nachman arXiv:2302.05390

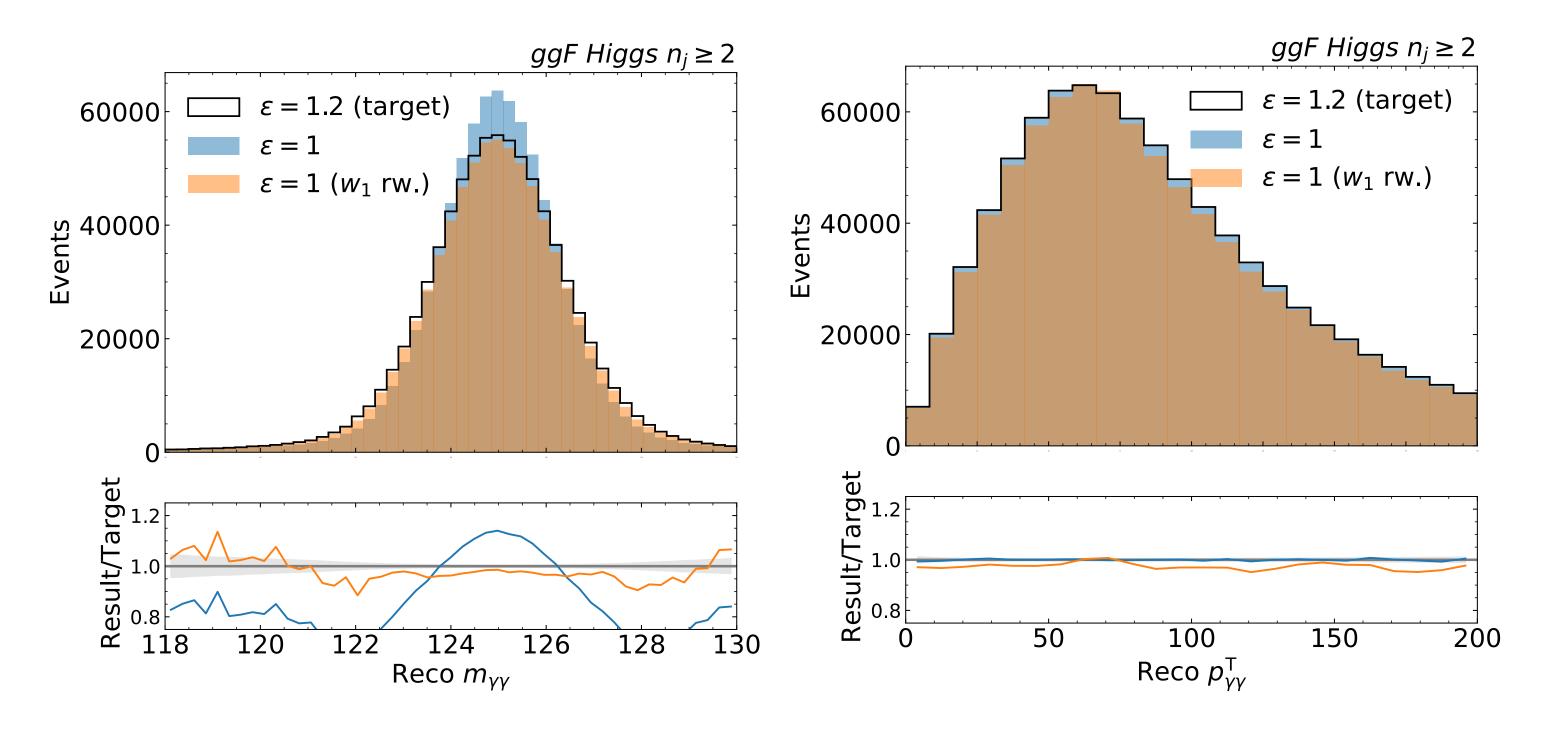
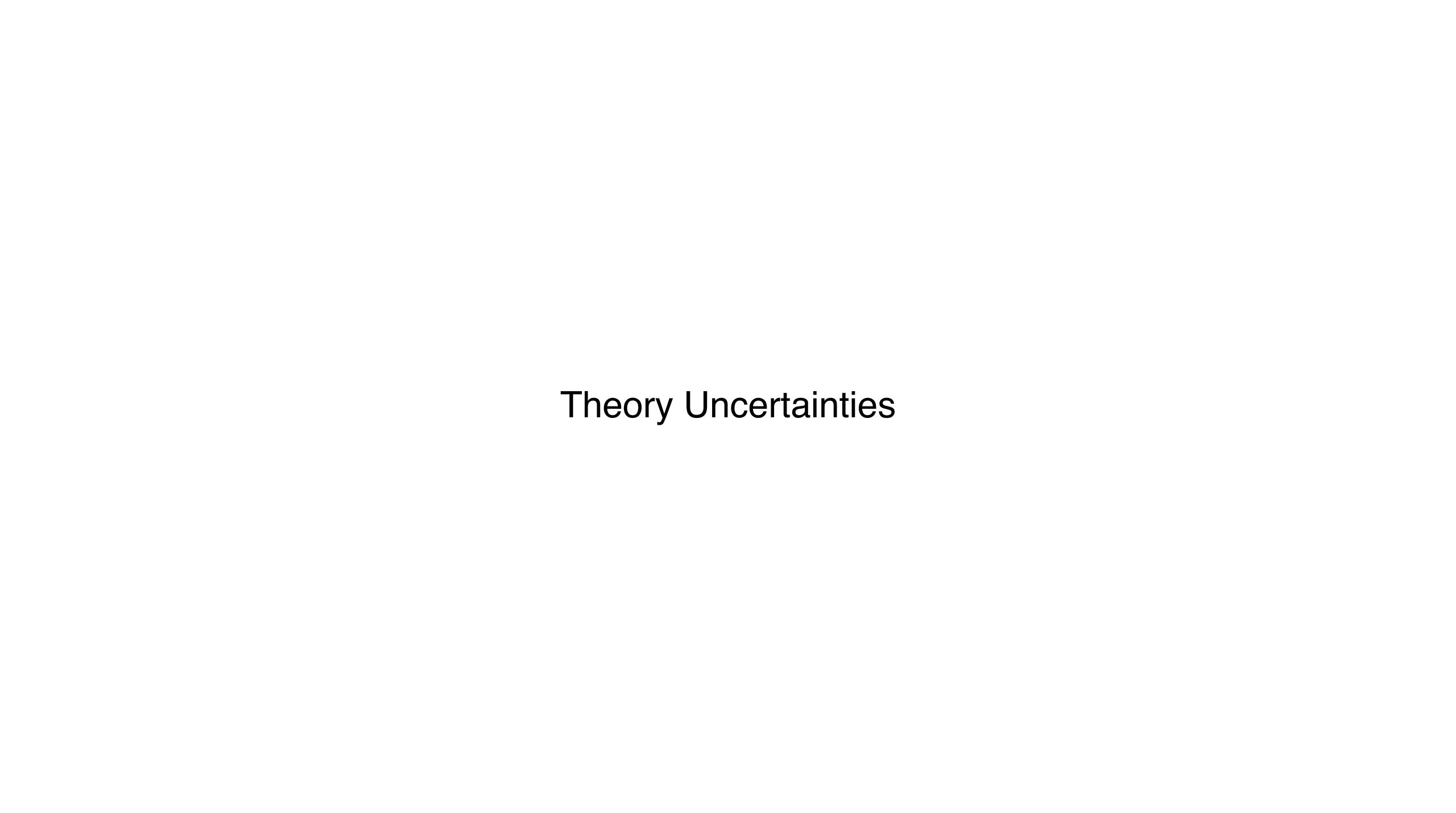


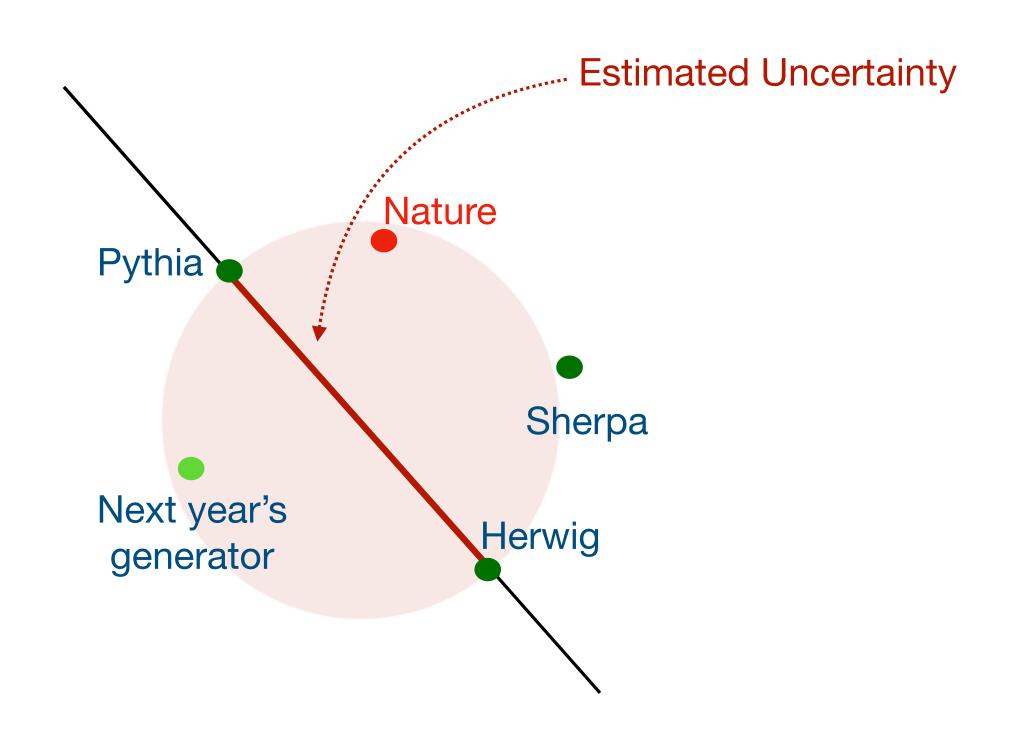
FIG. 6. Higgs boson cross section: the nominal detector-level spectra $m_{\gamma\gamma}$ (left) and $p_{\gamma\gamma}^{\rm T}$ (right) with $\epsilon_{\gamma} = 1$ reweighted by the trained w_1 conditioned at $\epsilon_{\gamma} = 1.2$ and compared to the spectra with $\epsilon_{\gamma} = 1.2$.



What are they?

Theory uncertainties often describe our <u>lack of understanding / ability to calculate</u>

No statistical origin for them (such as auxiliary measurement)



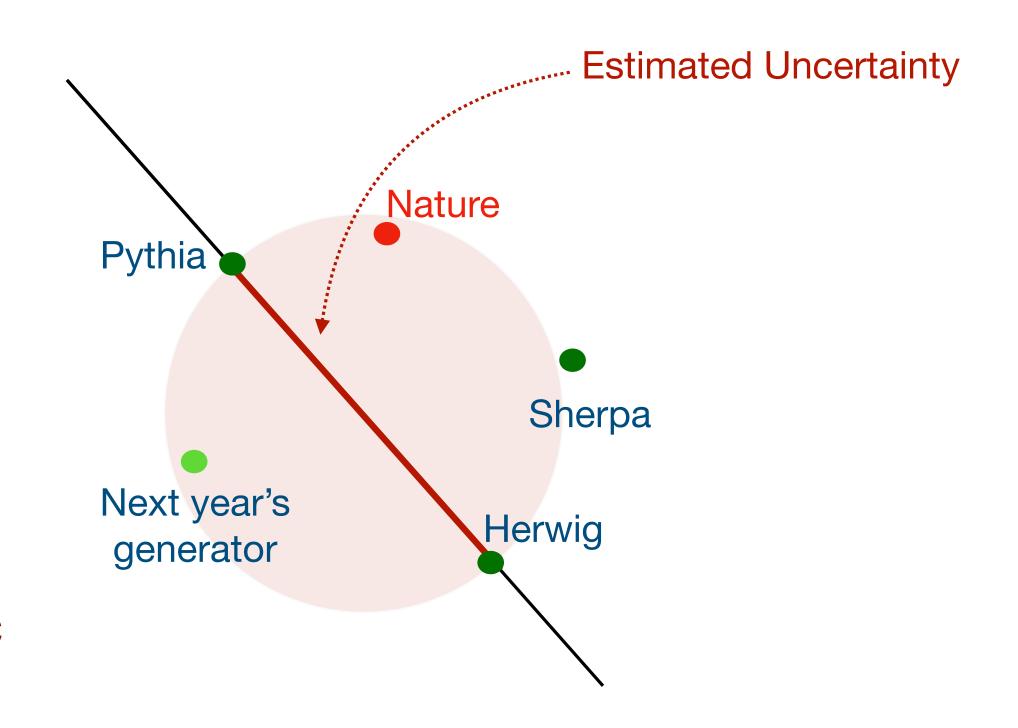
What are they?

Theory uncertainties often describe our <u>lack of understanding / ability to calculate</u>

No statistical origin for them (such as auxiliary measurement)

Eg. <u>Hadronisation</u>:

- Few different packages to simulate it
- None are correct!
- Use difference in performance of your data analysis algorithm on Pythia simulator vs Herwig simulator ad-hoc estimate of uncertainty



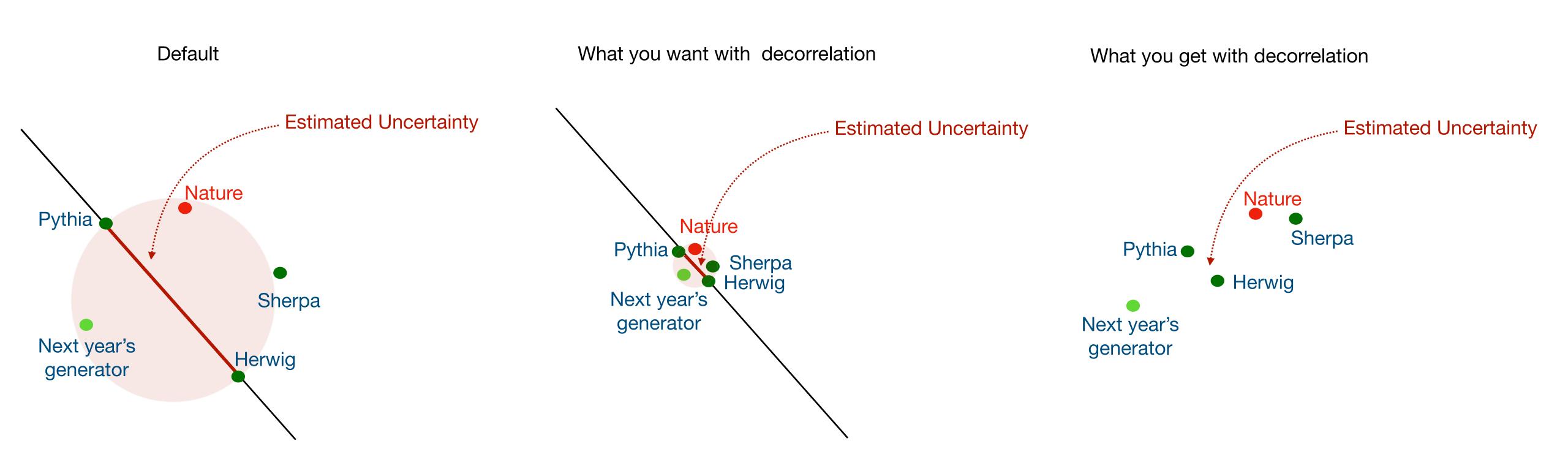
Open problems!

Not many new ideas on how to handle theory uncertainties

Besides suggestions for ML decorrelation ...

Danger of ML Decorrelation of Uncertainty

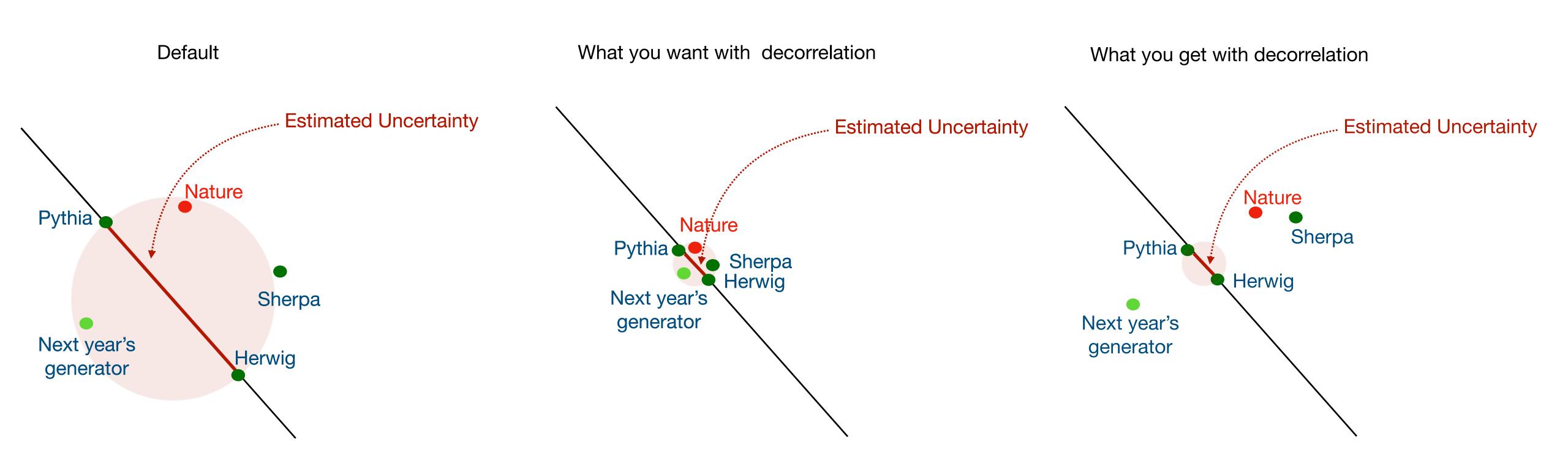
EPJC:s10052.022.10012.w: Aishik Ghosh, Benjamin Nachman



Instruction to AI: "Please shrink Pythia vs Herwig difference"

Danger of ML Decorrelation of Uncertainty

EPJC:s10052.022.10012.w: Aishik Ghosh, Benjamin Nachman



Instruction to AI: "Please shrink Pythia vs Herwig difference"

Model will learn to fool you!

Goodhart's Law

When a measure becomes a target, it ceases to be a good measure

=> Dangerous to optimise proxy metrics of uncertainty

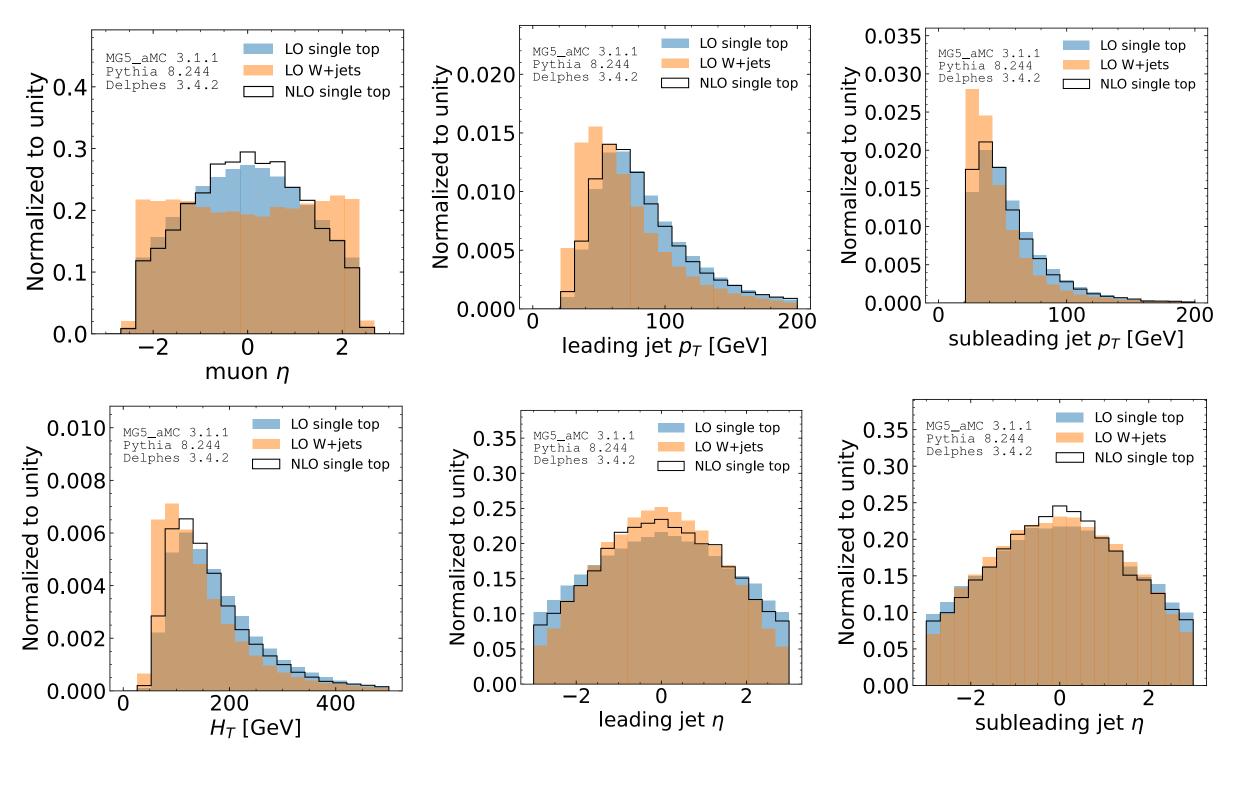
Case Study 2: Higher-order corrections

- We can't calculate QFT to infinite order
- Artefact of truncation of series: Varying certain unphysical scales changes predictions
- Uncertainty quantification: Vary scales (renormalization scale, factorisation scale) between 1/2 to 2 in MC, see change in prediction

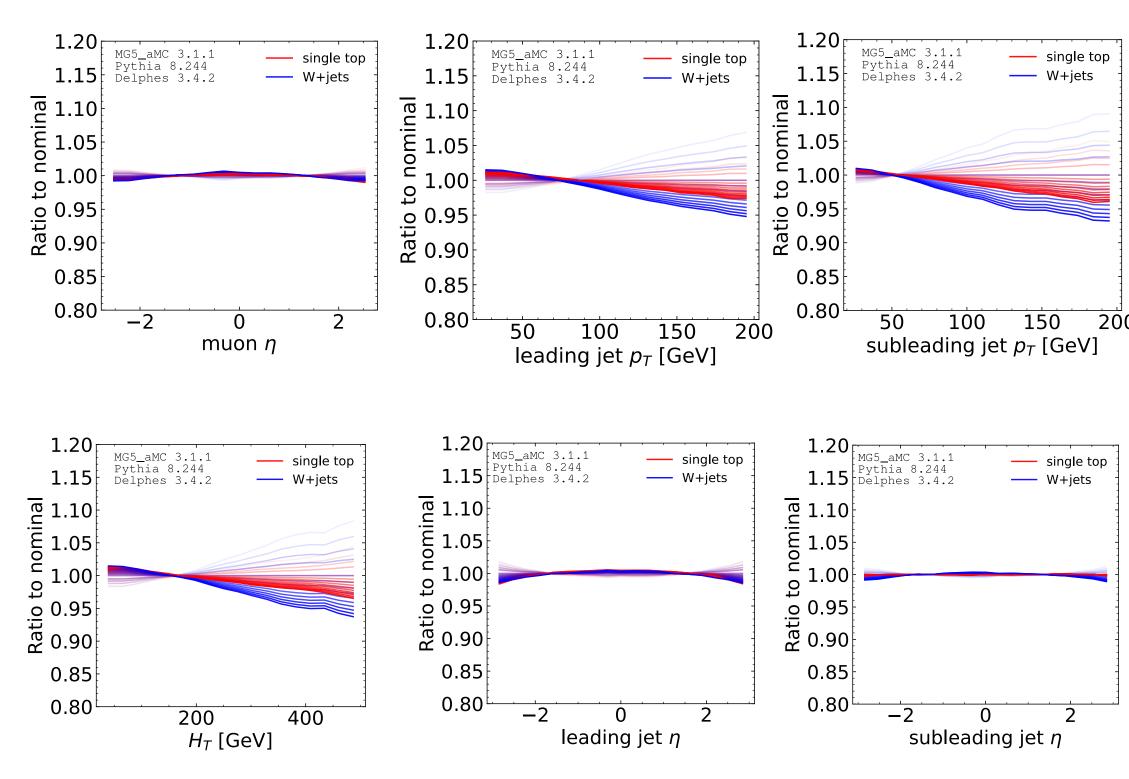
Scale uncertainty – Problem Setup

Goal: Single top vs W+Jets

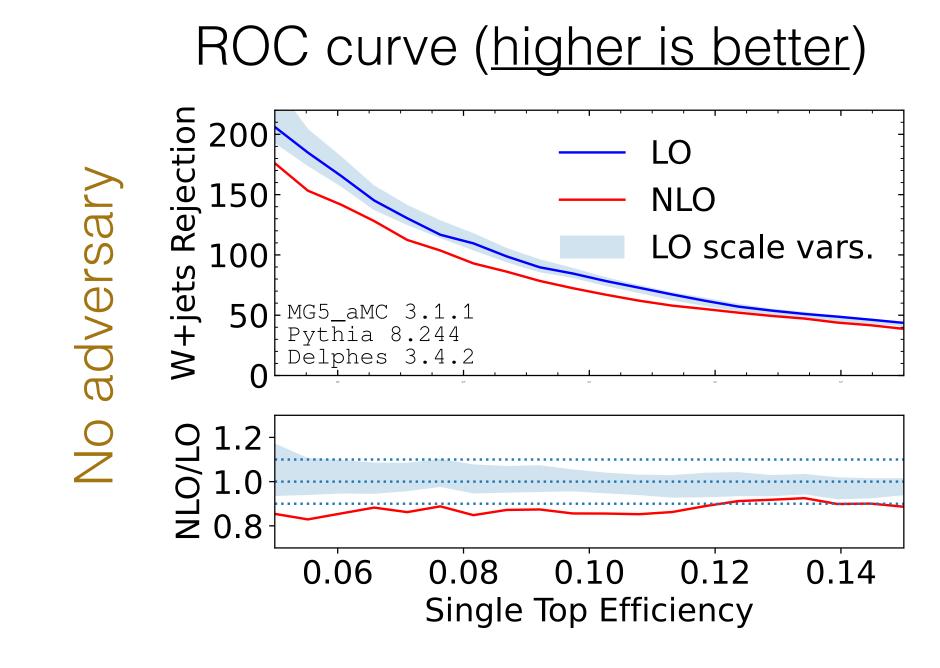
Decorrelation: Reduce difference in performance on scale variations at LO Cross-check: Test uncertainty estimate from {scale variations at LO} using NLO

