

# Gauged Quintessence

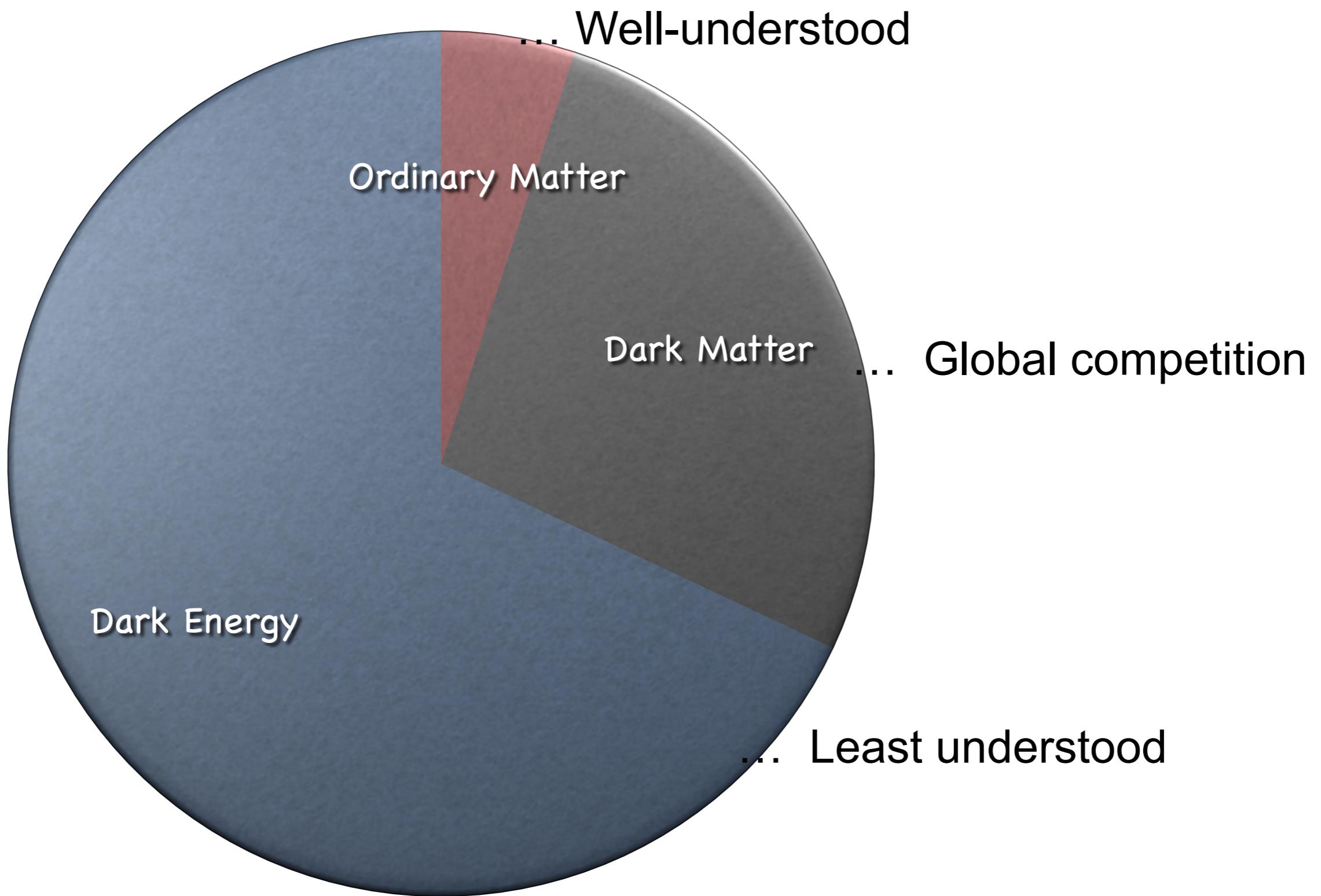
Hye-Sung Lee  
(KAIST)