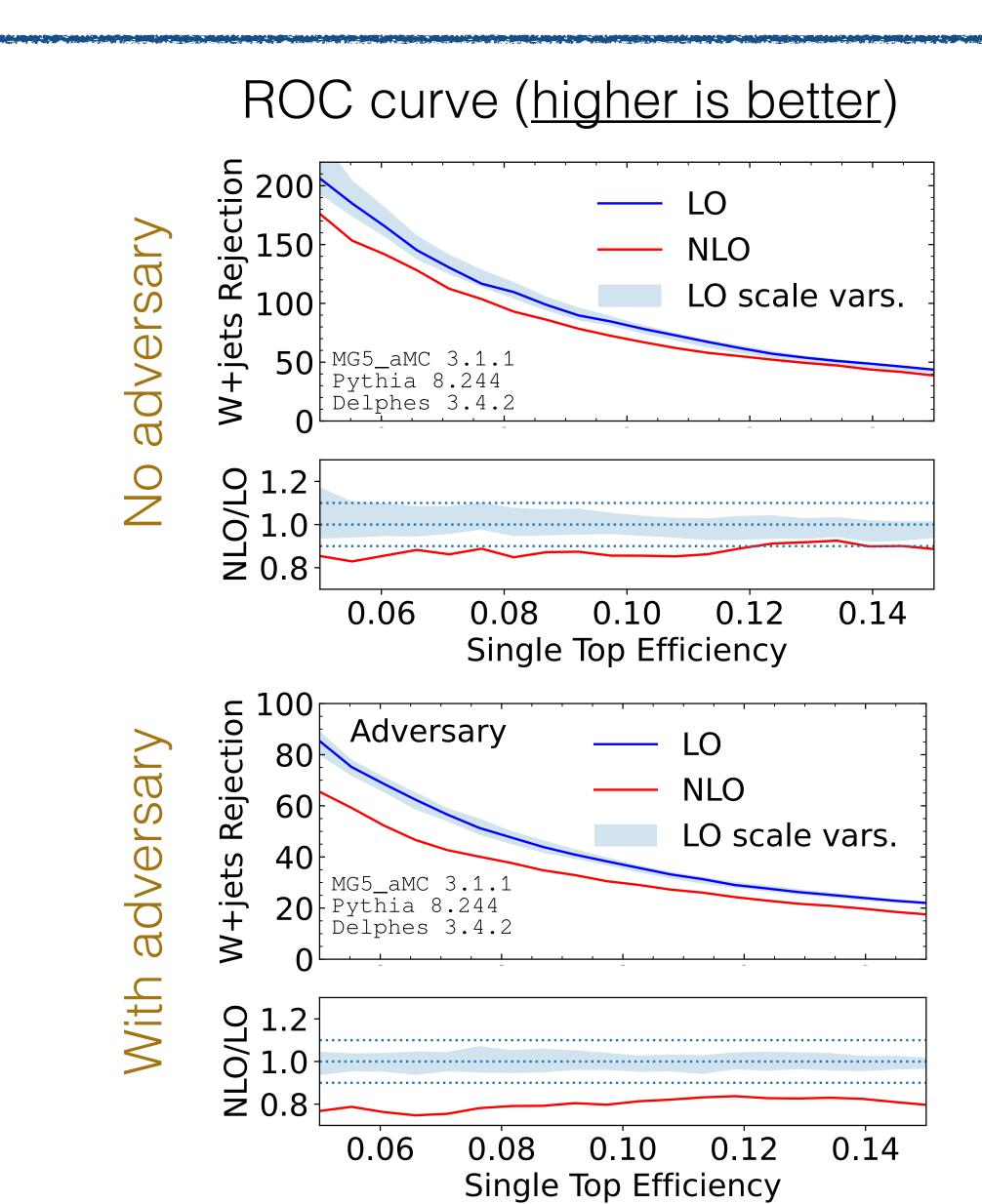


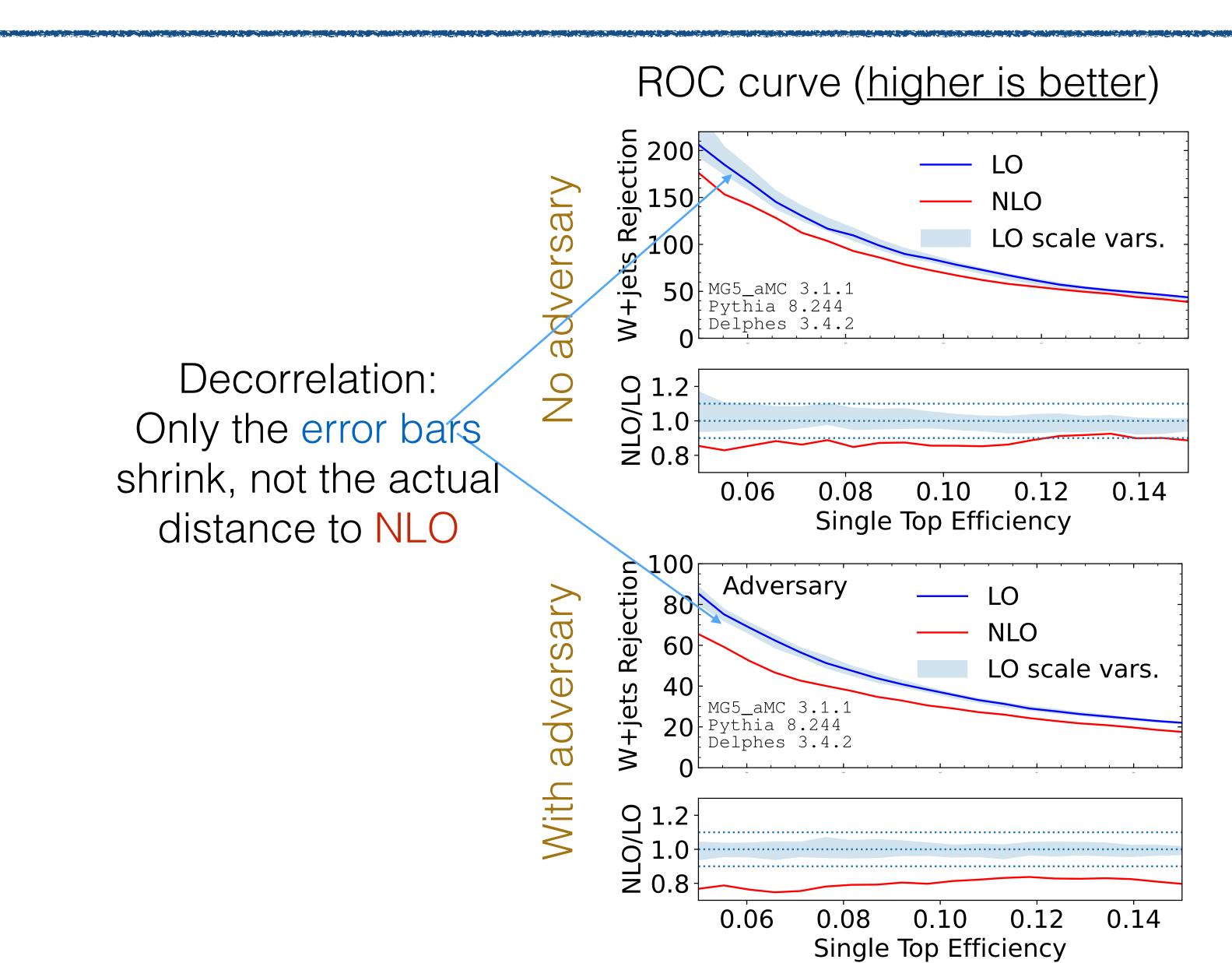
NLO vs LO



Factorisation scale variations going from 1/2 to 2





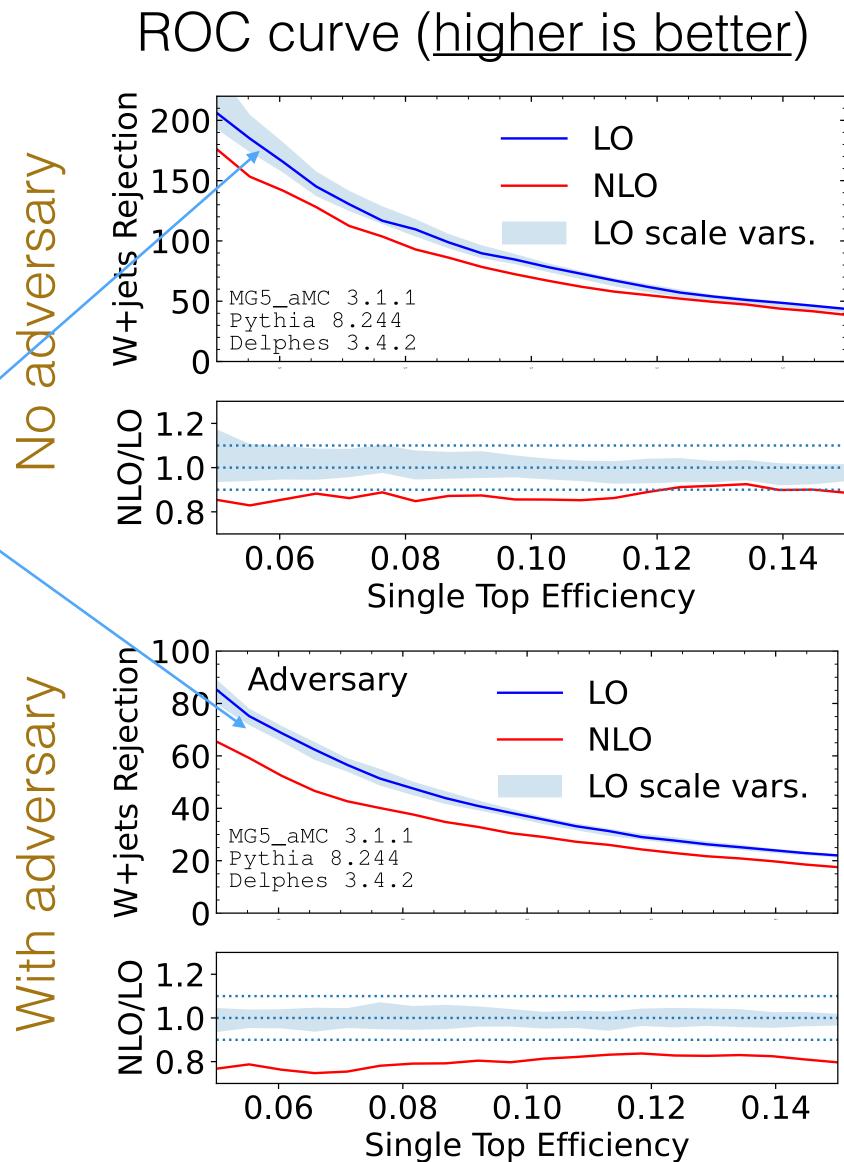


Adversary successfully <u>sacrifices</u>
separation power in order to reduce difference in performance between scale variations

Cross-check with NLO reveals <u>uncertainty</u> <u>severely underestimated</u> by decorrelation approach

In an typical LHC analysis, a cross-check with higher-order usually unavailable

Decorrelation: Only the error bars shrink, not the actual distance to NLO



If we can't decorrelate, what can we do?

If we can't decorrelate, what can we do?

Deep dive into scale uncertainties!

Scales

What is the error in cross-section due to truncation?

$$\sigma \in [\sigma_-, \sigma_+] \equiv [\sigma(\mu_{R,+}), \sigma(\mu_{R,-})]$$
,

$$\mu_0 = \frac{H_T}{2} = \frac{1}{2} \sum_{\text{final state}} \sqrt{p_T^2 + m^2}$$
 $\mu_{R,+} = 2$
 μ_0
 $\mu_{R,-} = 1/2$
 μ_0

Use dependence on scale to estimate uncertainty

Questions

- How accurate are these scale uncertainties?
- Is 1/2 to 2 a good range?
- Can we feed them into your stats package just like an experimental uncertainty?

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Use pull to examine

$$t_{\rm scale} = \frac{\sigma_{\rm NLO} - \sigma_{\rm LO}}{\Delta \sigma_{\rm LO \ scale}}$$

Critical issue:

need a large (>>10)
set of processes calculated
under identical conditions

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Madgraph paper

The automated computation of tree-level and next-to-leading order differential cross sections, and their matching to parton shower simulations

J. Alwall^a, R. Frederix^b, S. Frixione^b, V. Hirschi^c, F. Maltoni^d, O. Mattelaer^d, H.-S. Shao^e, T. Stelzer^f, P. Torrielli^g, M. Zaro^{hi}

Process		Syntax	Cross section (pb)				
Vector boson +jets			${ m LO~13~TeV}$		m NLO~13~TeV		
a.1 a.2 a.3 a.4	$pp ightarrow W^{\pm}$ $pp ightarrow W^{\pm}j$ $pp ightarrow W^{\pm}jj$ $pp ightarrow W^{\pm}jjj$	<pre>p p > wpm p p > wpm j p p > wpm j j p p > wpm j j</pre>	$1.375 \pm 0.002 \cdot 10^{5}$ $2.045 \pm 0.001 \cdot 10^{4}$ $6.805 \pm 0.015 \cdot 10^{3}$ $1.821 \pm 0.002 \cdot 10^{3}$	$\begin{array}{c} +15.4\% \ +2.0\% \\ -16.6\% \ -1.6\% \\ +19.7\% \ +1.4\% \\ -17.2\% \ -1.1\% \\ +24.5\% \ +0.8\% \\ -18.6\% \ -0.7\% \\ +41.0\% \ +0.5\% \\ -27.1\% \ -0.5\% \end{array}$	$1.773 \pm 0.007 \cdot 10^{5}$ $2.843 \pm 0.010 \cdot 10^{4}$ $7.786 \pm 0.030 \cdot 10^{3}$ $2.005 \pm 0.008 \cdot 10^{3}$	$\begin{array}{c} +5.2\% & +1.9\% \\ -9.4\% & -1.6\% \\ +5.9\% & +1.3\% \\ -8.0\% & -1.1\% \\ +2.4\% & +0.9\% \\ -6.0\% & -0.8\% \\ +0.9\% & +0.6\% \\ -6.7\% & -0.5\% \end{array}$	
a.5 a.6 a.7 a.8	$egin{aligned} pp & ightarrow Z \ pp & ightarrow Zj \ pp & ightarrow Zjj \ pp & ightarrow Zjjj \end{aligned}$	p p > z p p > z j p p > z j p p > z j j p p > z j j j	$4.248 \pm 0.005 \cdot 10^{4}$ $7.209 \pm 0.005 \cdot 10^{3}$ $2.348 \pm 0.006 \cdot 10^{3}$ $6.314 \pm 0.008 \cdot 10^{2}$	$\begin{array}{c} +14.6\% \ +2.0\% \\ -15.8\% \ -1.6\% \\ +19.3\% \ +1.2\% \\ -17.0\% \ -1.0\% \\ +24.3\% \ +0.6\% \\ -18.5\% \ -0.6\% \\ +40.8\% \ +0.5\% \\ -27.0\% \ -0.5\% \end{array}$	$5.410 \pm 0.022 \cdot 10^{4}$ $9.742 \pm 0.035 \cdot 10^{3}$ $2.665 \pm 0.010 \cdot 10^{3}$ $6.996 \pm 0.028 \cdot 10^{2}$	$\begin{array}{c} +4.6\% & +1.9\% \\ -8.6\% & -1.5\% \\ +5.8\% & +1.2\% \\ -7.8\% & -1.0\% \\ +2.5\% & +0.7\% \\ -6.0\% & -0.7\% \\ +1.1\% & +0.5\% \\ -6.8\% & -0.5\% \end{array}$	
a.9 a.10	$\begin{array}{c} pp \rightarrow \gamma j \\ pp \rightarrow \gamma jj \end{array}$	p p > a j p p > a j j	$1.964 \pm 0.001 \cdot 10^4$ $7.815 \pm 0.008 \cdot 10^3$	+31.2% +1.7% $-26.0% -1.8%$ $+32.8% +0.9%$ $-24.2% -1.2%$	$5.218 \pm 0.025 \cdot 10^4$ $1.004 \pm 0.004 \cdot 10^4$	$\begin{array}{c} +24.5\% \ +1.4\% \\ -21.4\% \ -1.6\% \\ +5.9\% \ +0.8\% \\ -10.9\% \ -1.2\% \end{array}$	

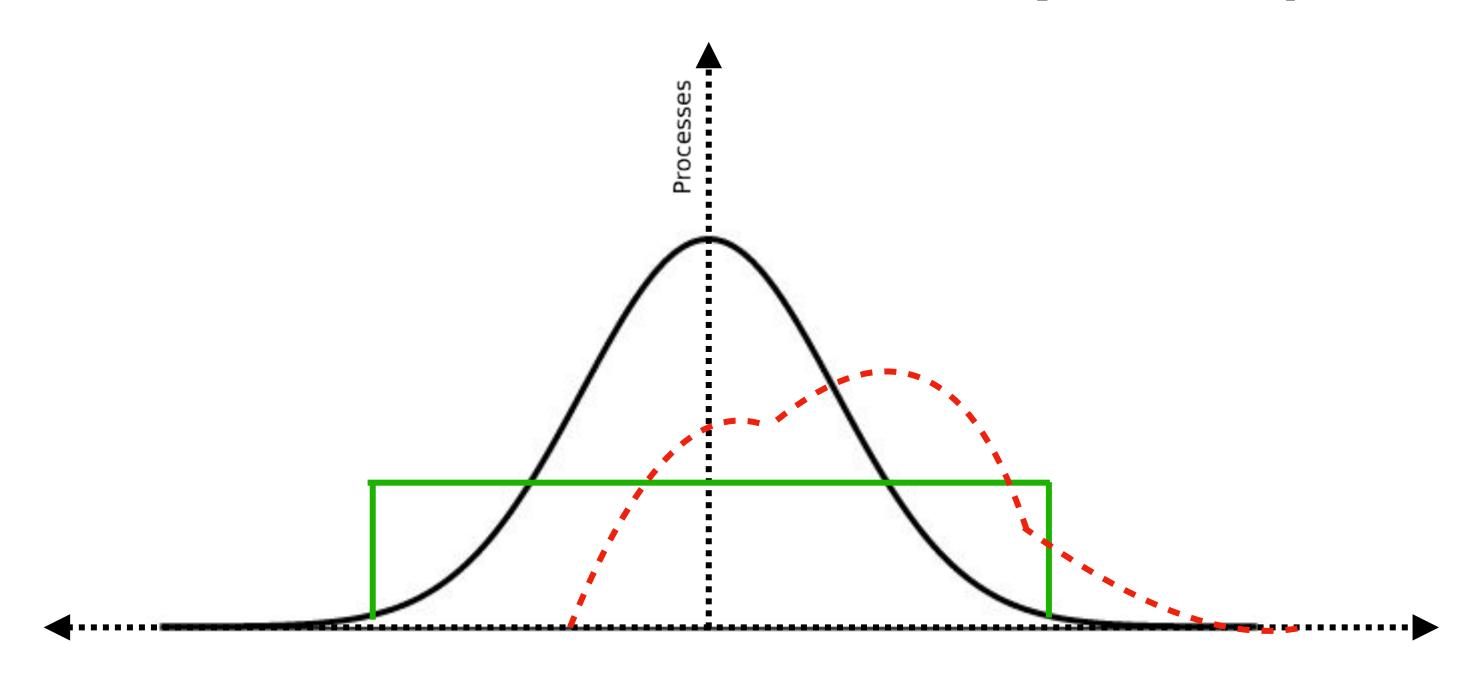
+127 more pp processes from 1405.0301!