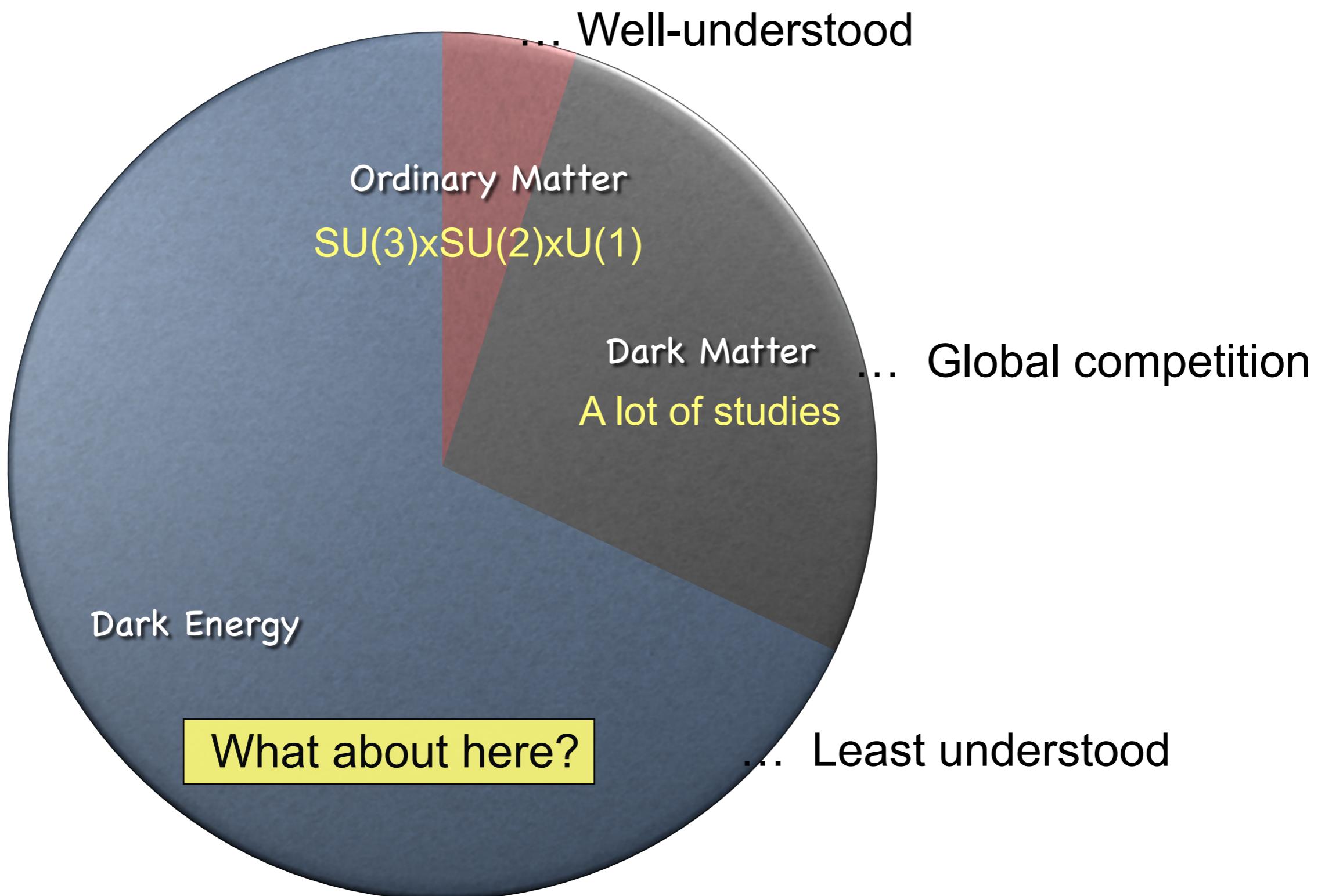
based on JCAP 02 (2023) 005 & work in progress  
with Kunio Kaneta, Jiheon Lee, Jaeok Yi