(Not a random sampling)

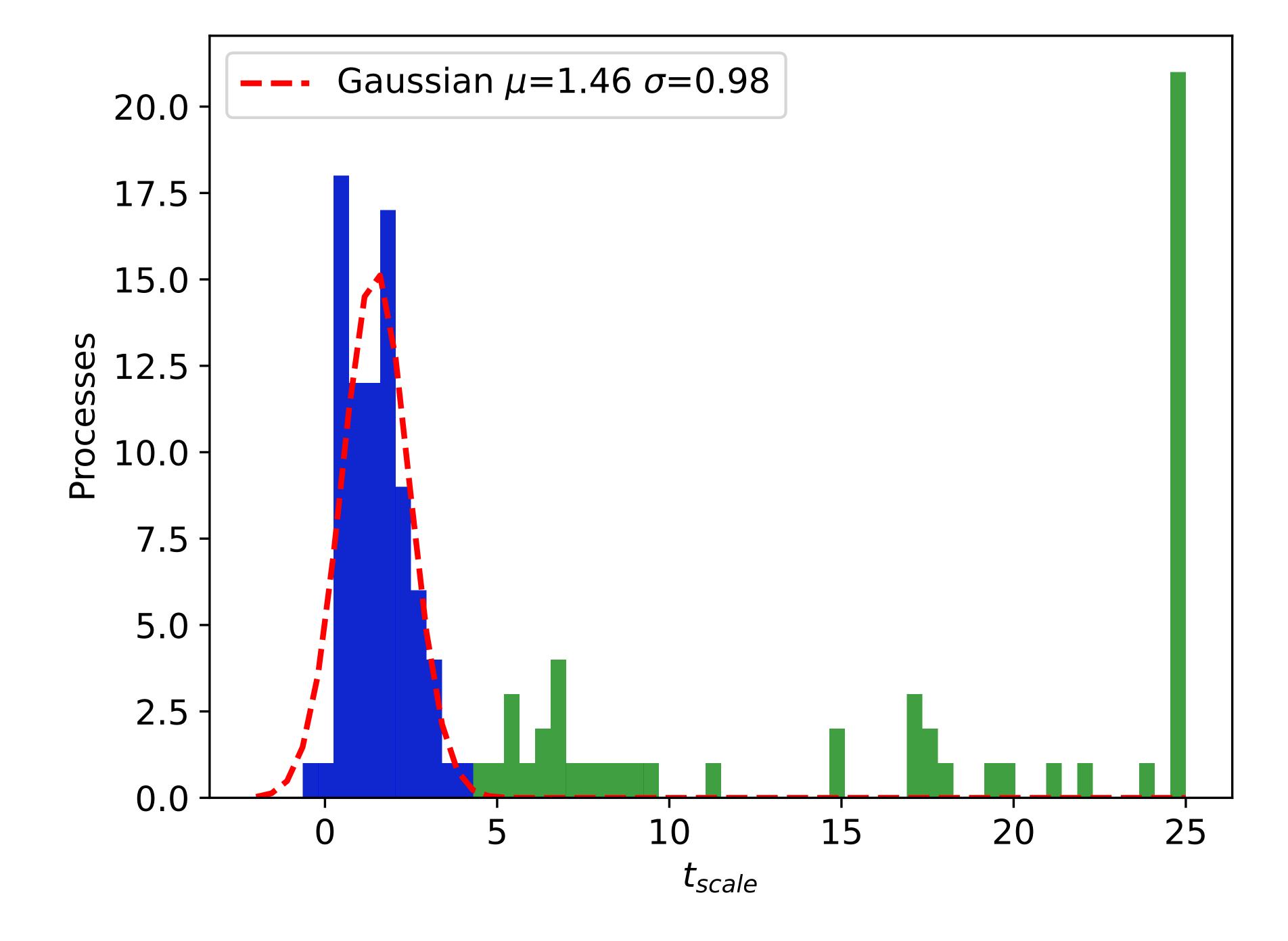
Plot the pulls

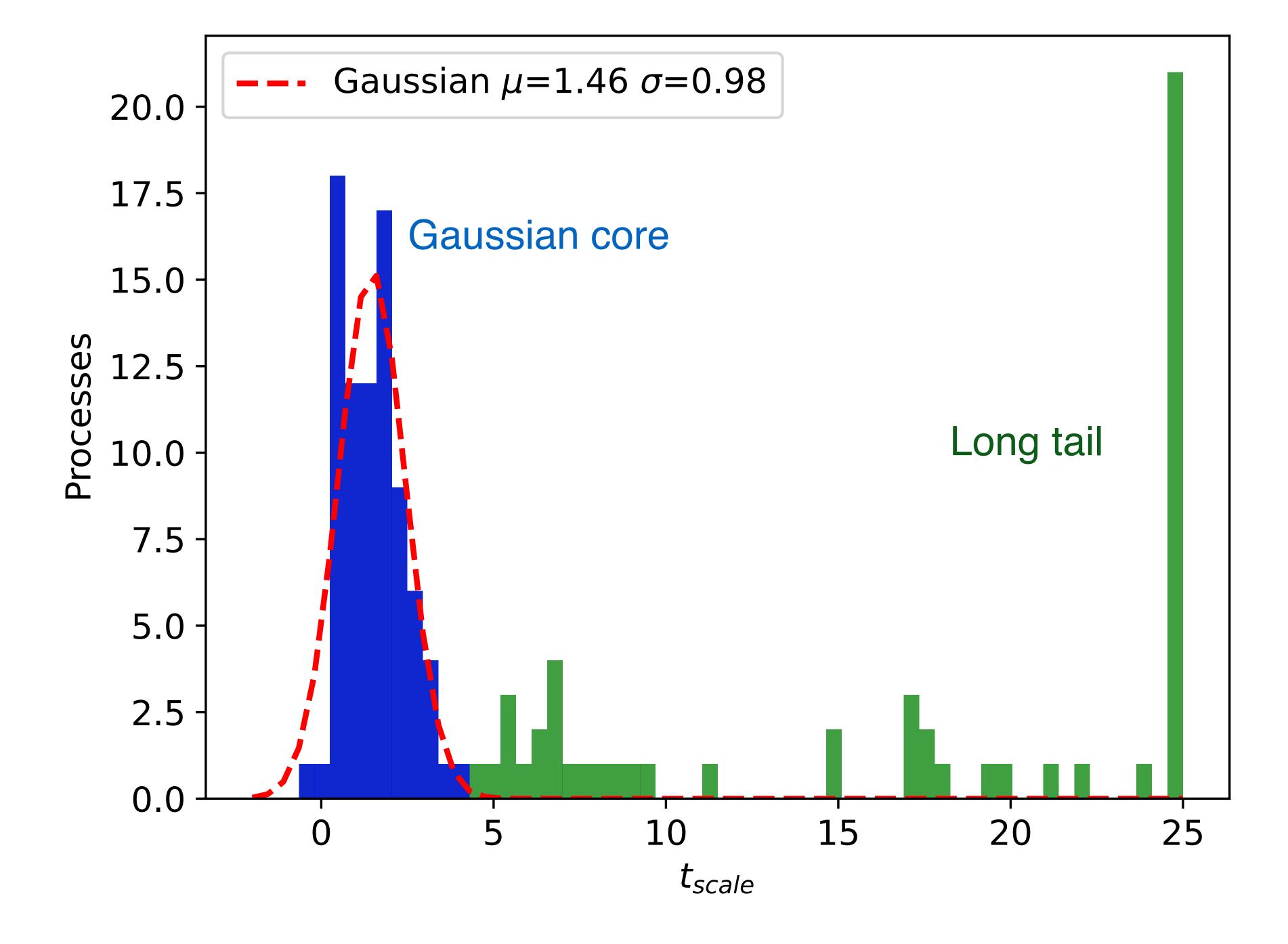
$$t_{
m scale} = rac{\sigma_{
m NLO} - \sigma_{
m LO}}{\Delta \sigma_{
m LO \ scale}}$$

Which of these distributions do you expect?



$$t_{\text{scale}} = \frac{\sigma_{\text{NLO}} - \sigma_{\text{LO}}}{\Delta \sigma_{\text{LO scale}}}$$





What processes populate the tail?

Process	$n_{ m part}$	$\Delta\sigma/\sigma_0$	$\frac{\sigma_{ m NLO} - \sigma_0}{\Delta \sigma}$
p p > wpm	1	1.54×10^{-1}	1.84
p p > wpm j	2	1.97×10^{-1}	1.96
pp > wpm j j	3	2.45×10^{-1}	0.59
pp > wpm j j j	4	4.10×10^{-1}	0.25
p p > z	1	1.46×10^{-1}	1.87
p p > z j	2	1.93×10^{-1}	1.82
pp>zjj	3	2.43×10^{-1}	0.56
pp>zjjj	4	4.08×10^{-1}	0.27
pp>aj	2	3.12×10^{-1}	5.33
рр > ајј	3	3.28×10^{-1}	0.85
p p > w + w - wpm	3	1.00×10^{-3}	610.69
p p > z w + w -	3	8.00×10^{-3}	92.39
p p > z z wpm	3	1.00×10^{-2}	85.00
p p > z z z	3	1.00×10^{-3}	302.75
p p > a w + w -	3	1.90×10^{-2}	42.33
p p > a a wpm	3	4.40×10^{-2}	47.24
p p > a z wpm	3	1.00×10^{-3}	1244.49
p p > a z z	3	2.00×10^{-2}	17.24

QCD processes follow (an expected) pattern

Table 1: Scale dependence for LHC processes with only QCD particles in the final state. For each process, we report the relative scale uncertainty, the number of final state particles, and the per-particle relative scale uncertainty.

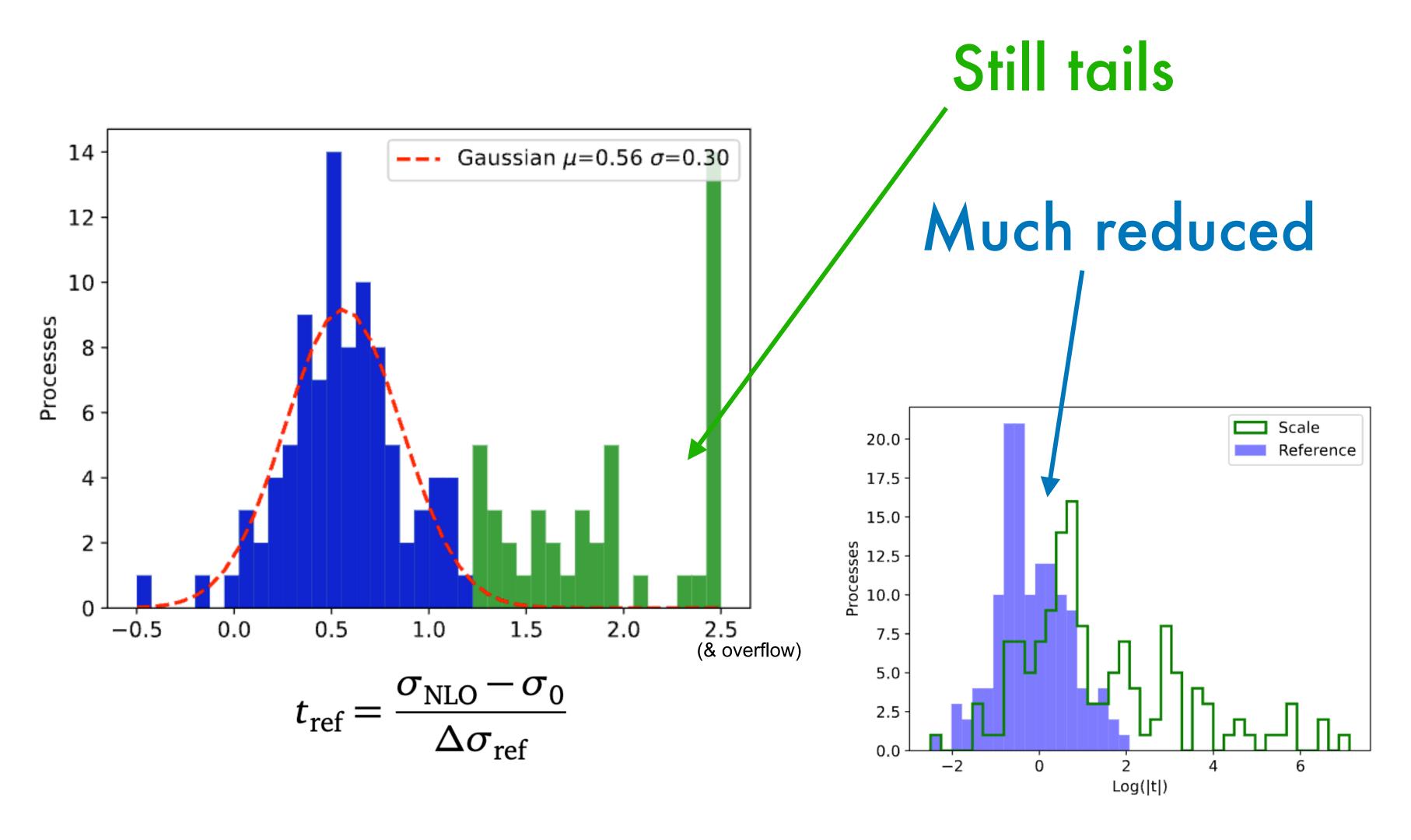
QCD processes follow (an expected) pattern

Process	$\frac{\Delta\sigma}{\sigma_0}$	n	$\frac{\Delta\sigma}{n\sigma_0}$
p p > j j p p > b b p p > t t p p > j j j p p > b b j p p > t t j p p > b b j j p p > t t j j p p > t t t j p p > t t t b b	$ \begin{vmatrix} +2.49 \times 10^{-1} & -1.88 \times 10^{-1} \\ +2.52 \times 10^{-1} & -1.89 \times 10^{-1} \\ +2.90 \times 10^{-1} & -2.11 \times 10^{-1} \\ +4.38 \times 10^{-1} & -2.84 \times 10^{-1} \\ +4.41 \times 10^{-1} & -2.85 \times 10^{-1} \\ +4.51 \times 10^{-1} & -2.90 \times 10^{-1} \\ +6.18 \times 10^{-1} & -3.56 \times 10^{-1} \\ +6.17 \times 10^{-1} & -3.56 \times 10^{-1} \\ +6.14 \times 10^{-1} & -3.56 \times 10^{-1} \\ +6.38 \times 10^{-1} & -3.65 \times 10^{-1} \\ +6.21 \times 10^{-1} & -3.57 \times 10^{-1} \end{vmatrix} $	2 2 3 3 4 4 4 4 4	$+1.24 \times 10^{-1} -9.40 \times 10^{-2}$ $+1.26 \times 10^{-1} -9.45 \times 10^{-2}$ $+1.45 \times 10^{-1} -1.06 \times 10^{-1}$ $+1.46 \times 10^{-1} -9.47 \times 10^{-2}$ $+1.47 \times 10^{-1} -9.50 \times 10^{-2}$ $+1.50 \times 10^{-1} -9.67 \times 10^{-2}$ $+1.54 \times 10^{-1} -8.90 \times 10^{-2}$ $+1.53 \times 10^{-1} -8.90 \times 10^{-2}$ $+1.60 \times 10^{-1} -9.12 \times 10^{-2}$ $+1.55 \times 10^{-1} -8.93 \times 10^{-2}$ $+1.47 \times 10^{-1} -9.34 \times 10^{-2}$
average			+1.4/ × 10

Table 1: Scale dependence for LHC processes with only QCD particles in the final state. For each process, we report the relative scale uncertainty, the number of final state particles, and the per-particle relative scale uncertainty.

$$\frac{\Delta\sigma_{\text{ref}}}{\sigma_0} = n \times \left\langle \frac{\Delta\sigma}{n\sigma_0} \right\rangle_{\text{QCD}}$$

Make correction in UQ for FIV processes



Tilman Plehn's 'reference process' method

Follow up, open questions

Would be even more interesting to repeat study for NLO → NNLO

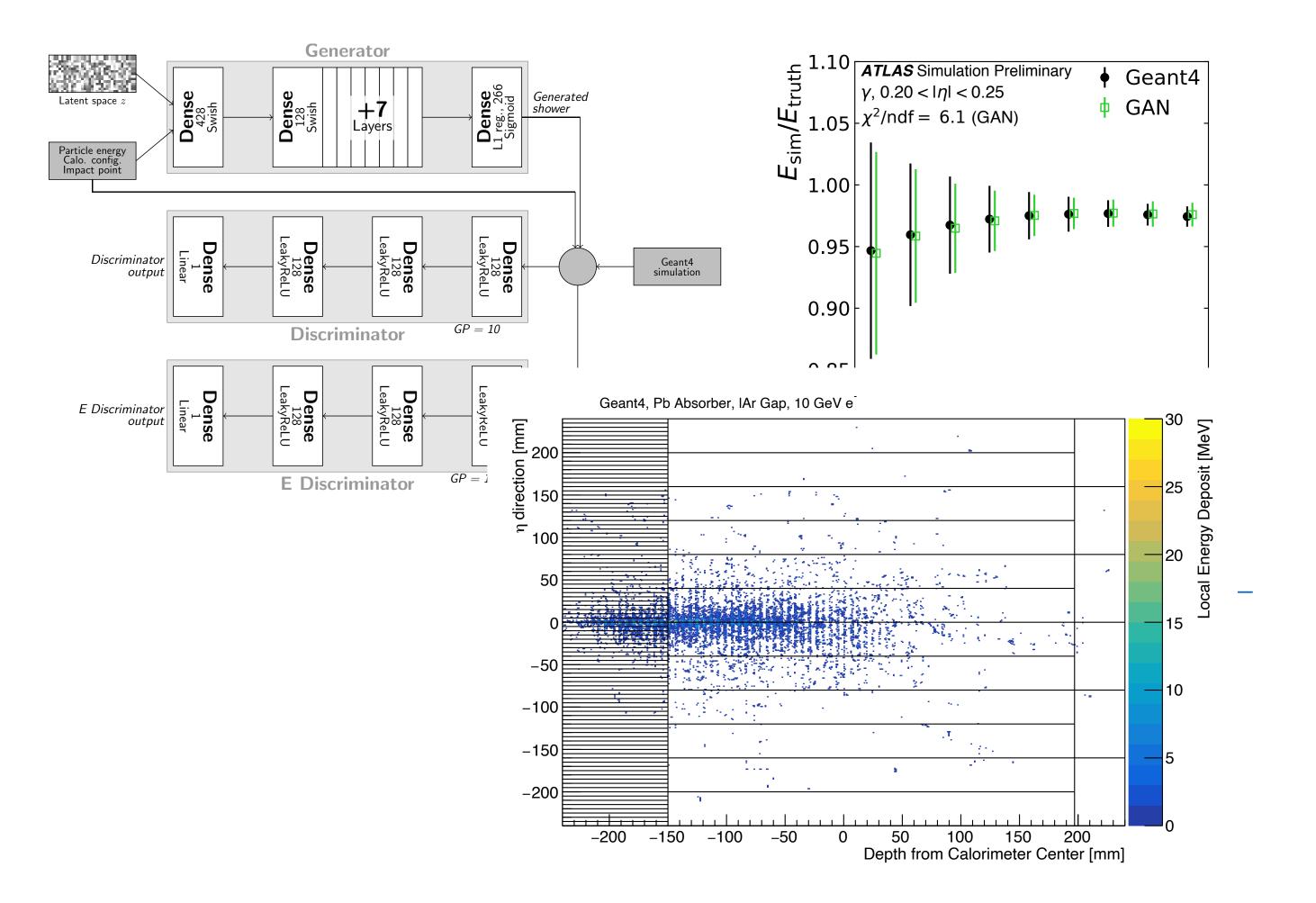
Can we use ML to automatically find patterns of failure?

Why did we find a Gaussian-ish core?

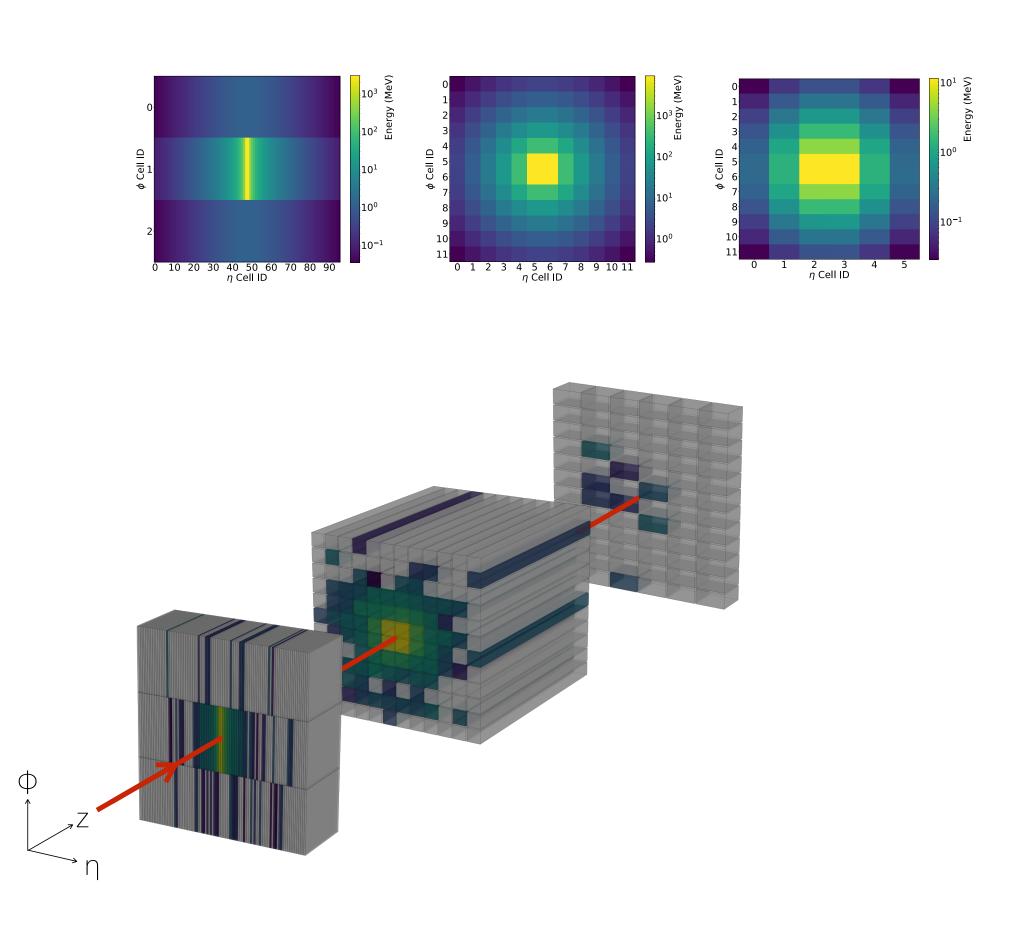
Quantifying Metrics for Generative Models

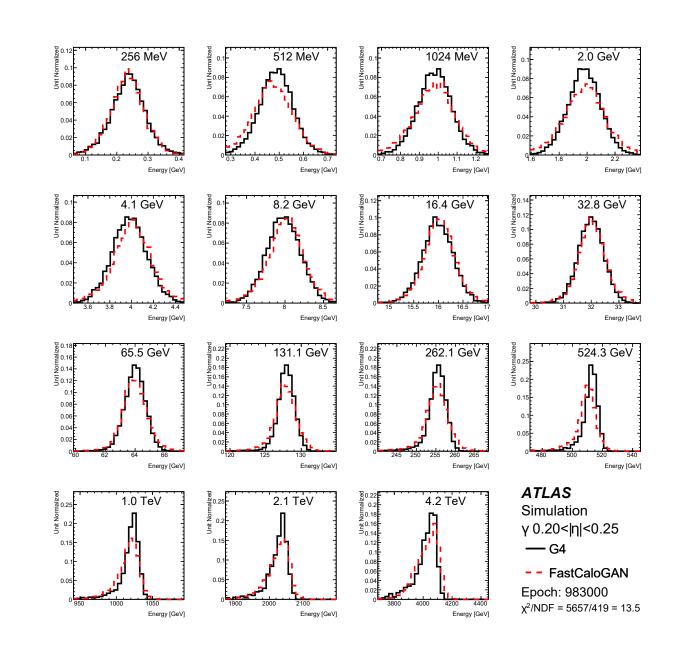
Generative Models for Simulation

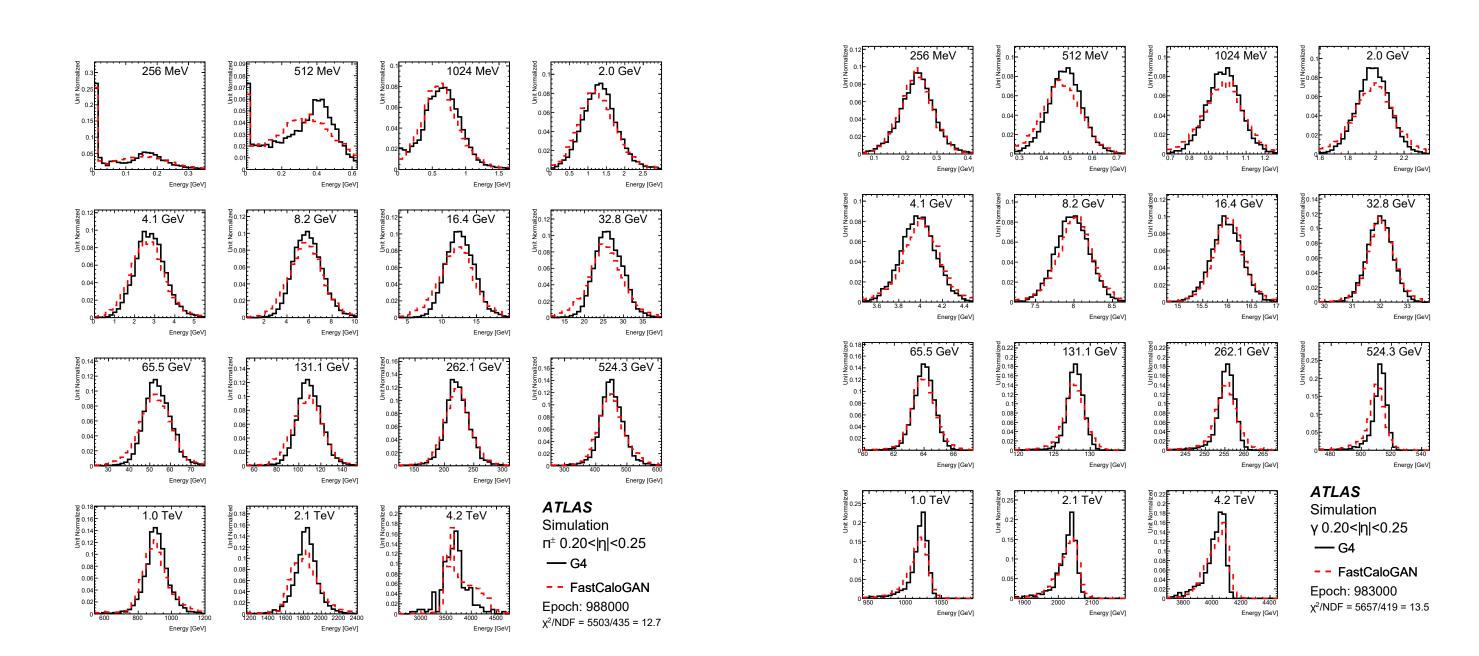
Ghosh, ATLAS Collaboration, 2019

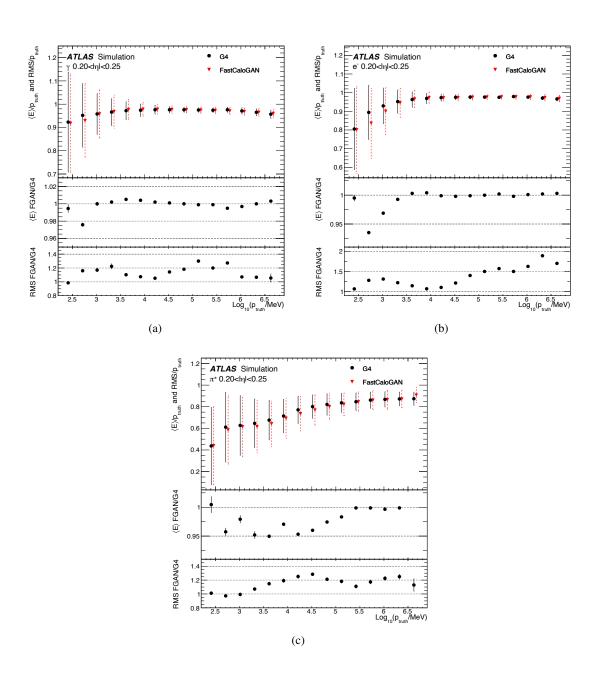


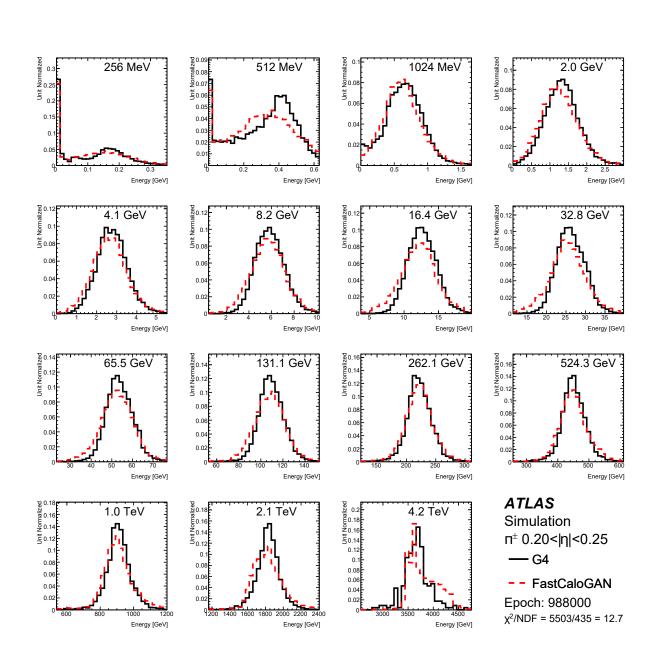
Paganini et al.