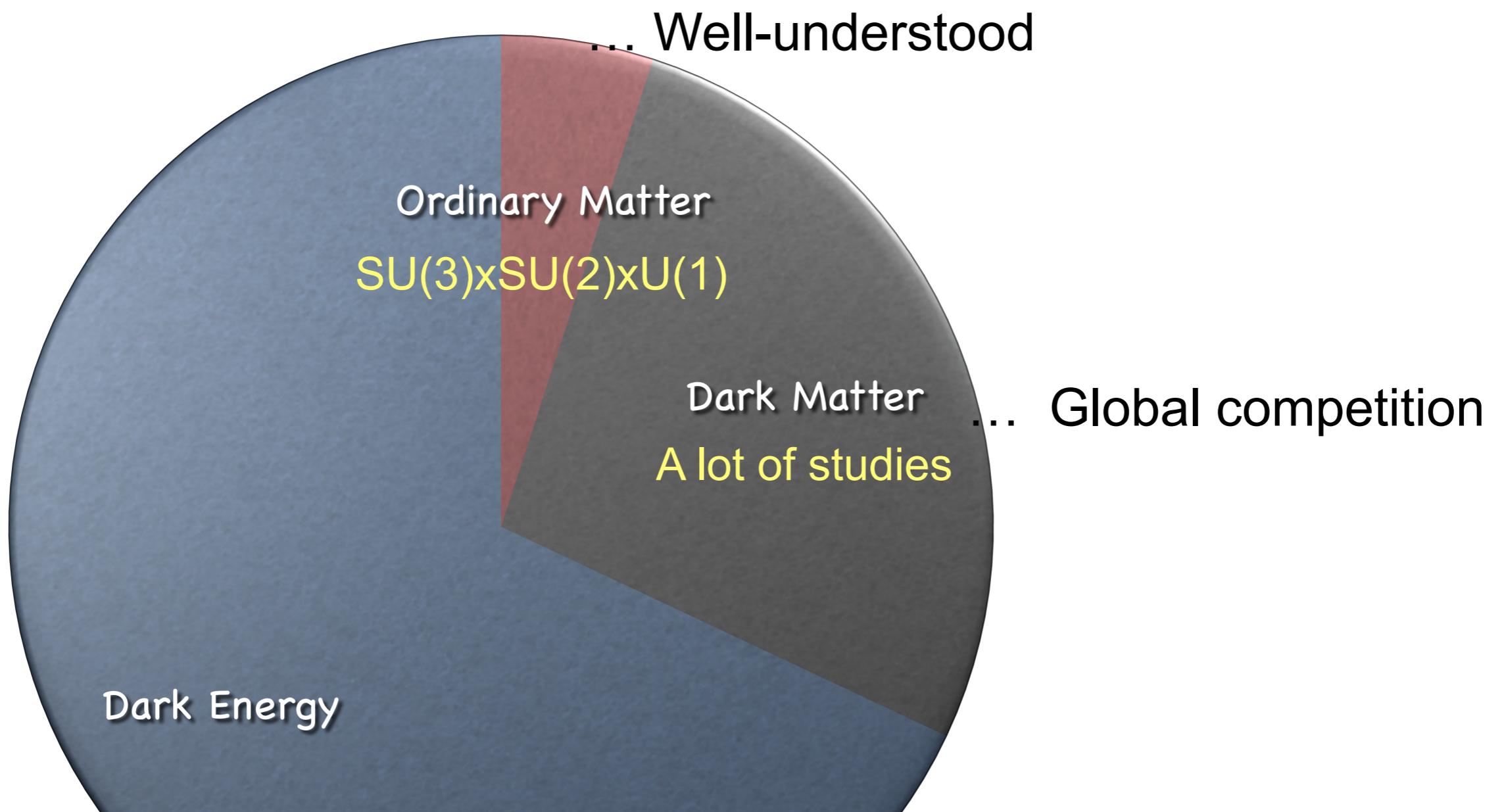
KIAS Seminar (May 4, 2023)

The universe is an enormous direct product of representations of symmetry groups.

- Steven Weinberg -







Quintessence [Ratra, Peebles (1988)]  
: first dark energy field model with a singlet scalar

Gauged Quintessence [Kaneta, LEE, Lee, Yi (2023)]  
: first gauge symmetry model  
in the quintessence scalar field

# Why dark energy symmetry?

New particles/fields were often followed by a new gauge symmetry.

- (i) Neutrino (to explain energy spectrum in beta decay) [Pauli 1930]  
→ weak interaction [Fermi 1934] (later identified as the SU(2)).
- (ii) Quark (to explain plethora of hadrons) [Gell-Mann, Zweig 1964]  
→ SU(3) gauge strong interaction [Han & Nambu 1965]
- (iii) Dark matter (to explain galaxy rotation curve) [Rubin 1970's]  
→ Dark matter symmetry? [Numerous studies]
- (iii) Dark energy field (to explain accelerated expansion) [Ratra & Peebles 1988]  
→ Dark energy symmetry?

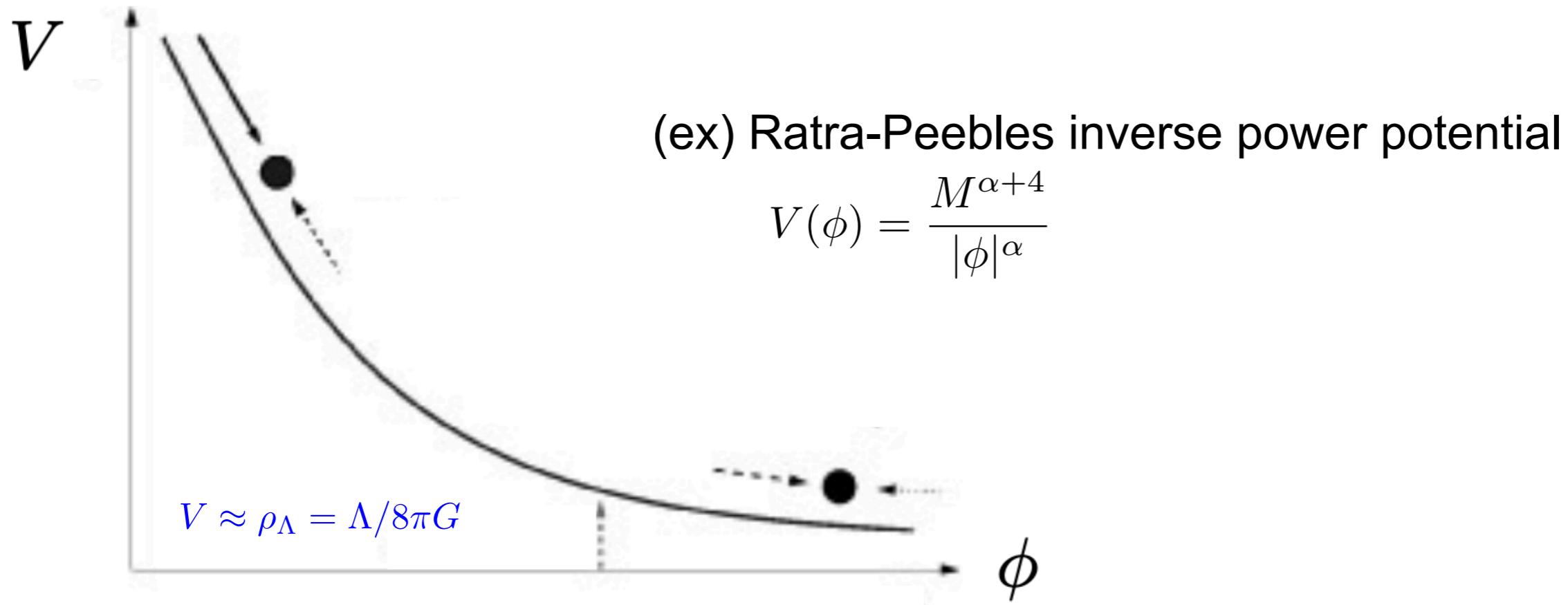
A new gauge symmetry may help understanding the new particles/fields.

## Outline of this talk

1. Quintessence at a glance
2. Gauged quintessence
3. Coherent dark gauge boson
4. Evolution of the universe
5. Remarks on the Hubble tension
6. Summary and Outlooks

# Quintessence at a glance

# Quintessence



## Quintessence

- Proposed by Ratra and Peebles (1988).
- Dynamic dark energy model with a scalar field ( $\phi$ ).
- A scalar rolls down a potential slowly in the present universe.
- Its potential energy is identified as the dark energy.
- Tracking behavior: The  $\phi$  initial value does not really matter. Only the potential determines the the present time value of  $\phi$  and its equation of state (addressing the cosmological coincidence problem) [Steinhardt, Wang, Zlatev (1999)].