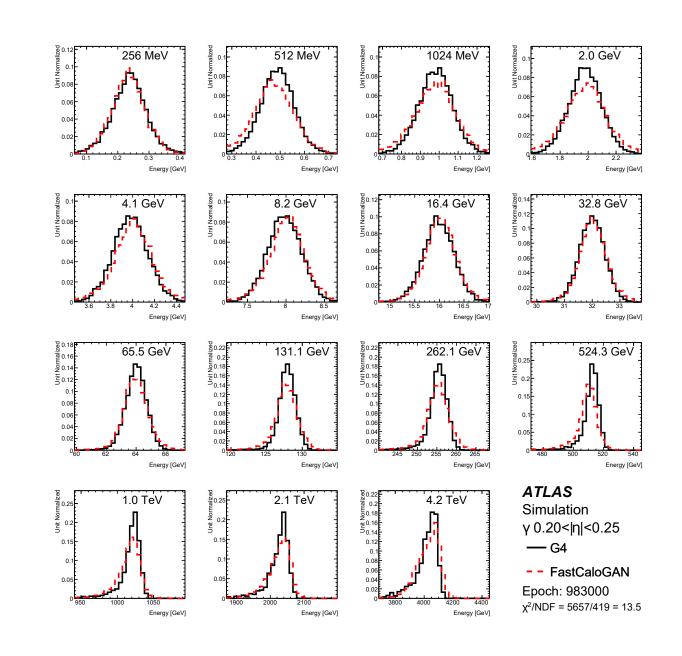


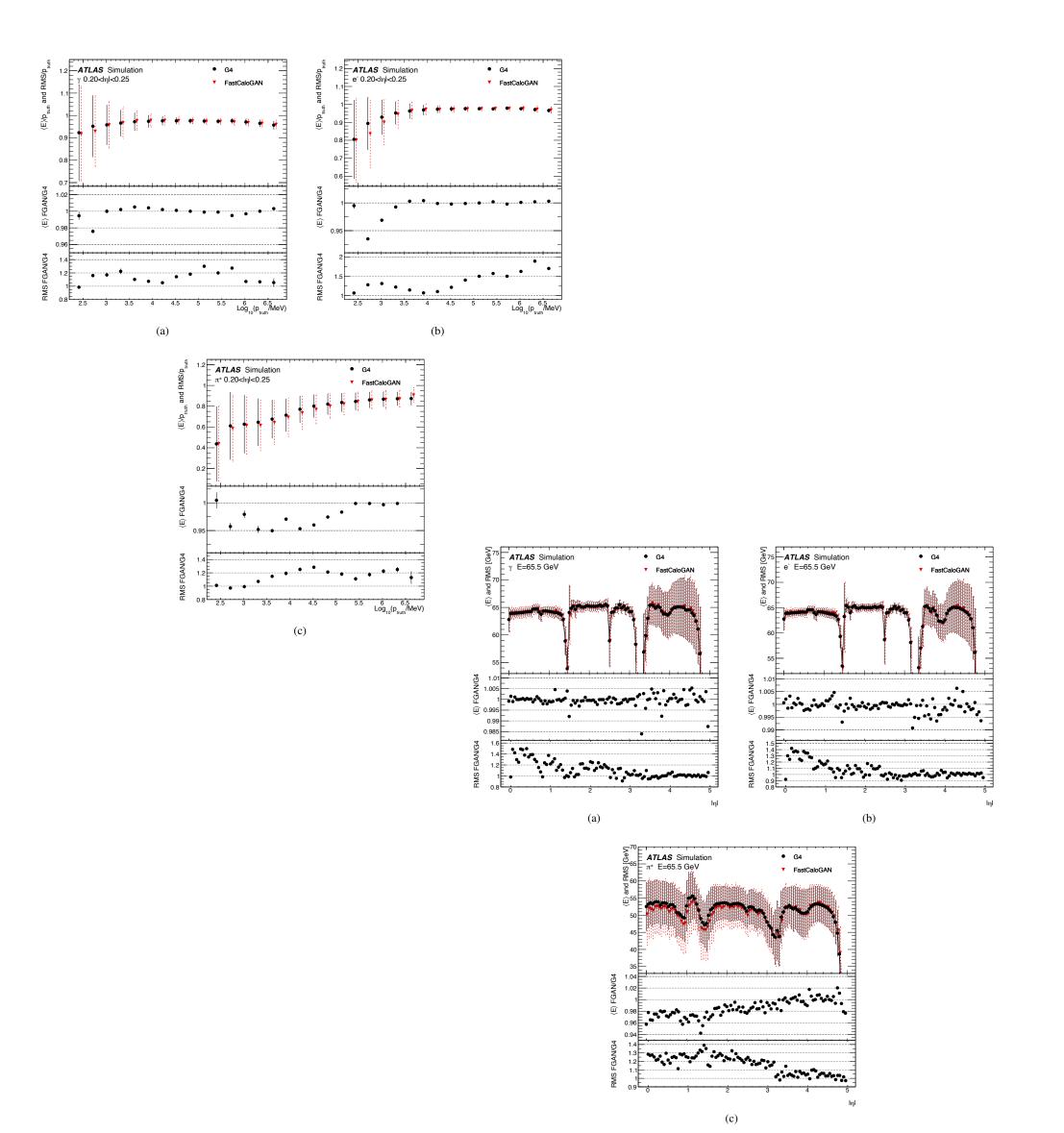


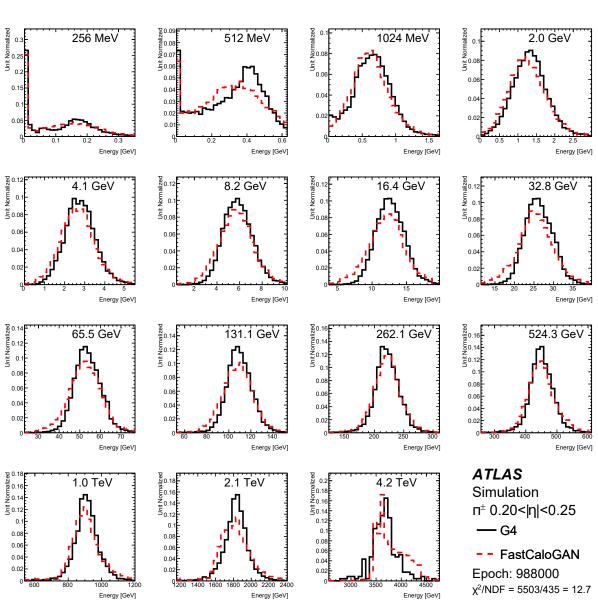


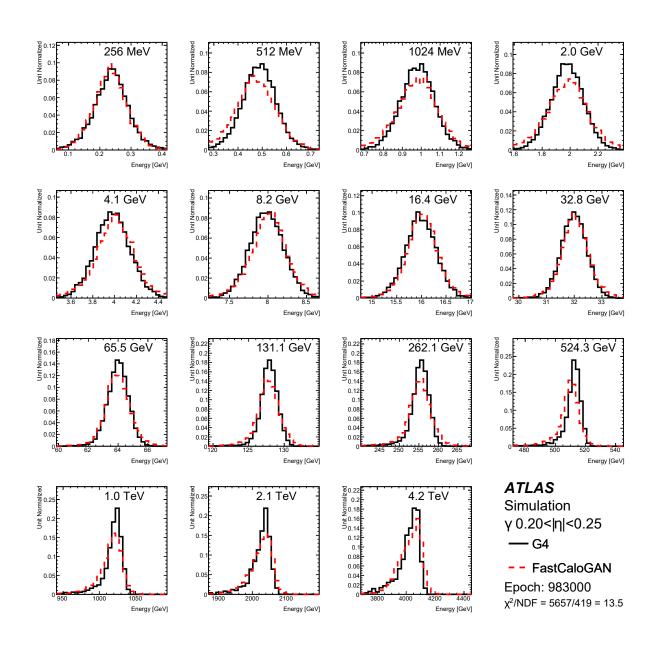


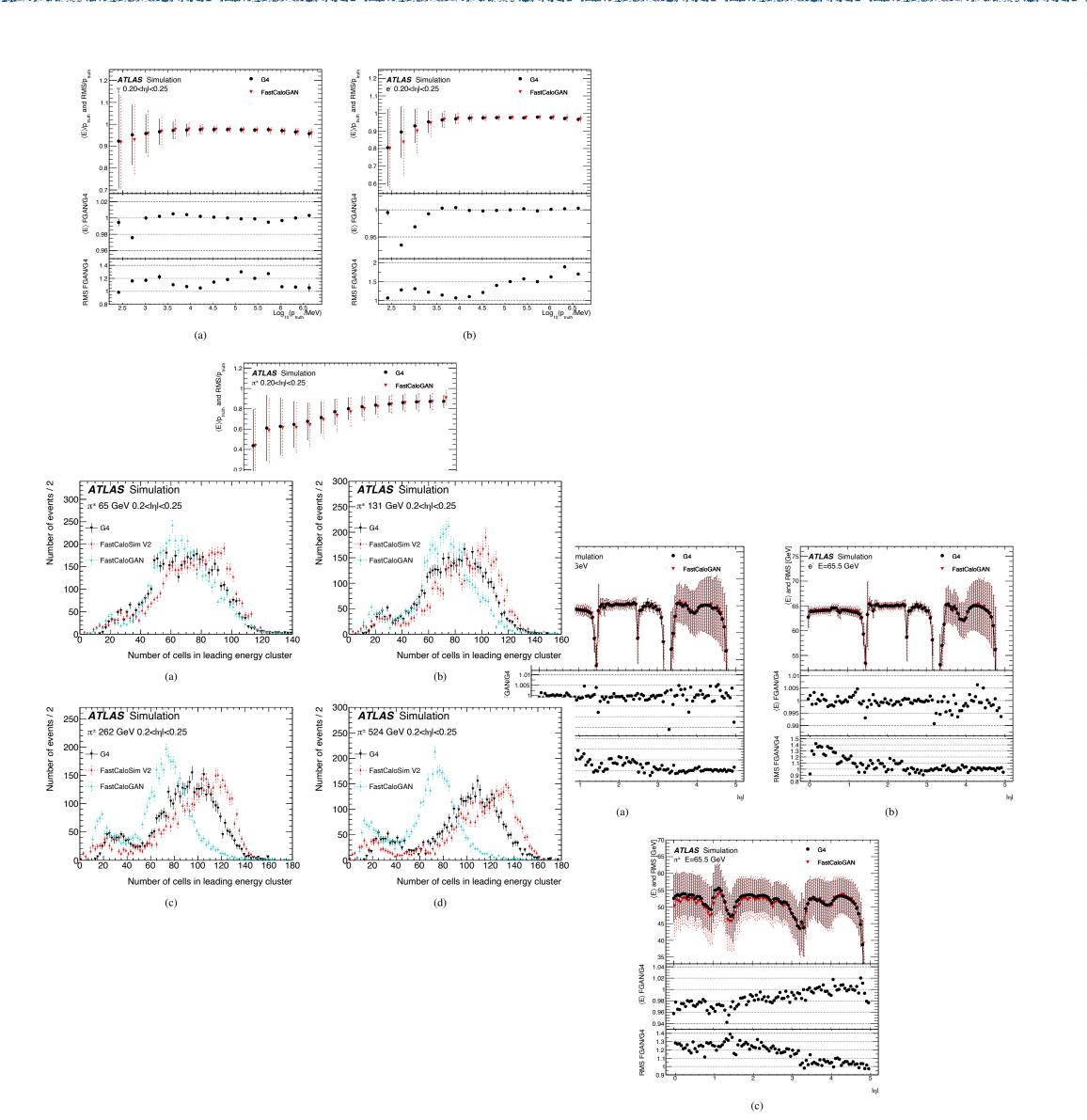


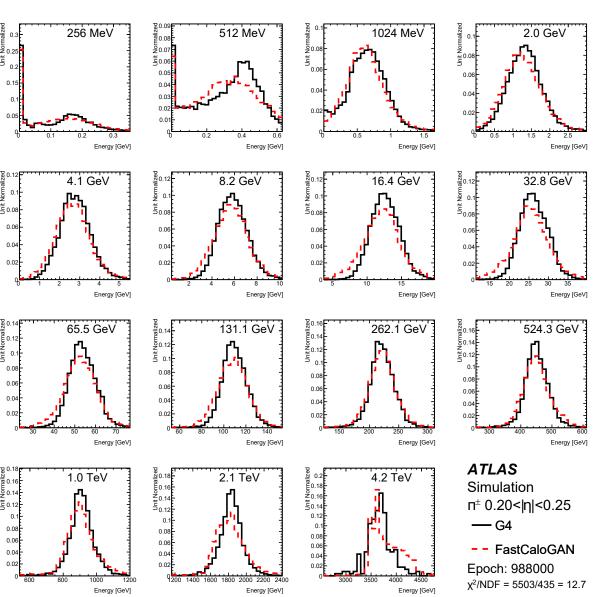


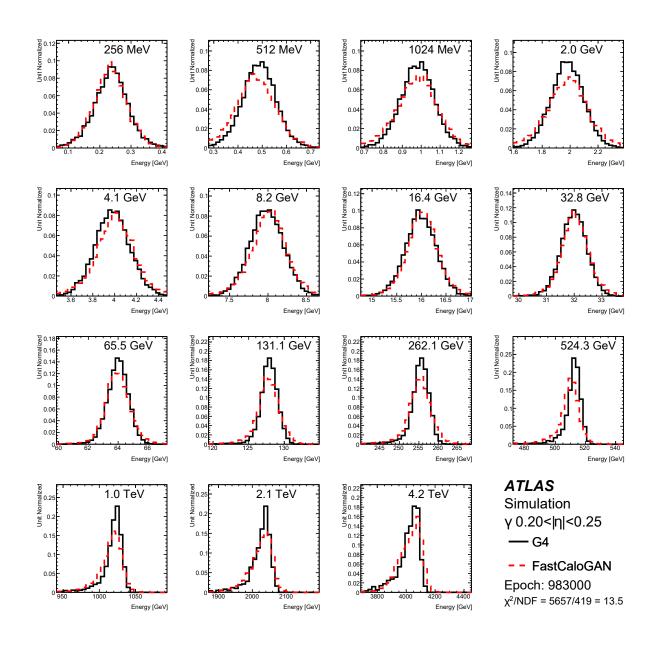


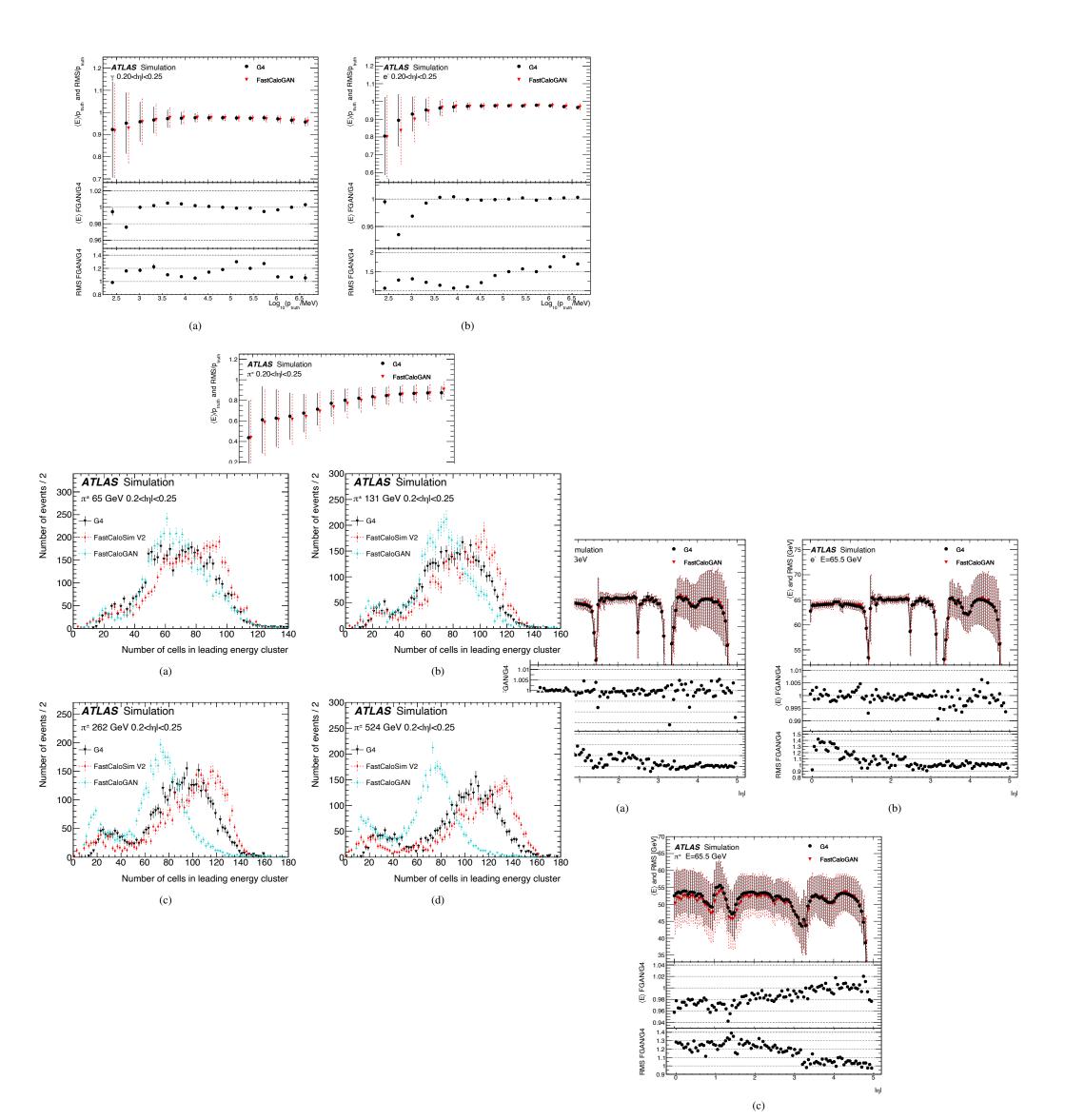


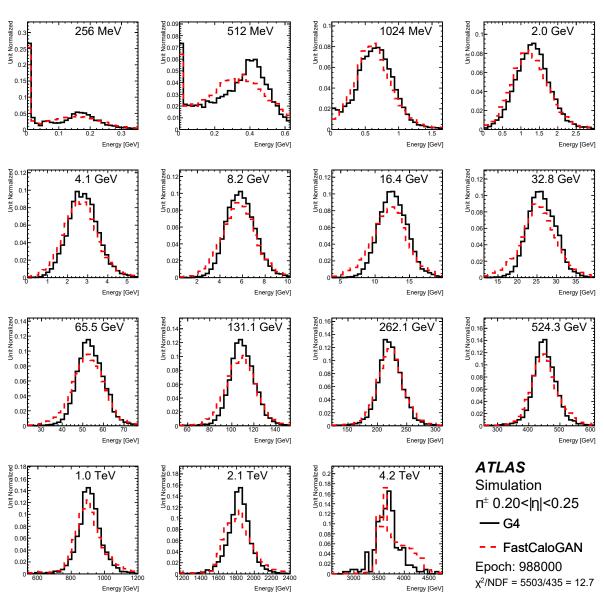


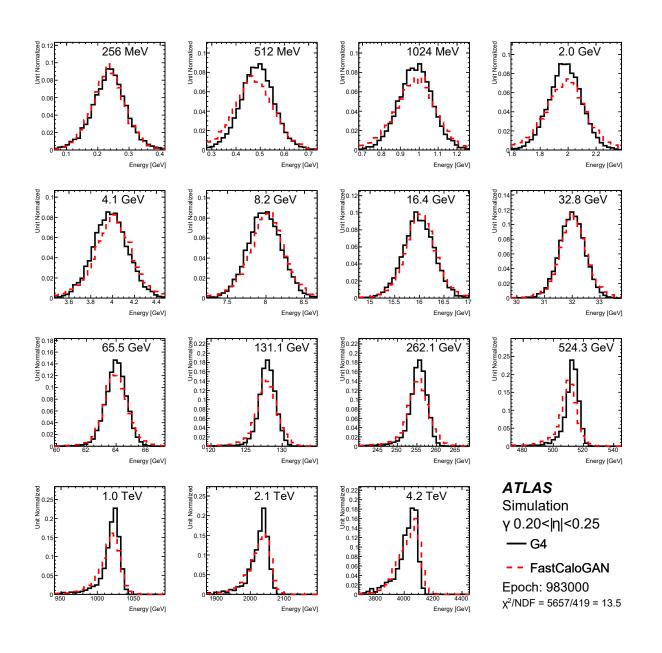


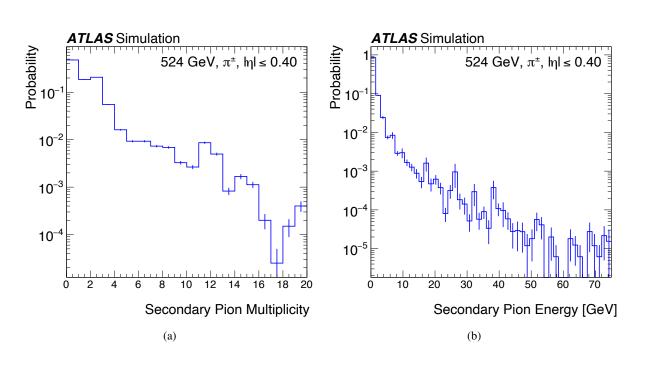


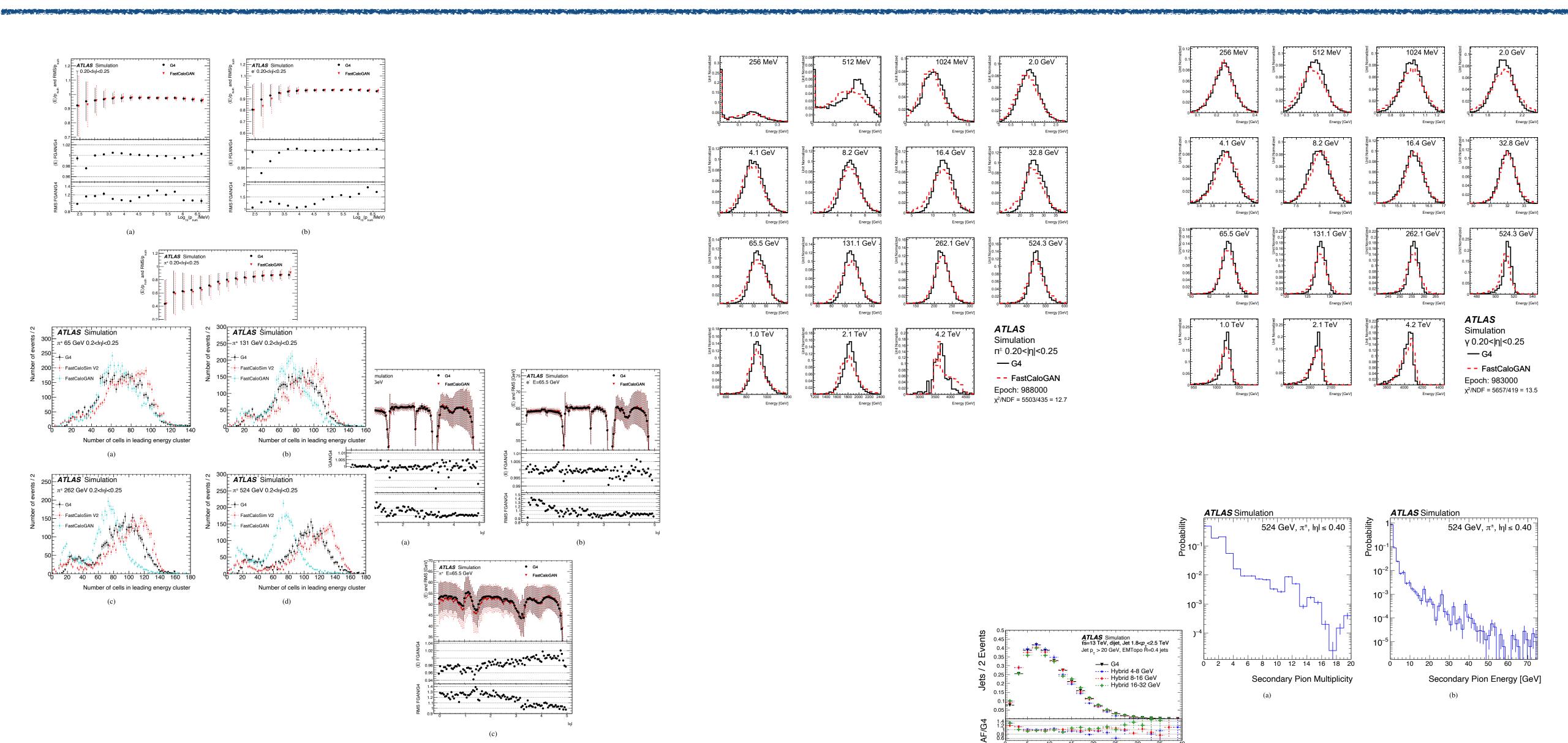


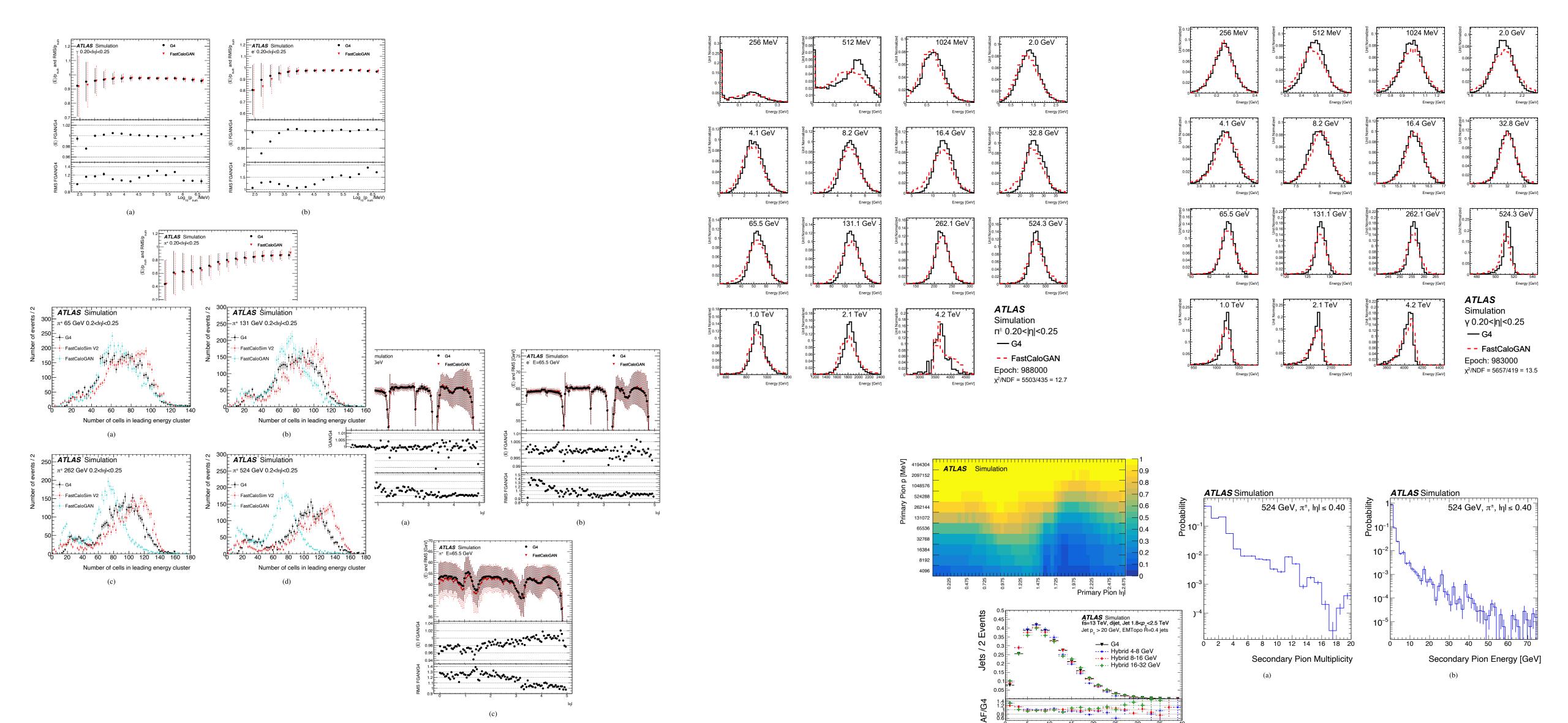


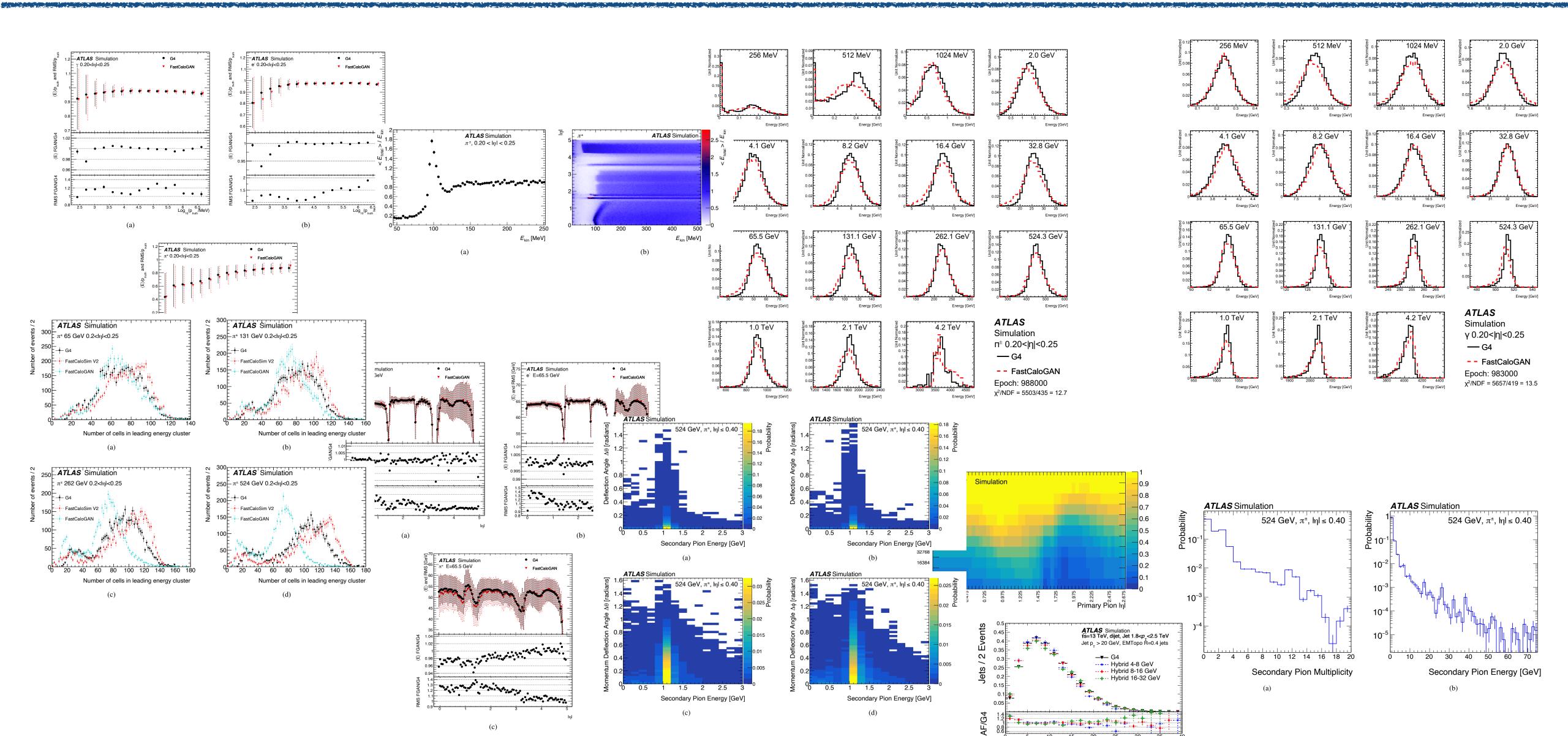


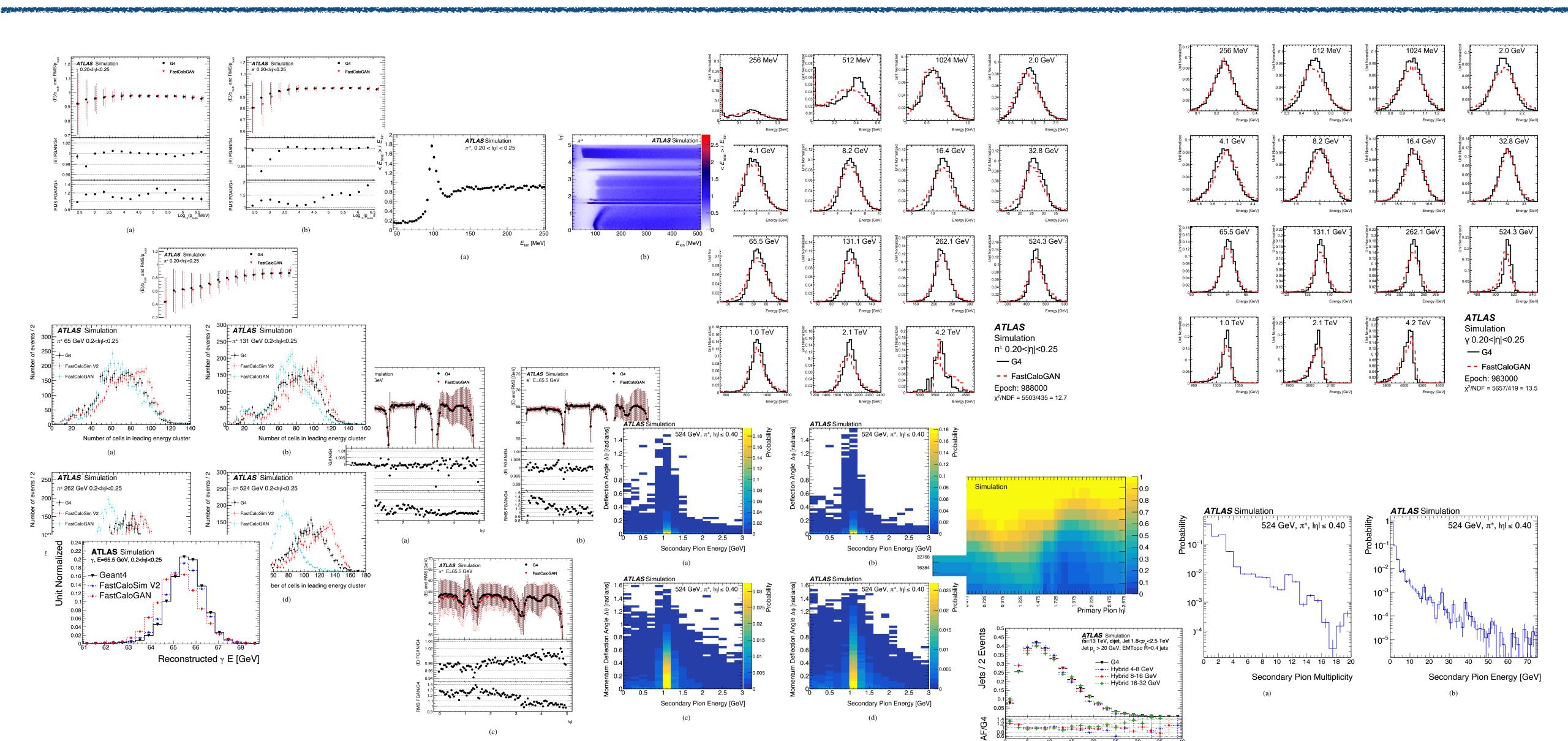












Can we automise the evaluation?

Krause and Shih, 2021

5.4 Classifier metrics

In much of the GAN literature (see e.g. [8]), a common metric is to train classifiers to distinguish between different categories of data (e.g. e^+ vs. π^+), and to see if there is any difference in classifier performance when real data and generated data are interchanged. For example, one might train a classifier on e^+ vs. π^+ GEANT4 images, and compare this to a classifier trained on e^+ vs. π^+ GAN images. If the classifier trained on real images performs similarly to the classifier trained on generated images, then this is evidence that the generated images are approximating the real images well. One can repeat this test for different combinations of real and generated data.

The ultimate test of whether $p_{\text{generated}}(x) = p_{\text{data}}(x)$ would be a direct binary classifier between real and generated images of the *same* type. If the generated and true probability

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Classify Geant4 vs generated and use AUC as single metric

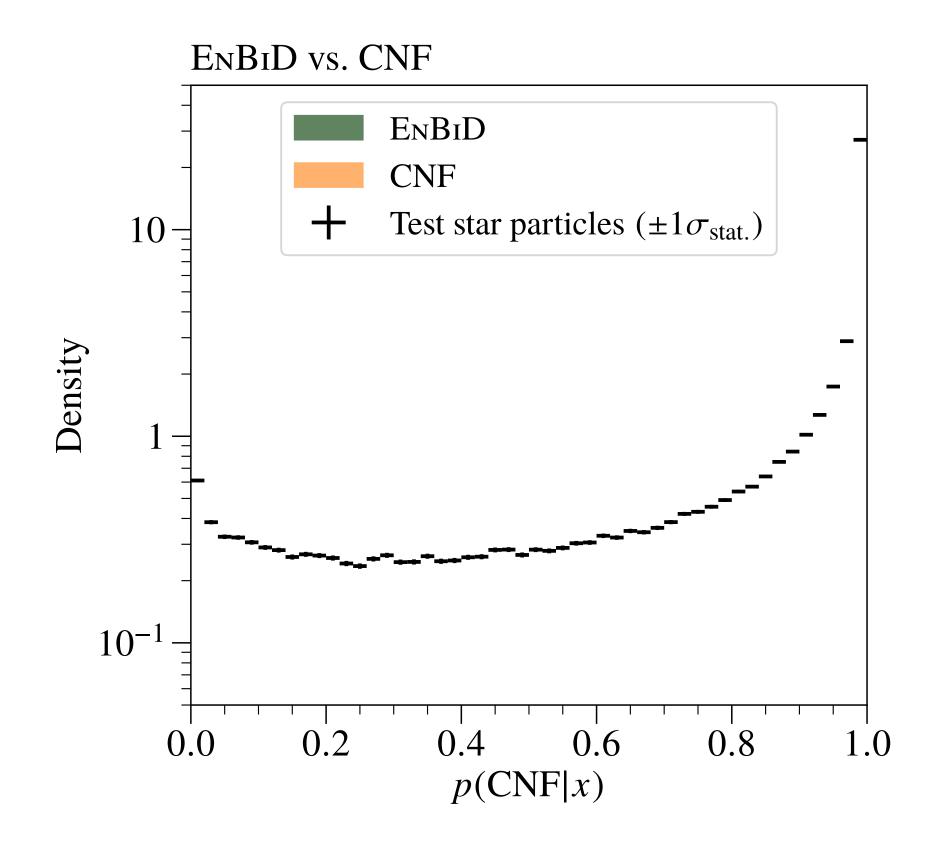
But not the end of the story...

Another classifier test

Lim et al, 2022

Compare two generative models:

Classify generative model1 vs model2, check if test dataset agrees better with one or the other



A comparison of metrics

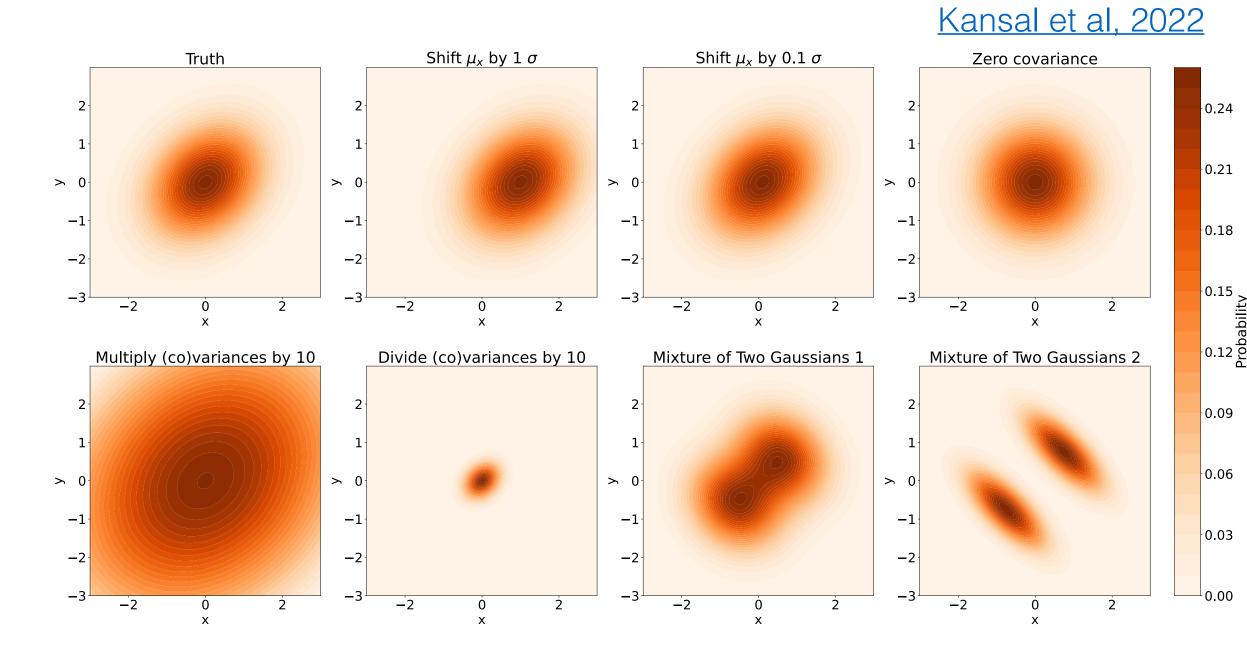
On the Evaluation of Generative Models in High Energy Physics

Raghav Kansal, * Anni Li, and Javier Duarte, University of California San Diego, La Jolla, CA 92093, USA

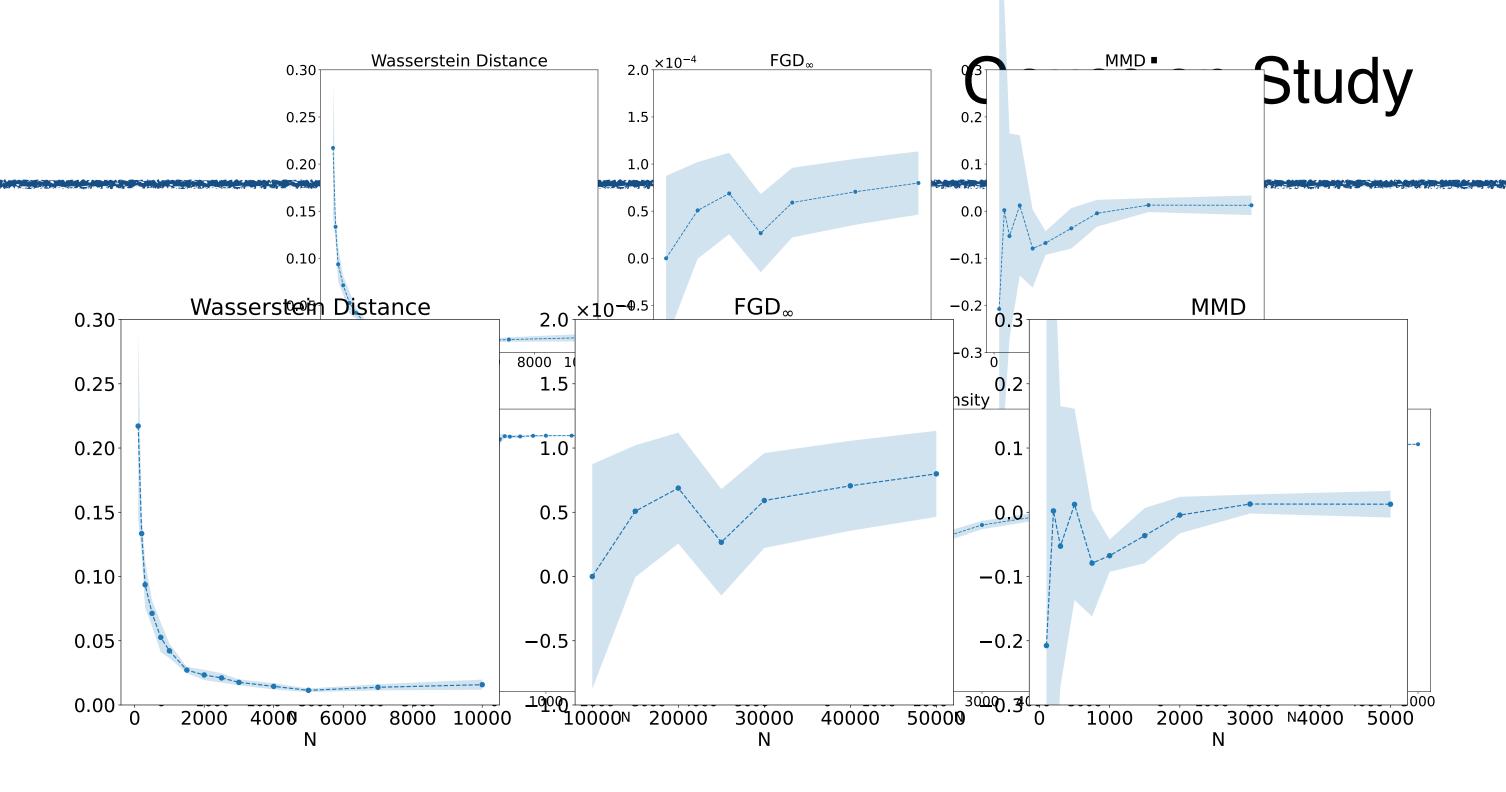
Nadezda Chernyavskaya, Maurizio Pierini European Center for Nuclear Research (CERN), 1211 Geneva 23, Switzerland

Breno Orzari , Thiago Tomei Universidade Estadual Paulista, São Paulo/SP, CEP 01049-010, Brazil

(Dated: November 21, 2022)



- Detailed comparison on Gaussian toys where you have full control
- Application on jet dataset with hand designed distortions