# Quintessence

$$S = \int d^4x \sqrt{-g} \left[ \frac{1}{2} m_{Pl}^2 R - \frac{1}{2} (\partial_\mu \phi)^2 - V(\phi) \right]$$

$$g_{\mu\nu} = \text{Diag}\{-1, a(t)^2, a(t)^2, a(t)^2\}$$

$$m_\phi^2 = \frac{\partial^2 V}{\partial \phi^2} \quad (m_\phi \text{ decreases for a Ratra-Peebles potential.})$$

$$\ddot{\phi} + 3H\dot{\phi} + \frac{\partial V}{\partial \phi} = 0 \quad (\text{equation of motion})$$

$$H \equiv \frac{\dot{a}}{a} \quad (\text{Hubble parameter})$$

$$w \equiv \frac{p}{\rho} = \frac{\frac{1}{2}\dot{\phi}^2 - V}{\frac{1}{2}\dot{\phi}^2 + V} \quad (\text{equation of state})$$

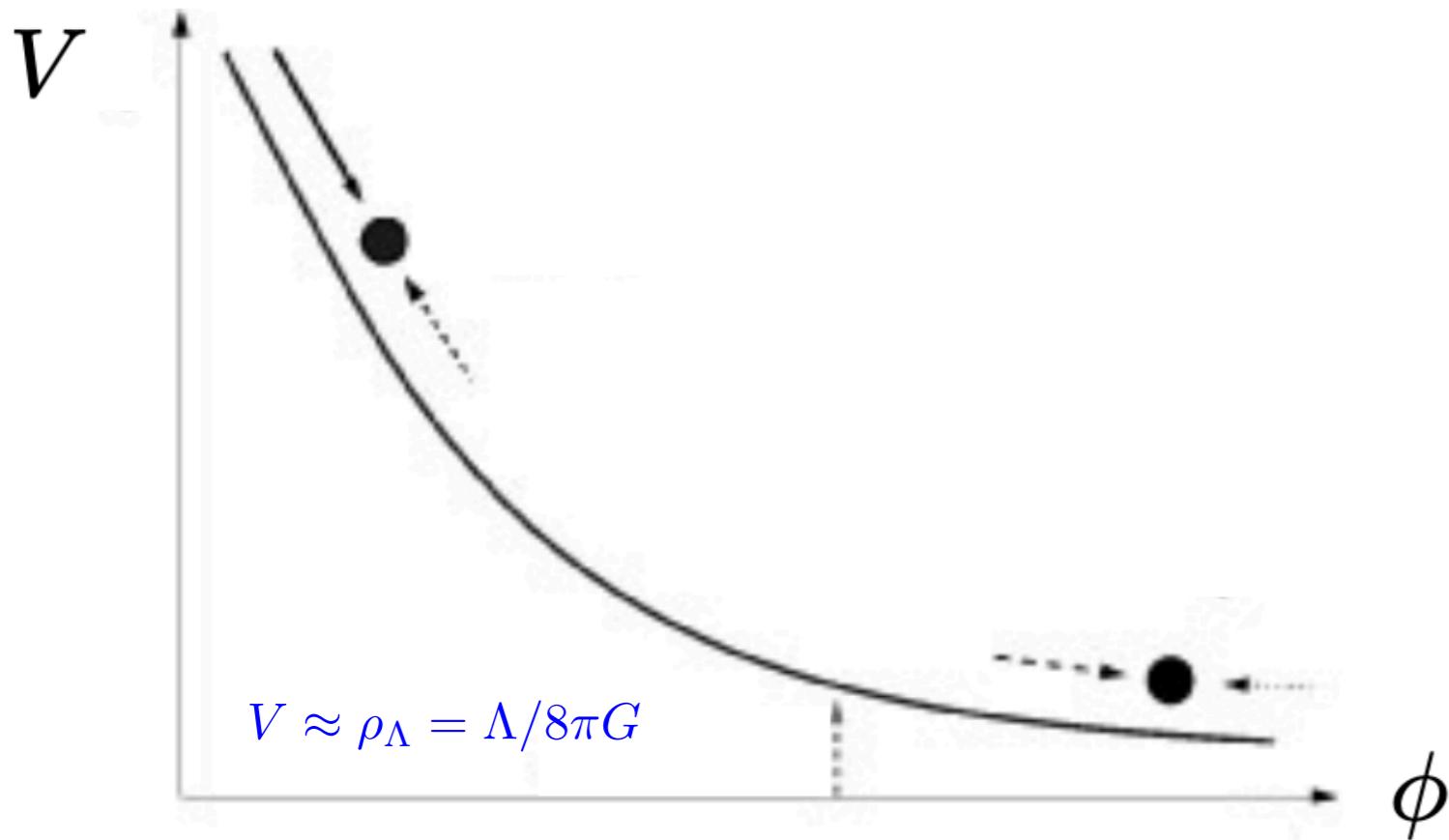
$$\rho \propto a^{-3(1+w)}$$

$$= -1 + \frac{\dot{\phi}^2}{V} + \dots \quad \text{for } \dot{\phi}^2 \ll V(\phi) \quad (\text{slow-roll})$$

$$\frac{\ddot{a}}{a} = -\frac{4\pi G}{3}(1+3w)\rho$$

( $w < -1/3$  for the accelerated expansion.  $w = -1$  for  $\Lambda$ )