- FGD_{∞} , MMD unbiased
- W too expensive for large N

Metric	Truth	Shift μ_x by 1σ	Shift μ_x by 0.1σ	Zero covariance	Multiply (co)variances by 10	Divide (co)variances by 10	Mixture of Two Gaussians 1	Mixture of Two Gaussians 2
Wasserstein	0.016 ± 0.004	1.14 ± 0.02	0.043 ± 0.008	0.077 ± 0.006	9.8 ± 0.1	0.97 ± 0.01	0.036 ± 0.003	0.191 ± 0.005
$FGD_{\infty} \times 10^3$	0.08 ± 0.03	$\textbf{1011} \pm \textbf{1}$	11.0 ± 0.1	32.3 ± 0.2	9400 ± 8	935.1 ± 0.7	0.07 ± 0.03	0.03 ± 0.03
MMD	0.01 ± 0.02	16.4 ± 0.9	0.07 ± 0.04	0.40 ± 0.08	$19\mathrm{k}\pm1\mathrm{k}$	4.3 ± 0.1	0.06 ± 0.02	0.35 ± 0.03
Precision	0.972 ± 0.005	0.91 ± 0.01	0.976 ± 0.004	0.969 ± 0.006	0.34 ± 0.01	1.0 ± 0.0	0.975 ± 0.003	0.9976 ± 0.0007
Recall	0.997 ± 0.001	0.992 ± 0.003	0.997 ± 0.001	0.9976 ± 0.0006	0.998 ± 0.001	0.58 ± 0.02	0.996 ± 0.001	0.9970 ± 0.0009
Density	3.23 ± 0.06	2.48 ± 0.08	3.19 ± 0.07	3.1 ± 0.1	0.60 ± 0.02	5.7 ± 0.3	2.99 ± 0.09	0.989 ± 0.009
Coverage	0.876 ± 0.002	0.780 ± 0.006	0.872 ± 0.005	0.872 ± 0.004	0.60 ± 0.01	0.406 ± 0.008	0.871 ± 0.002	0.956 ± 0.006

 FGD_{∞} promising but no sensitivity to higher moments, requires extrapolation

0.000 0.025 0.050 0.075 0.100 0.125 0.150 0.175 0.200 $\text{Jet } m/p_{ au}$

0.000 0.025 0.050 0.075 0.100 0.125 0.150 0.175 0.200 Jet m/p_T

Jet Study

Metric	Truth	Smeared	Shifted	Removing tail	Particle features smeared	$\eta^{ m rel}$ smeared	$p_{ m T}^{ m rel}$ smeared	$p_{ m T}^{ m rel}$ shifted
$W_1^M \times 10^3$	0.28 ± 0.05	2.1 ± 0.2	6.0 ± 0.3	0.6 ± 0.2	1.7 ± 0.2	0.9 ± 0.3	0.5 ± 0.2	5.8 ± 0.2
Wasserstein EFP	0.02 ± 0.01	0.09 ± 0.05	0.10 ± 0.02	0.016 ± 0.007	0.19 ± 0.08	0.03 ± 0.01	0.03 ± 0.02	0.06 ± 0.02
$FGD_{\infty} EFP \times 10^3$	0.01 ± 0.02	21.5 ± 0.3	26.8 ± 0.3	2.31 ± 0.07	23.4 ± 0.3	$\boldsymbol{3.59 \pm 0.09}$	2.29 ± 0.05	28.9 ± 0.2
MMD EFP $\times 10^3$	-0.006 ± 0.005	0.17 ± 0.06	0.9 ± 0.1	0.03 ± 0.02	0.35 ± 0.09	0.08 ± 0.05	0.01 ± 0.02	1.8 ± 0.1
Precision EFP	0.9 ± 0.1	0.94 ± 0.04	0.978 ± 0.005	0.88 ± 0.08	0.7 ± 0.1	0.94 ± 0.06	0.7 ± 0.1	0.79 ± 0.09
Recall EFP	0.9 ± 0.1	0.88 ± 0.07	0.97 ± 0.01	0.92 ± 0.06	0.83 ± 0.05	0.92 ± 0.07	0.8 ± 0.1	0.8 ± 0.1
Wasserstein PN	1.65 ± 0.06	1.7 ± 0.1	2.4 ± 0.4	1.71 ± 0.08	4.5 ± 0.1	1.79 ± 0.05	4.0 ± 0.4	7.6 ± 0.2
$FGD_{\infty} PN \times 10^3$	0.8 ± 0.7	40 ± 2	193 ± 9	5.0 ± 0.9	1250 ± 10	20 ± 1	1230 ± 10	$\textbf{3640} \pm \textbf{10}$
MMD PN $\times 10^3$	-2 ± 2	4 ± 8	80 ± 10	-1 ± 4	500 ± 100	3 ± 2	560 ± 60	1100 ± 40
Precision PN	0.68 ± 0.07	0.64 ± 0.04	0.71 ± 0.06	0.73 ± 0.03	0.09 ± 0.04	0.75 ± 0.08	0.08 ± 0.04	0.39 ± 0.08
Recall PN	0.70 ± 0.05	0.61 ± 0.04	0.61 ± 0.08	0.73 ± 0.06	0.014 ± 0.009	0.7 ± 0.1	0.01 ± 0.01	0.57 ± 0.09
Classifier LLF AUC	0.50	0.52	0.54	0.50	0.97	0.81	0.93	0.99
Classifier HLF AUC	0.50	0.53	0.55	0.50	0.84	0.64	0.74	0.92

Kansal et al, 2022

- FGD_{∞} on EFPs does quite well in these tests
- Would be interesting to see it used and stress tested!

Jet Study

Does this convince us to stop looking at plots?

1D Histograms, 2D correlations, ... oh but did you look at that plot?

What would we ideally want? (Open Problem)

- Metric that let's us quickly compare generative models, meaningful numbers (does not saturate quickly)
- Reproducible and stable, comparable between different studies
- Insensitive to irrelevant numerical differences eg. Discrete output models
- Robust to simple transformation of input? Expect it to be sensitive to eg. log transformations
- If we truly had a "single ultimate metric", could we use it as a loss function / automated HPO? Would metric still be meaningful?

oh but did you look at that plot ? \rightarrow oh but did you look at that metric for this $E/\eta/\phi$?

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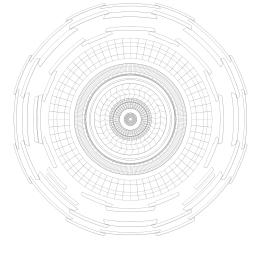
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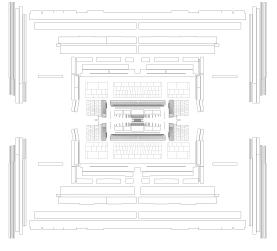
Realistic Target

- Have O(5) metrics, that provide meaningful, orthogonal information about different aspects
 - Stats based: Metrics focused on tails, bulk, higher moments, lower moments, overfitting, interpolation
 - Physics info: energy modelling, pointing, substructure, shape, interpolation
 oh but did you look at that plot ? → oh but did you look at that metric for this E/η/φ?
- Back-port these ideas for uncertainty quantification of traditional simulators

Conclusion

- Uncertainties a central problem in experimental science, ML can help (but use mindfully!)
- Lots of room for novel ideas and innovative work
 - Multiple NPs, fast profiling
 - ML to improve quantification & mitigation of theory uncertainties
- Generative models: Metrics that capture specific range of properties worth exploring
 - What we develop could be back-ported to traditional simulation!





Thank you!

- We want to select an analysis strategy with best final measurement performance
- Full statistical quantification of performance → Computationally expensive 'Profile Likelihood'
- But there's an old trick! If you've collapsed your high-dimensional data into a single observable, you can estimate your sensitivity with cheaper performance metrics:

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- But there's an old trick! If you've collapsed your high-dimensional data into a single observable, you can estimate your sensitivity with cheaper performance metrics:

$$AMS_1 = \sqrt{2\left((s+b)\ln\frac{s+b}{b_0} - s - b + b_0\right) + \frac{(b-b_0)^2}{\sigma_b^2}},$$

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Question: How can we optimise analysis for this metric?

Median Significance of Discovery (Including uncertainties)

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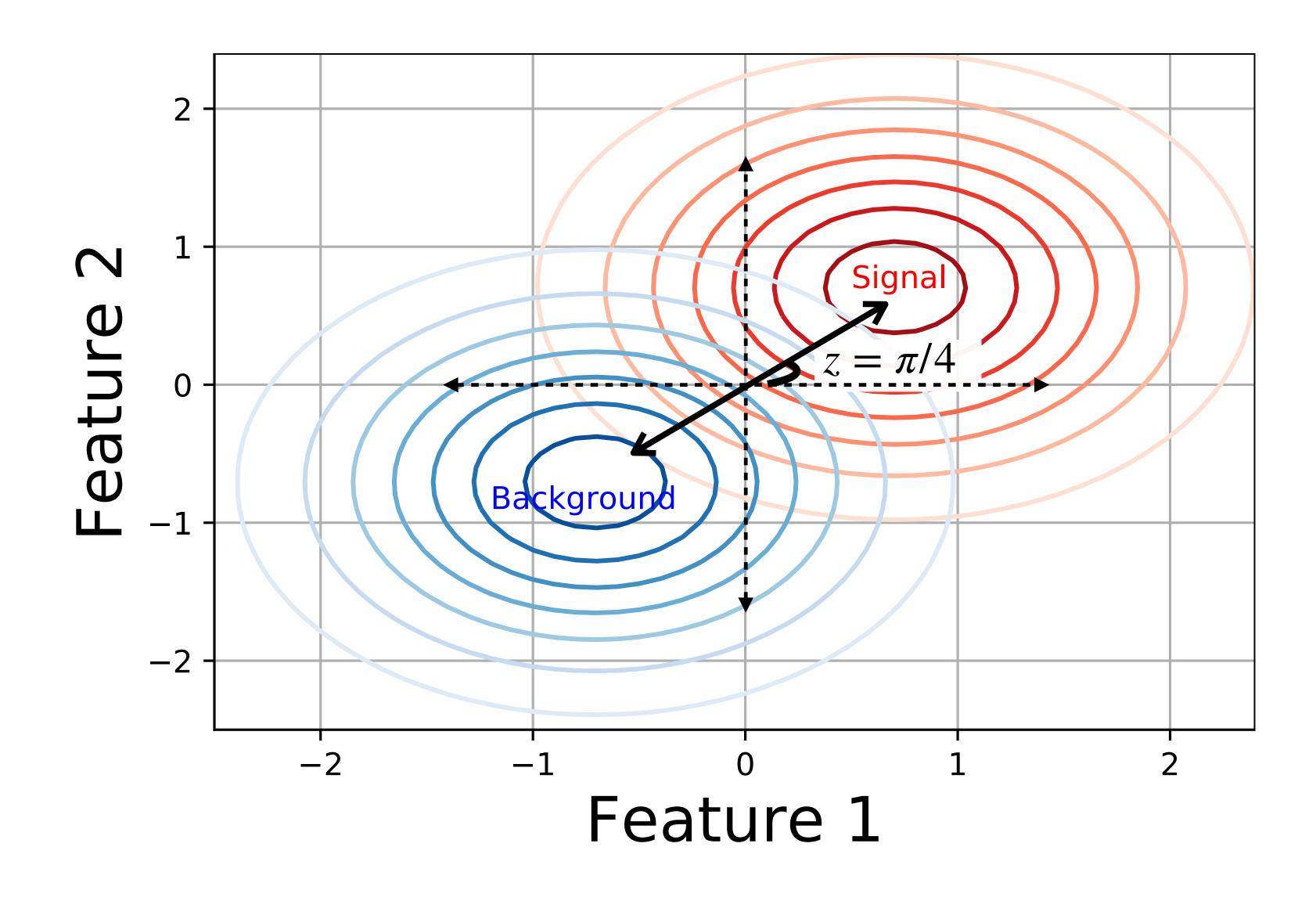
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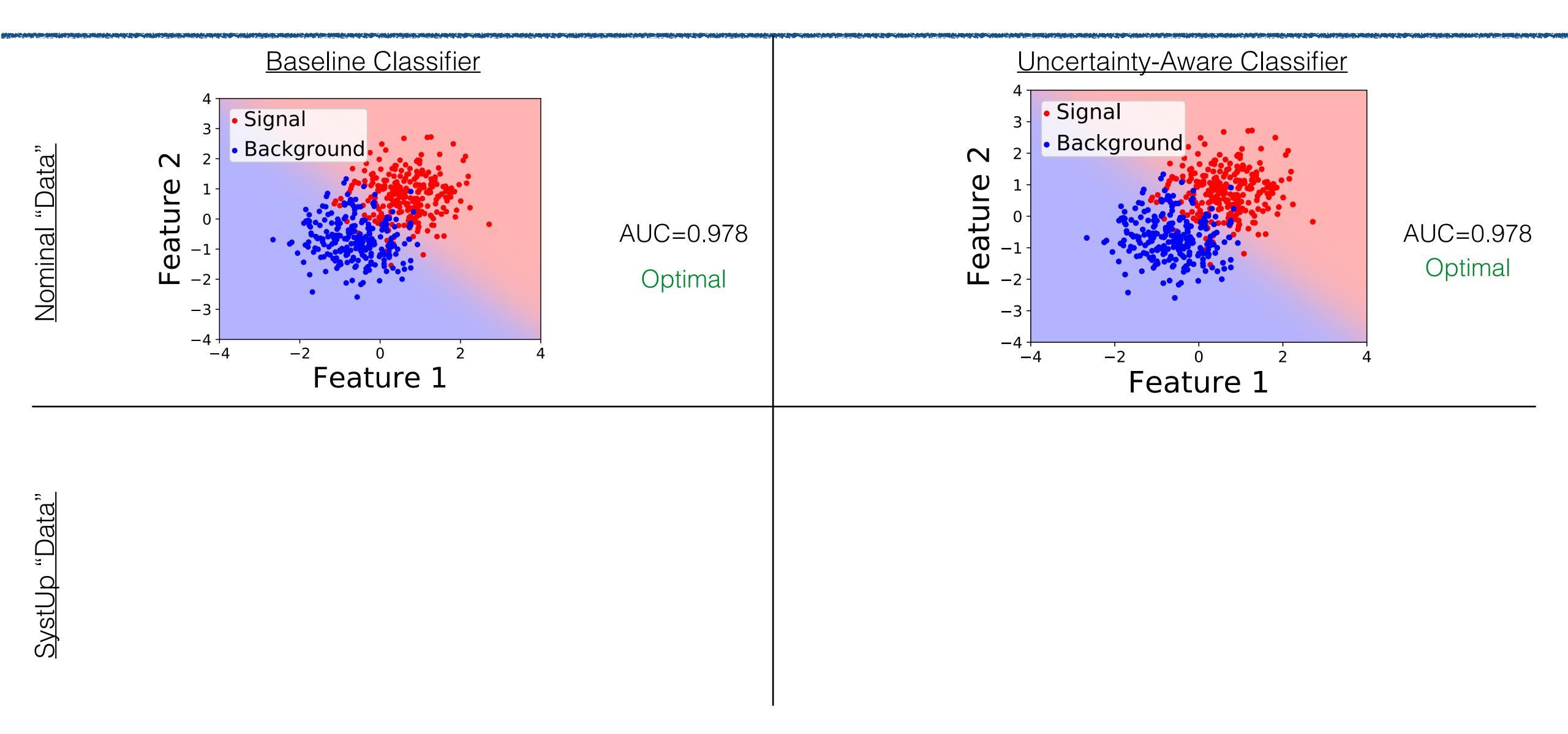
Toy Problem Definition



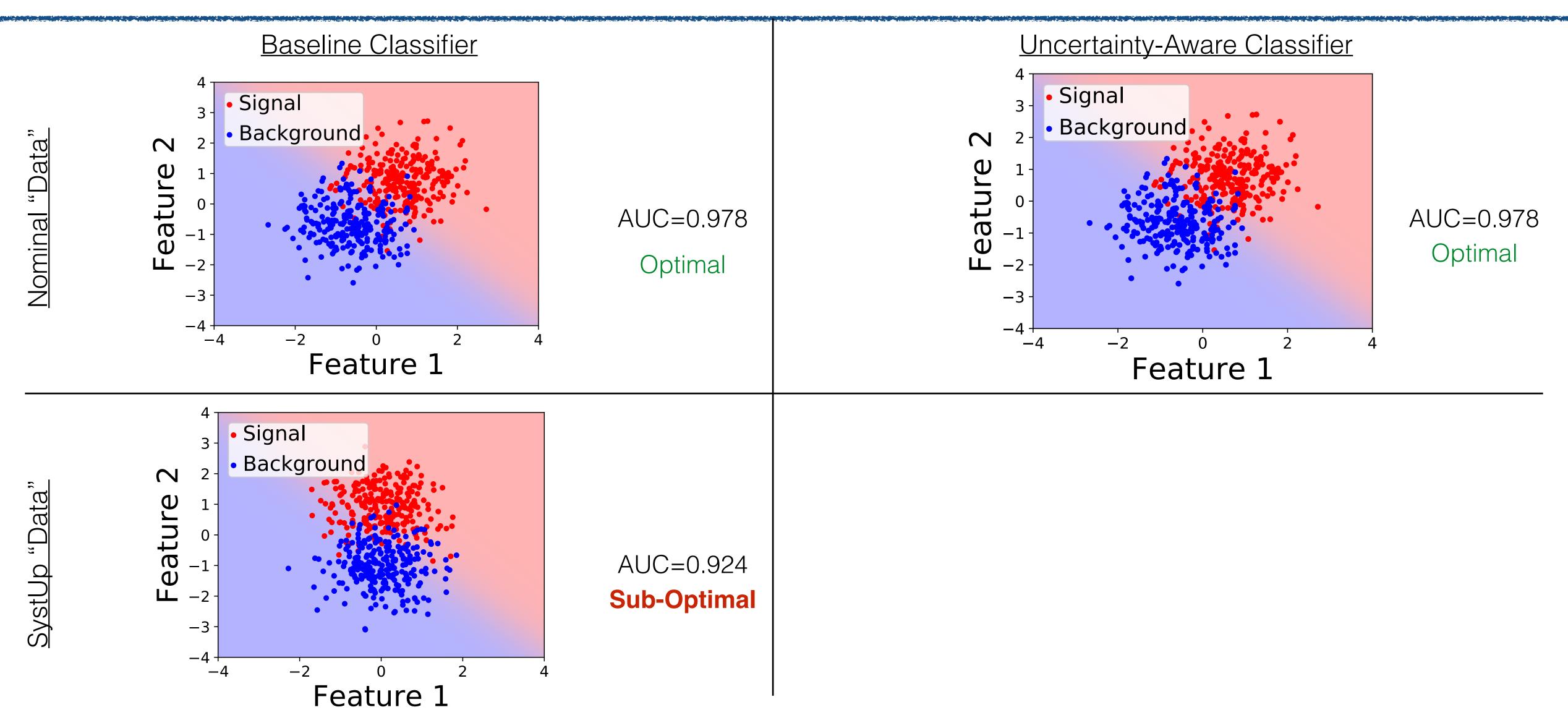
$$\mu = \frac{N_{s,obs}}{N_{s,exp}}$$

$$z = Angle$$

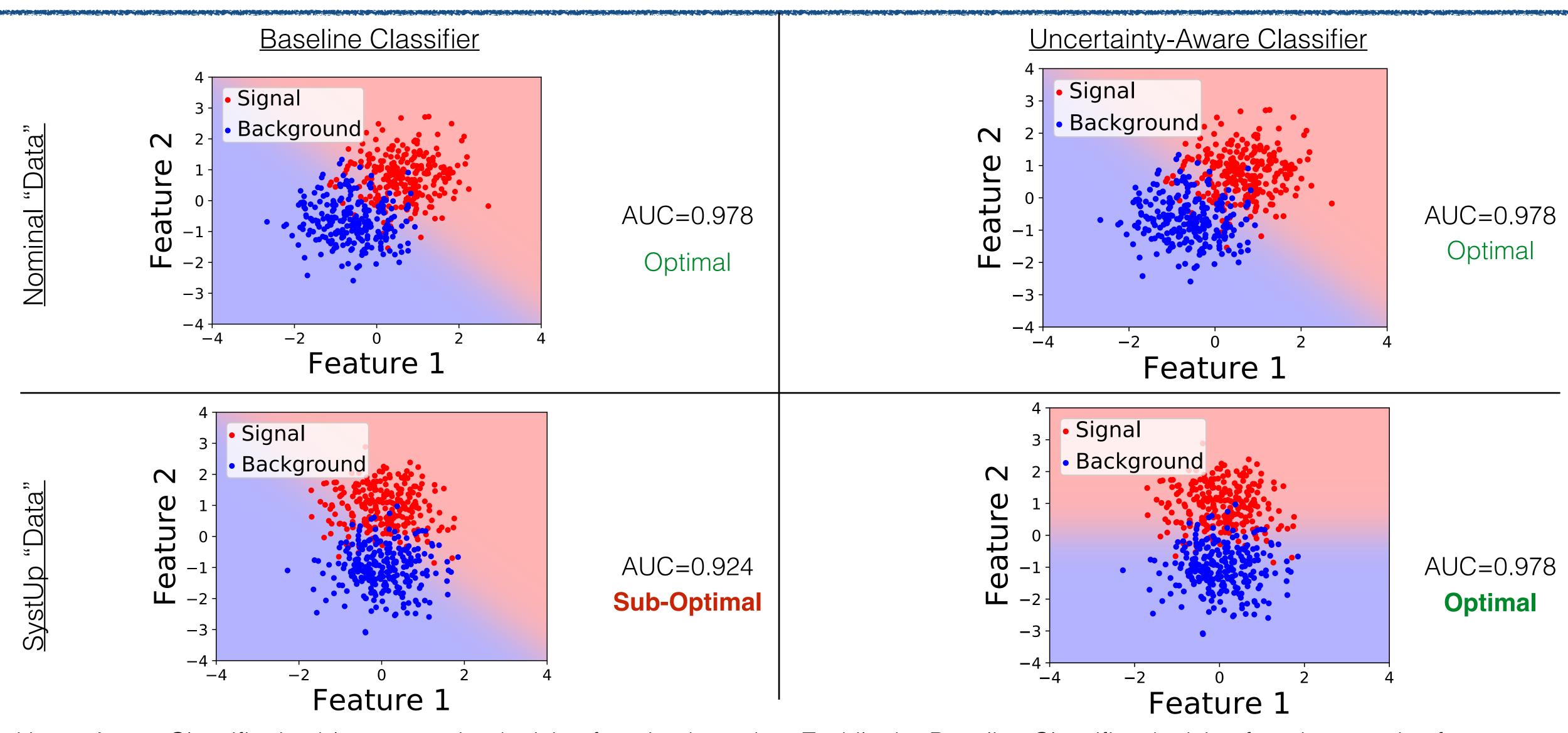
Nominal and Systematic Up Examples



Nominal and Systematic Up Examples



Nominal and Systematic Up Examples



Uncer-Aware Classifier is able to rotate its decision function based on Z while the Baseline Classifier decision function remains frozen56

Profile Likelihood

Standard method of including the systematic uncertainty into the likelihood computation

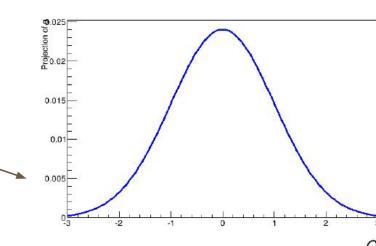
We simply make the selection/observable a function of z

In principle could also be done in cut-based analysis: make cut a continuous function of z

The Profile Likelihood approach

- The profile likelihood is a way to include **systematic uncertainties in the likelihood**
 - systematics included as "constrained" nuisance parameters
 - the idea behind is that systematic uncertainties on the measurement of μ come from *imperfect knowledge* of parameters of the model (S and B prediction)
 - still *some knowledge* is implied: " $\theta = \theta_0 \pm \Delta \theta$ "

$$\mathcal{L}(\boldsymbol{n}, \boldsymbol{\theta}^0 | \mu, \boldsymbol{\theta}) = \prod_{i \in bins} \mathcal{P}(n_i | \mu \cdot S_i(\boldsymbol{\theta}) + B_i(\boldsymbol{\theta})) \times \prod_{j \in syst} \mathcal{G}(\theta_j^0 | \theta_j, \Delta \theta_j)$$



- usually θ^0 =0 and $\Delta\theta$ =1 (convention)
- define **effect of systematic** *j* on prediction *x* in bin *i* at "+1" and "-1",
- then interpolate & extrapolate for any value of θ

external / α priori knowledge interpreted as "auxiliary/subsidiary measurement", implemented as constraint/penalty term, i.e. probability density function (usually Gaussian, interpreting " $\pm \Delta\theta$ " as Gaussian standard deviation)

From Michele Pinamonti's talk:

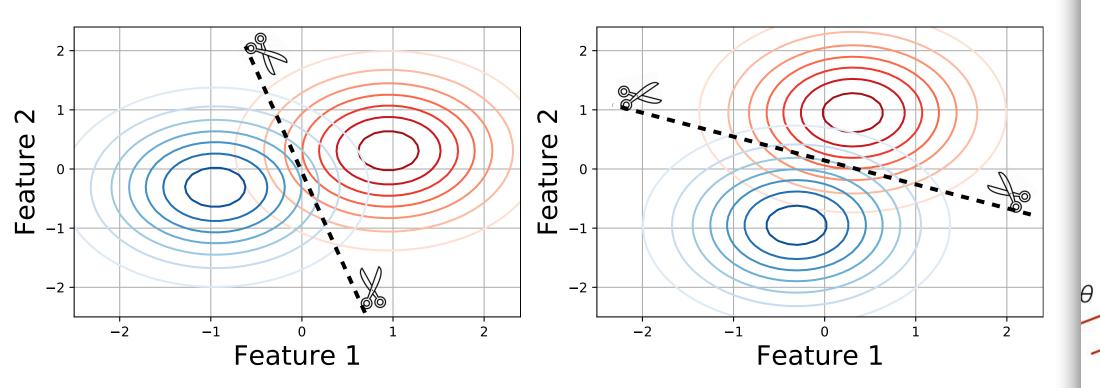
https://indico.cern.ch/event/727396/contributions/3021899/attachments/1657532/2654085/ Statistical_methods_at_ATLAS_and_CMS_2.pdf

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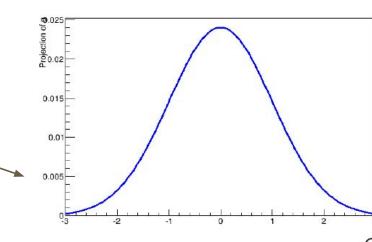
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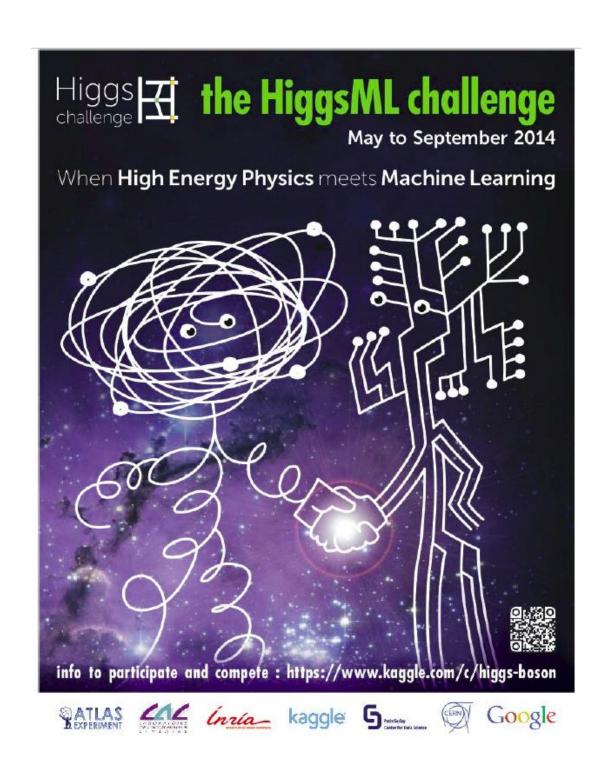
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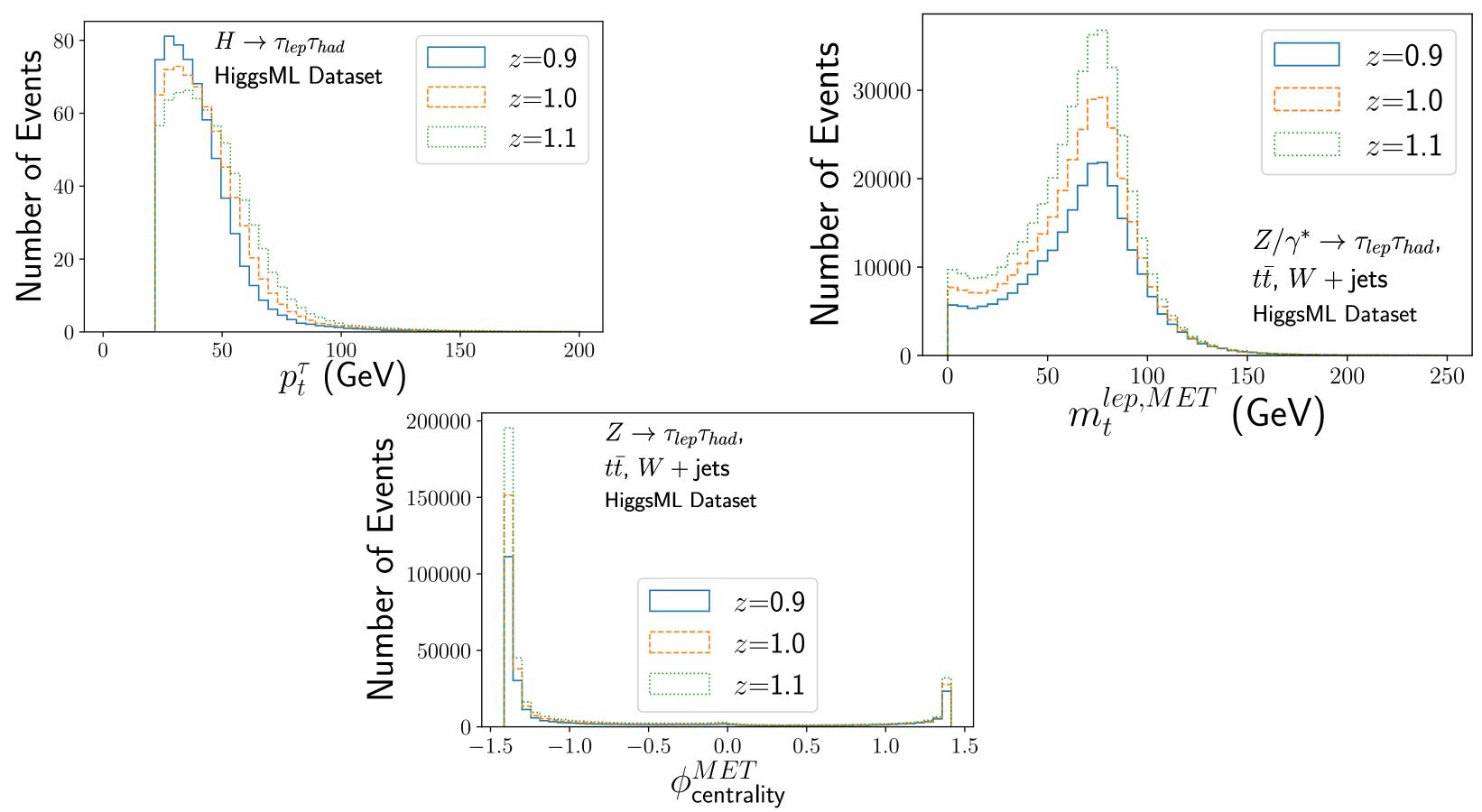
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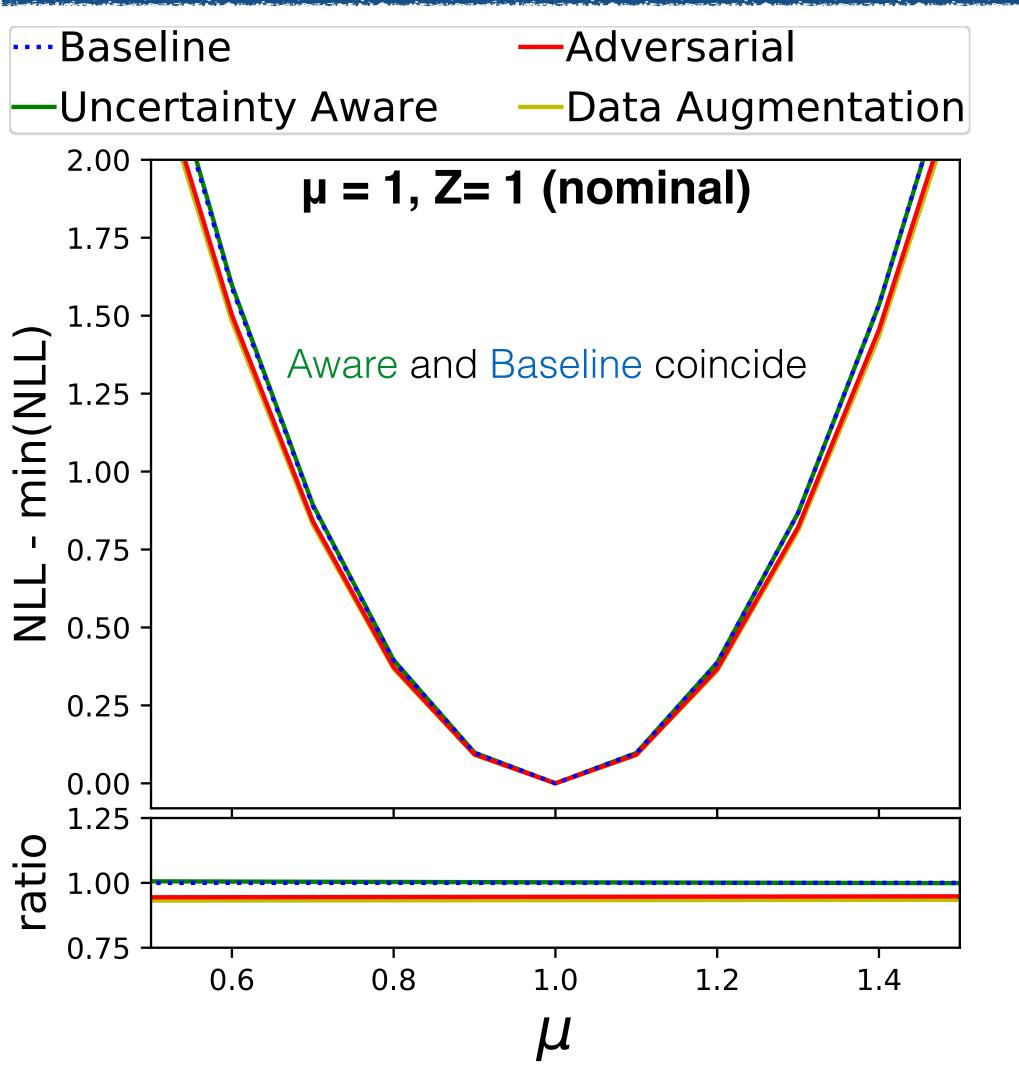
Physics Data: HiggsML + Tau Energy Scale (TES) Uncertainty

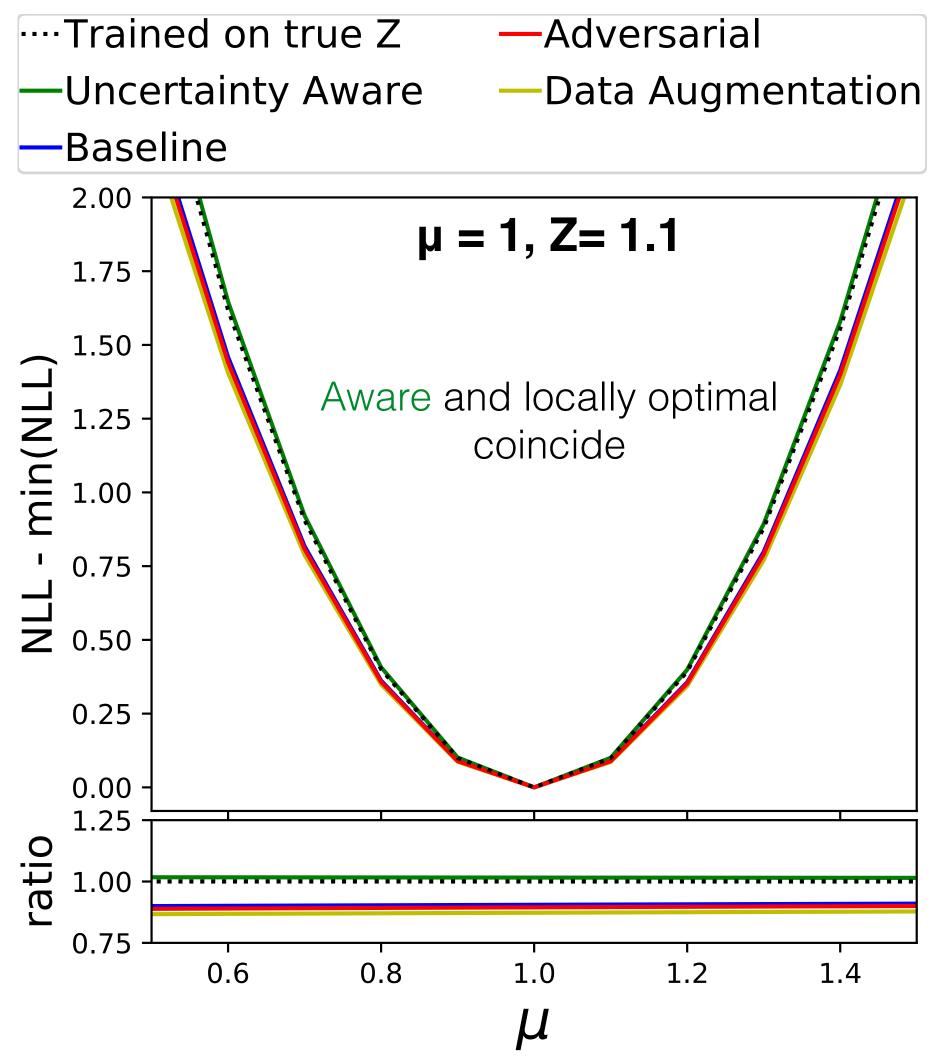


Parameter of Interest is Higgs signal strength μ , and TES is the nuisance parameter Z



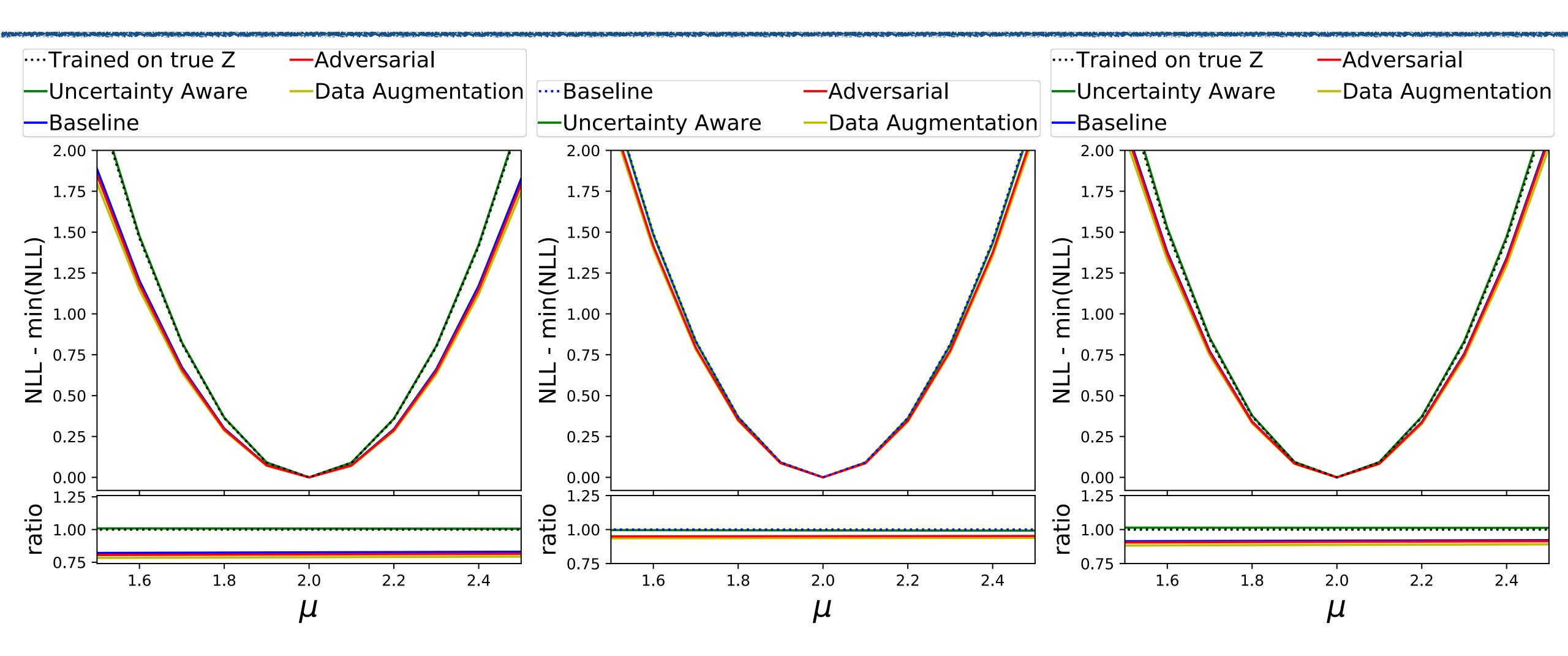
Test performance for "observed" data at nominal and above nominal Z





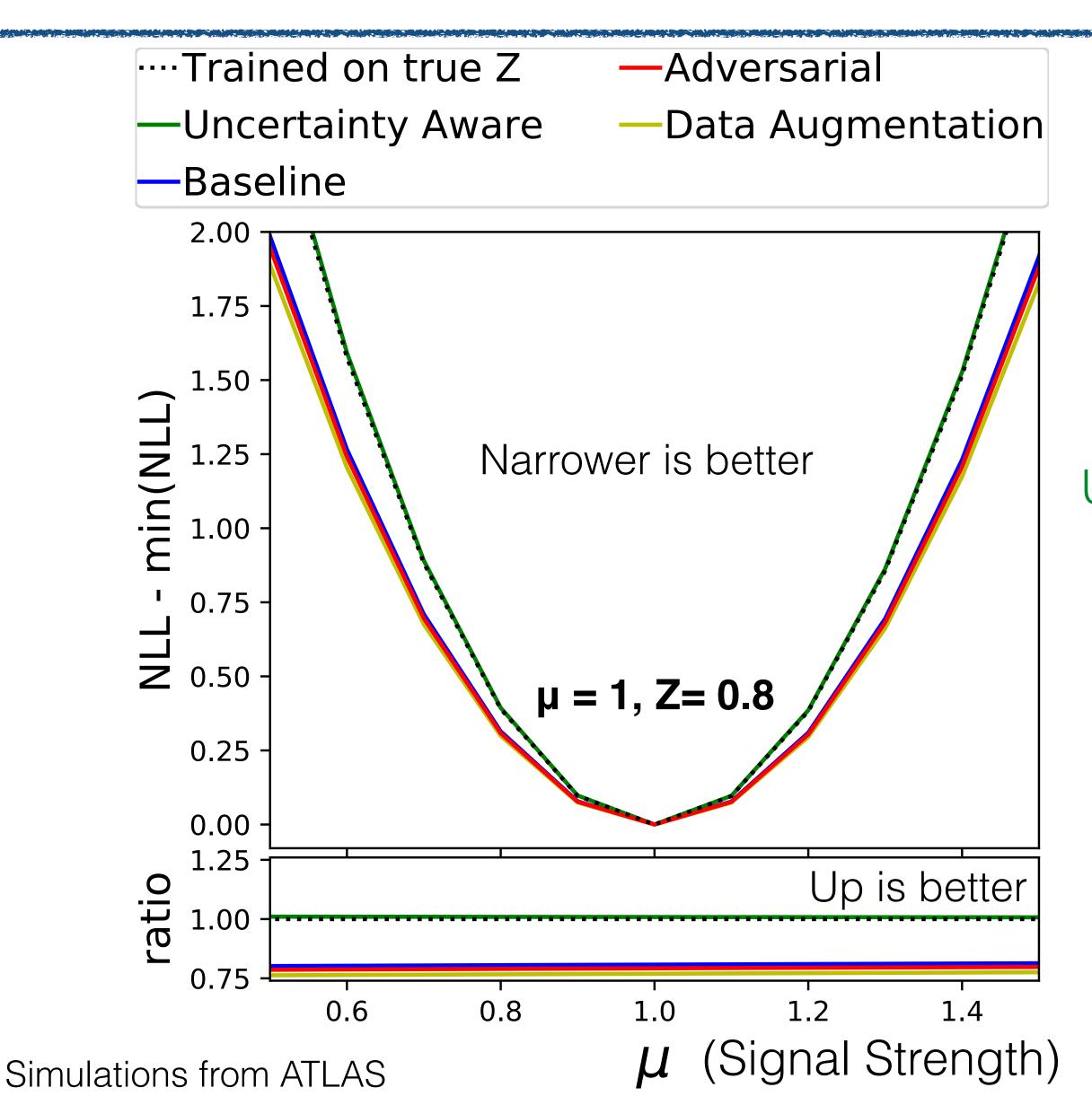
In every case the Aware Classifier is as good as the optimal one, no other technique matches its performance everywhere

Test performance for "observed" datasets at $\mu=2$



In every case the Aware Classifier is as good as the optimal one, no other technique matches its performance everywhere

Physics Data: HiggsML + Tau Energy Scale (TES) Uncertainty



Uncertainty-Aware coincides with classifier trained on true Z

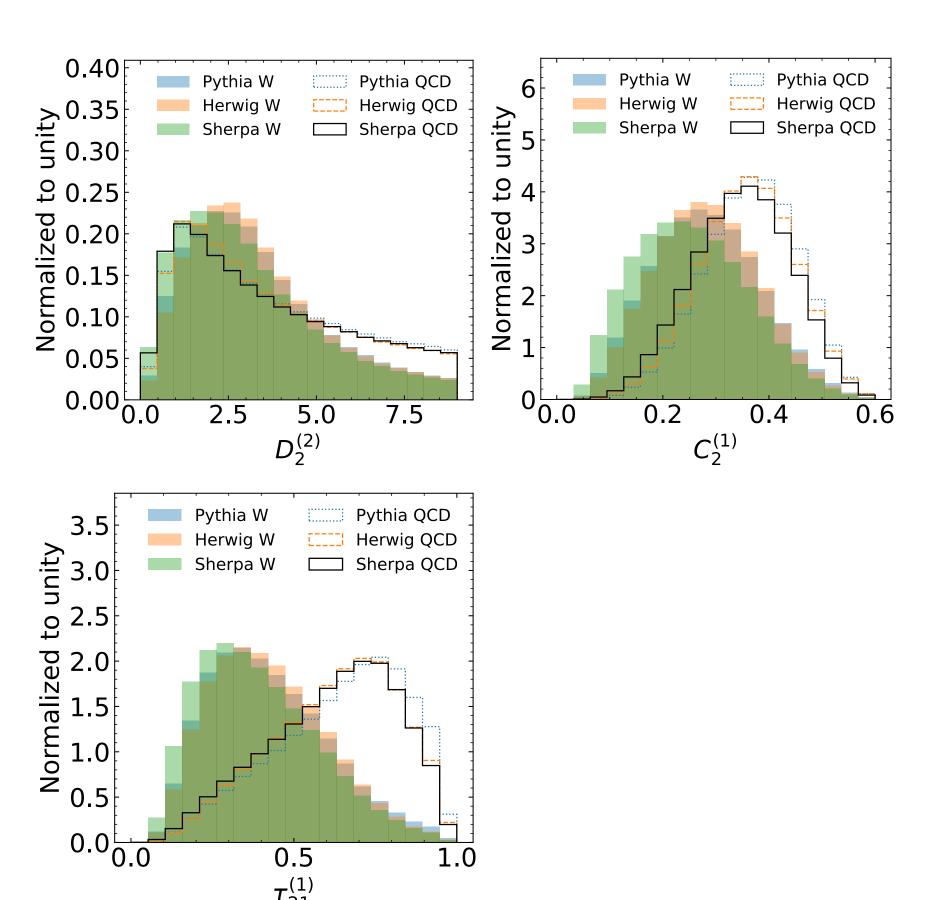
⇒ Can't get much better than that!

Case Study 1: Two-point uncertainty (fragmentation modelling)

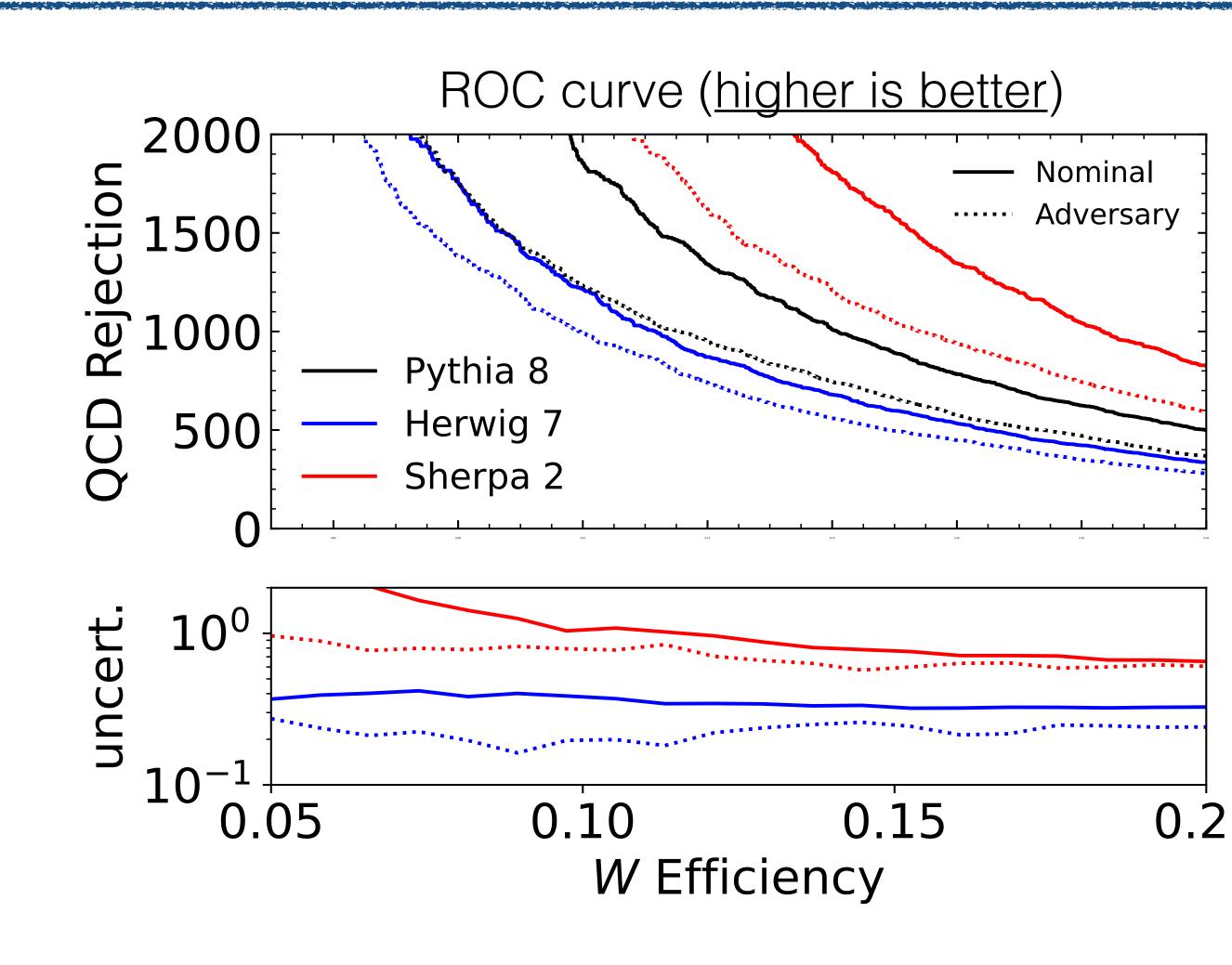
Goal: W jets vs QCD jets

Decorrelation: Reduce difference in performance on Herwig vs Pythia

Cross-check: Test uncertainty estimate from {Herwig vs Pythia} using Sherpa



Case Study 1: Two-point uncertainty - Result

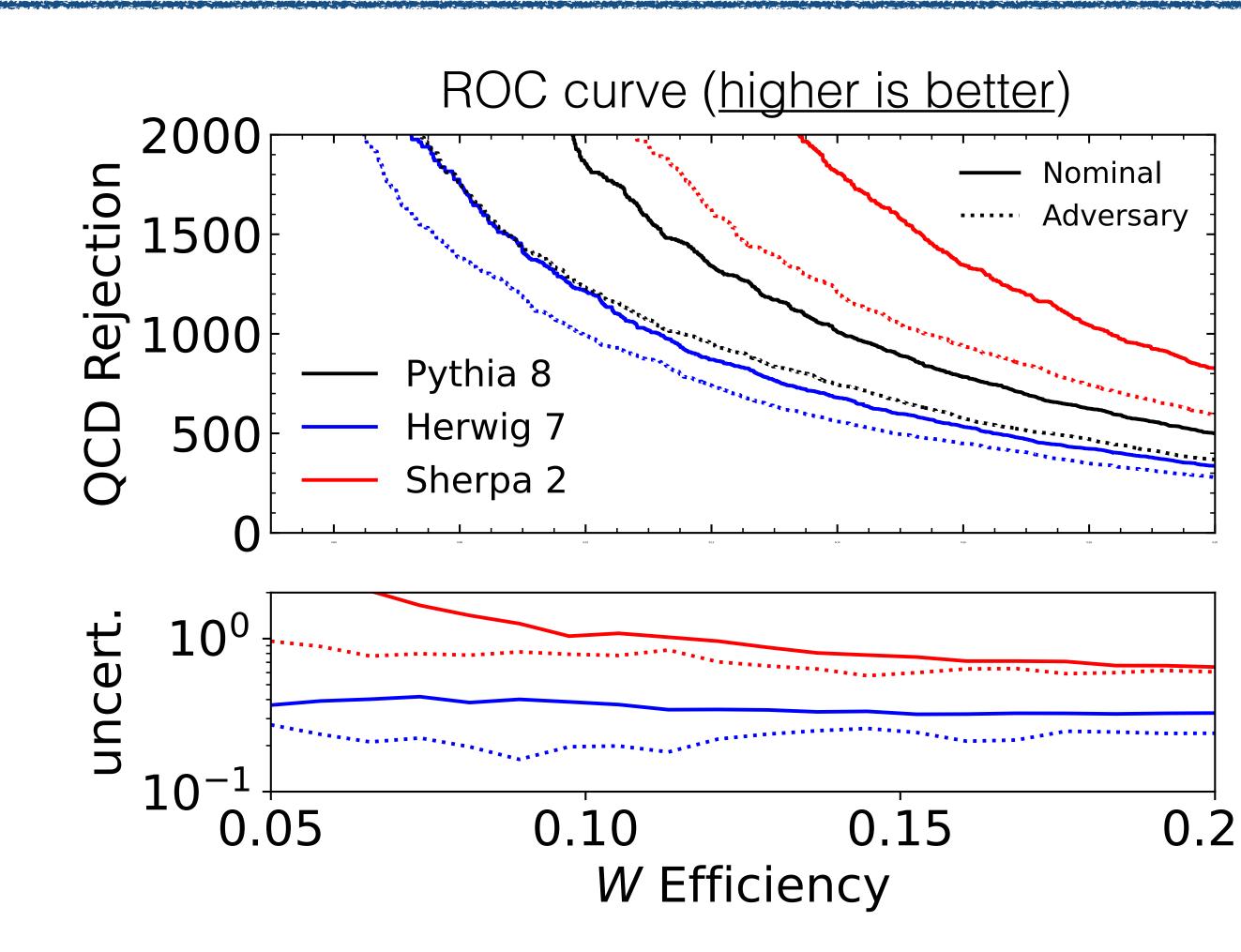


Case Study 1: Two-point uncertainty - Result

Adversary successfully <u>sacrifices separation</u> <u>power</u> in order to reduce difference in performance between <u>Herwig</u> and <u>Pythia</u>

Cross-check with **Sherpa** reveals <u>uncertainty</u> <u>severely underestimated</u> by usual **Herwig** vs **Pythia** comparison

In an typical LHC analysis, a cross-check with third generator rarely performed, similar to prior work suggesting decorrelation for theory uncertainties

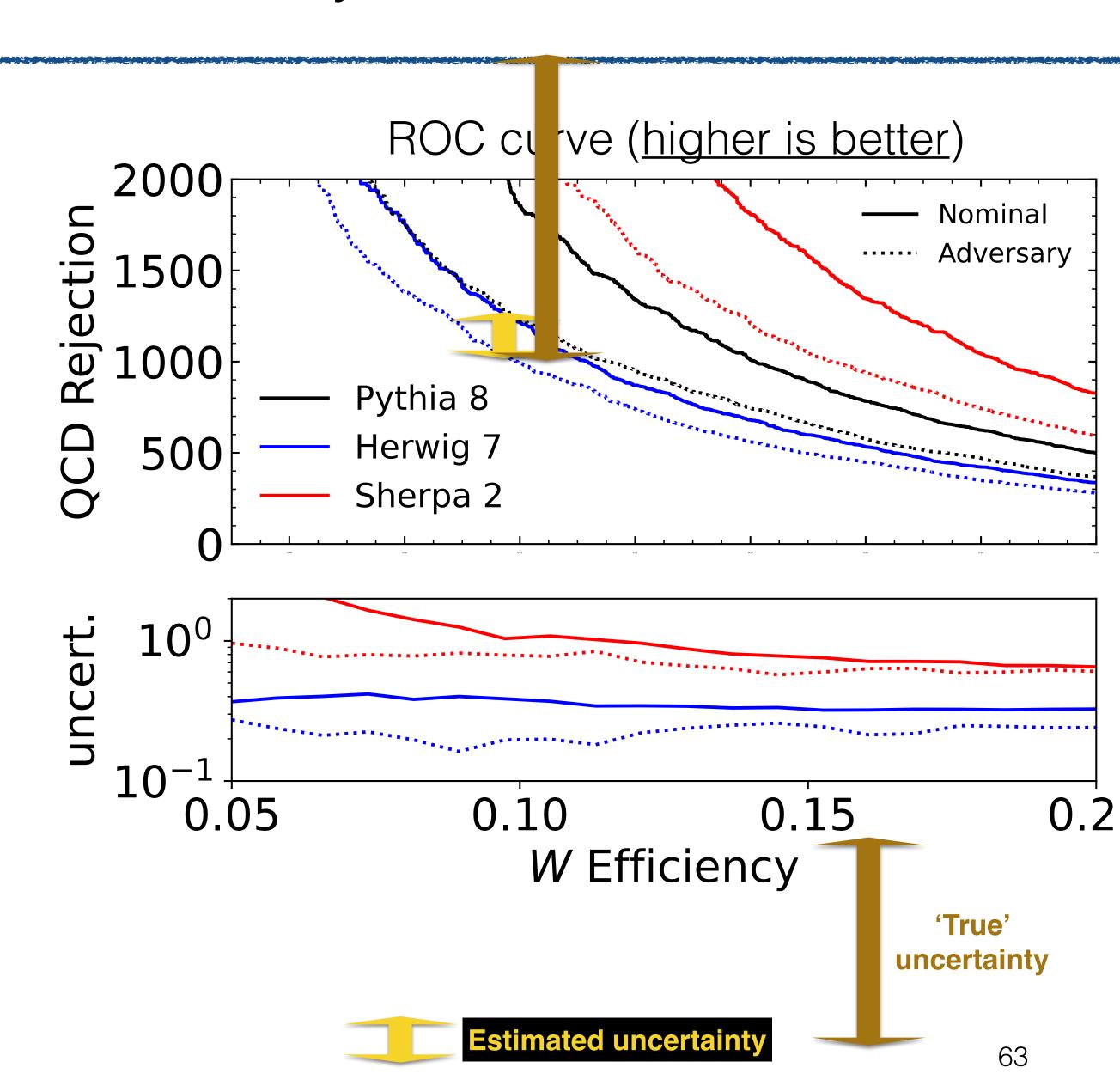


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Make correction in UQ for EW processes

Process	$n_{\rm part}$	$\Delta\sigma/\sigma_0$	$\frac{\sigma_{ m NLO} - \sigma_0}{\Delta \sigma}$	$\Delta\sigma_{ m ref}/\sigma_0$	$rac{\sigma_{ m NLO} - \sigma_0}{\Delta \sigma_{ m ref}}$
p p > wpm	1	1.54×10^{-1}	1.84	1.47×10^{-1}	1.92
p p > wpm j	2	1.97×10^{-1}	1.96	2.94×10^{-1}	1.31
p p > wpm j j	3	2.45×10^{-1}	0.59	4.41×10^{-1}	0.33
p p > wpm j j j	4	4.10×10^{-1}	0.25	5.88×10^{-1}	0.18
p p > z	1	1.46×10^{-1}	1.87	1.47×10^{-1}	1.86
p p > z j	2	1.93×10^{-1}	1.82	2.94×10^{-1}	1.19
p p > z j j	3	2.43×10^{-1}	0.56	4.41×10^{-1}	0.31
p p > z j j j	4	4.08×10^{-1}	0.27	5.88×10^{-1}	0.19
рр > а ј	2	3.12×10^{-1}	5.33	2.94×10^{-1}	5.66
рр > ајј	3	3.28×10^{-1}	TATOMINICAL CONTRACTOR	4.41×10^{-1}	0.63
p p > w+ w- wpm	3	1.00×10^{-3}	7	4.41×10^{-1}	1.39
p p > z w + w -	3	8.00×10^{-3}	92.39	4.41×10^{-1}	1.68
p p > z z wpm	3	1.00×10^{-2}	85.00	4.41×10^{-1}	1.93
p p > z z z	3	1.00×10^{-3}	302.75	4.41×10^{-1}	0.69
p p > a w + w -	3	1.90×10^{-2}	42.33	4.41×10^{-1}	1.82
p p > a a wpm	3	4.40×10^{-2}	47.24	4.41×10^{-1}	4.72
p p > a z wpm	3	1.00×10^{-3}	1244.49	4.41×10^{-1}	2.82
p p > a z z	3	2.00×10^{-2}	17.24	4.41×10^{-1}	0.78

Surviving tails

Process	n_{part}	$\Delta\sigma/\sigma_0$	$\frac{\sigma_{\rm NLO}-\sigma_0}{\Delta\sigma}$	$\Delta\sigma_{ m ref}/\sigma_0$	$\frac{\sigma_{ m NLO}-\sigma_0}{\Delta\sigma_{ m ref}}$
p p > h	1 3.	48 × 10 ⁻¹	3.02	1.47×10^{-1}	7.15

Large corrections loop-induced 2->1 process

Universe is a perfect simulator

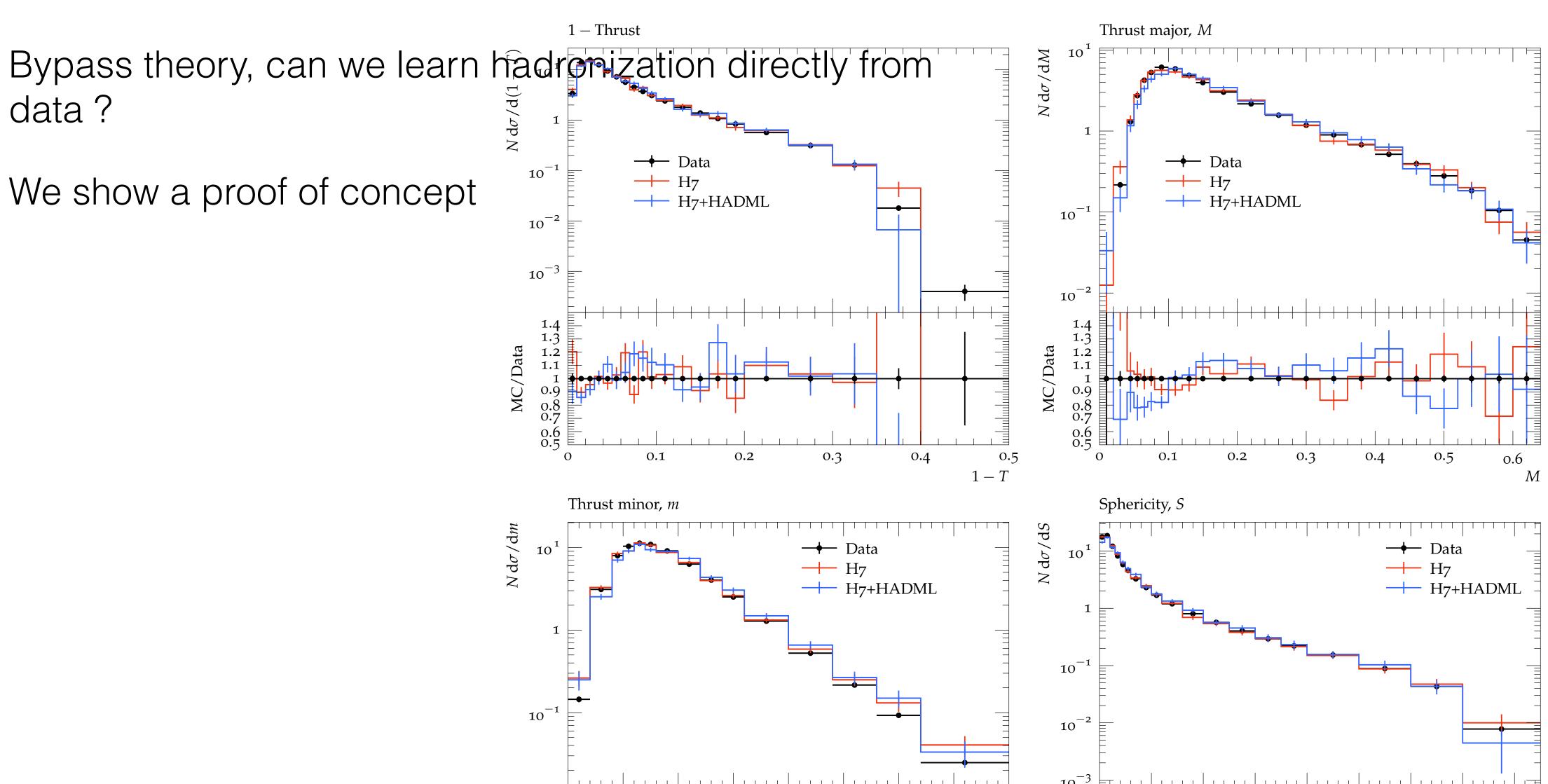
PRD.106.096020: Aishik Ghosh, Xiangyang Ju, Benjamin Nachman, and Andrzej Siodmok

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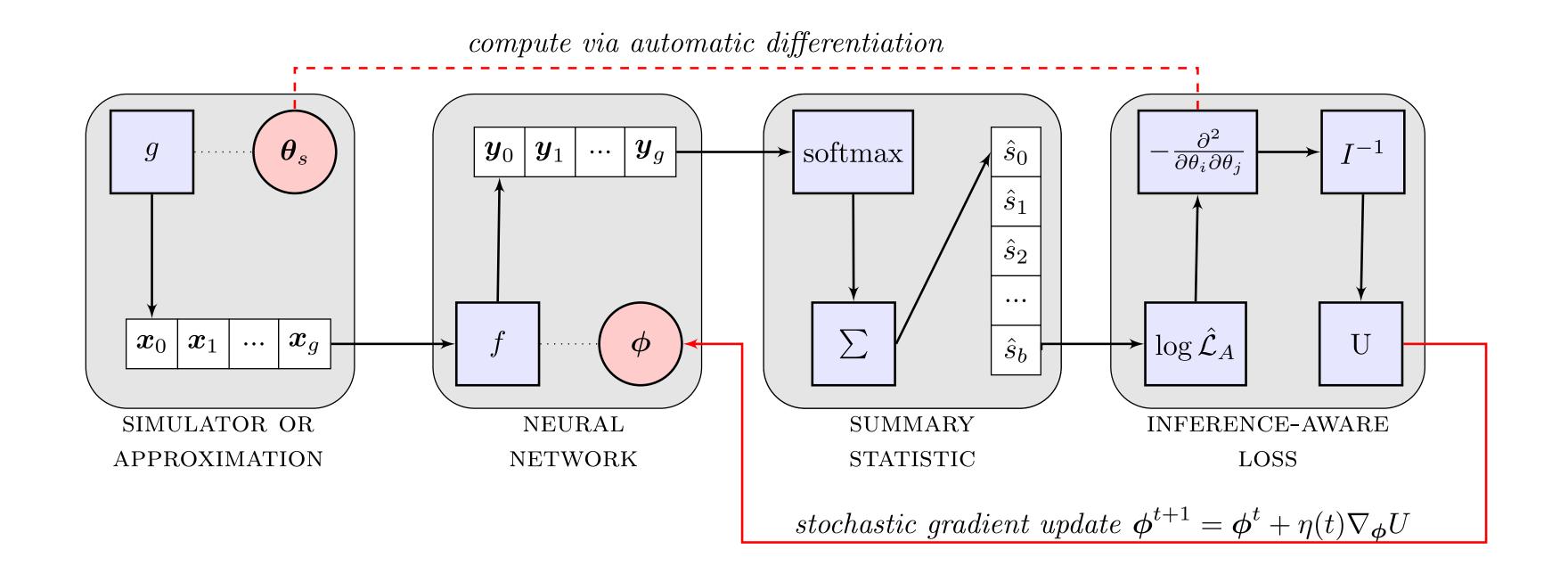
data?

We show a proof of concept



Example 1: INFERNO

- Write your analysis code differentiably, use uncertainty on final measurement as loss function
- Model is like a multi-class classifier, but classes have no meaning —> no concept of AUC
- · Evaluation: Poisson fit of simulation vs data in each category, similar to histograms

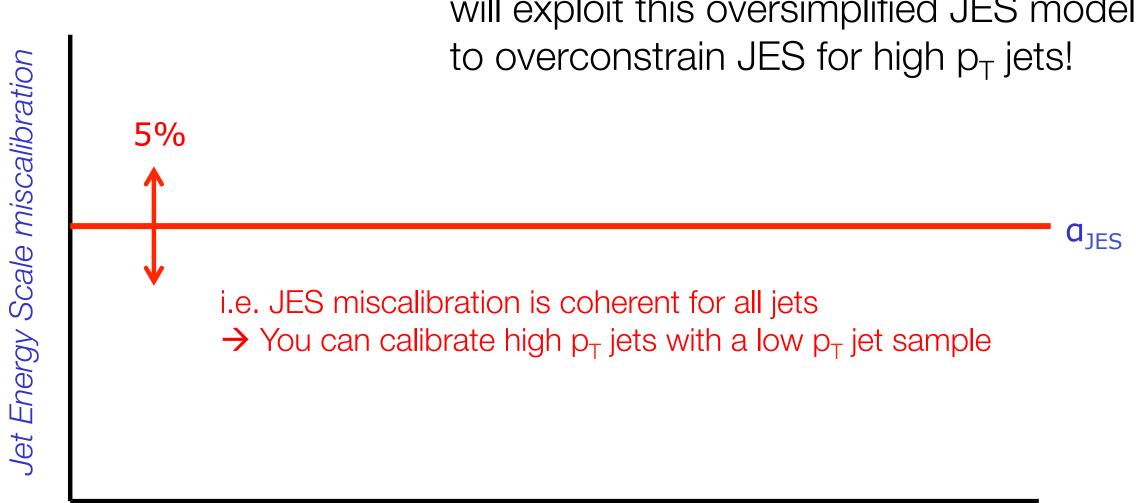


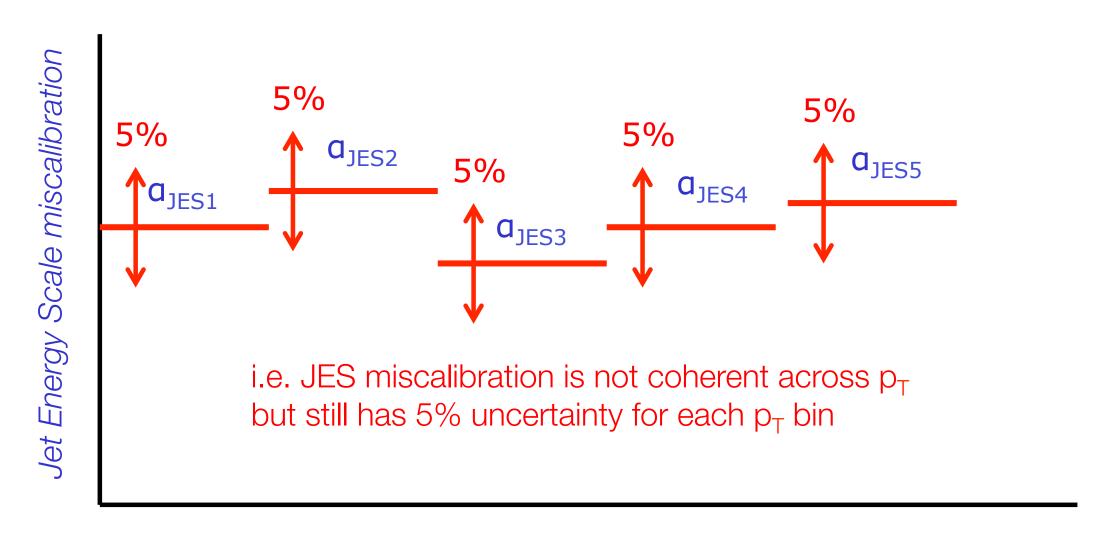
Overconstraining NP

From W. Verkerke:

Our modelling of NPs might be over-simplified

If you assume one NP – chances are that your physics Likelihood will exploit this oversimplified JES model





Jet p_T