# Quintessence

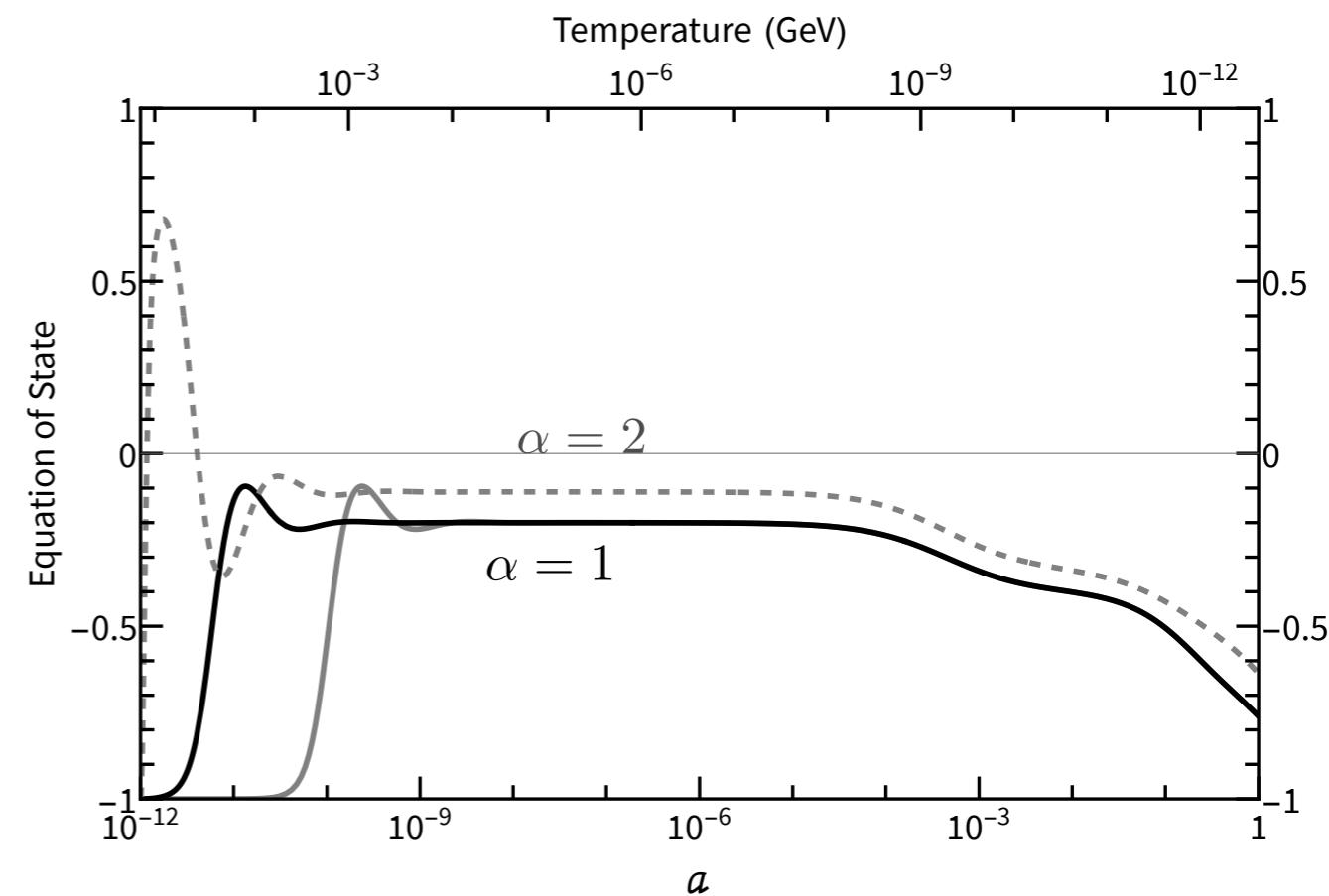
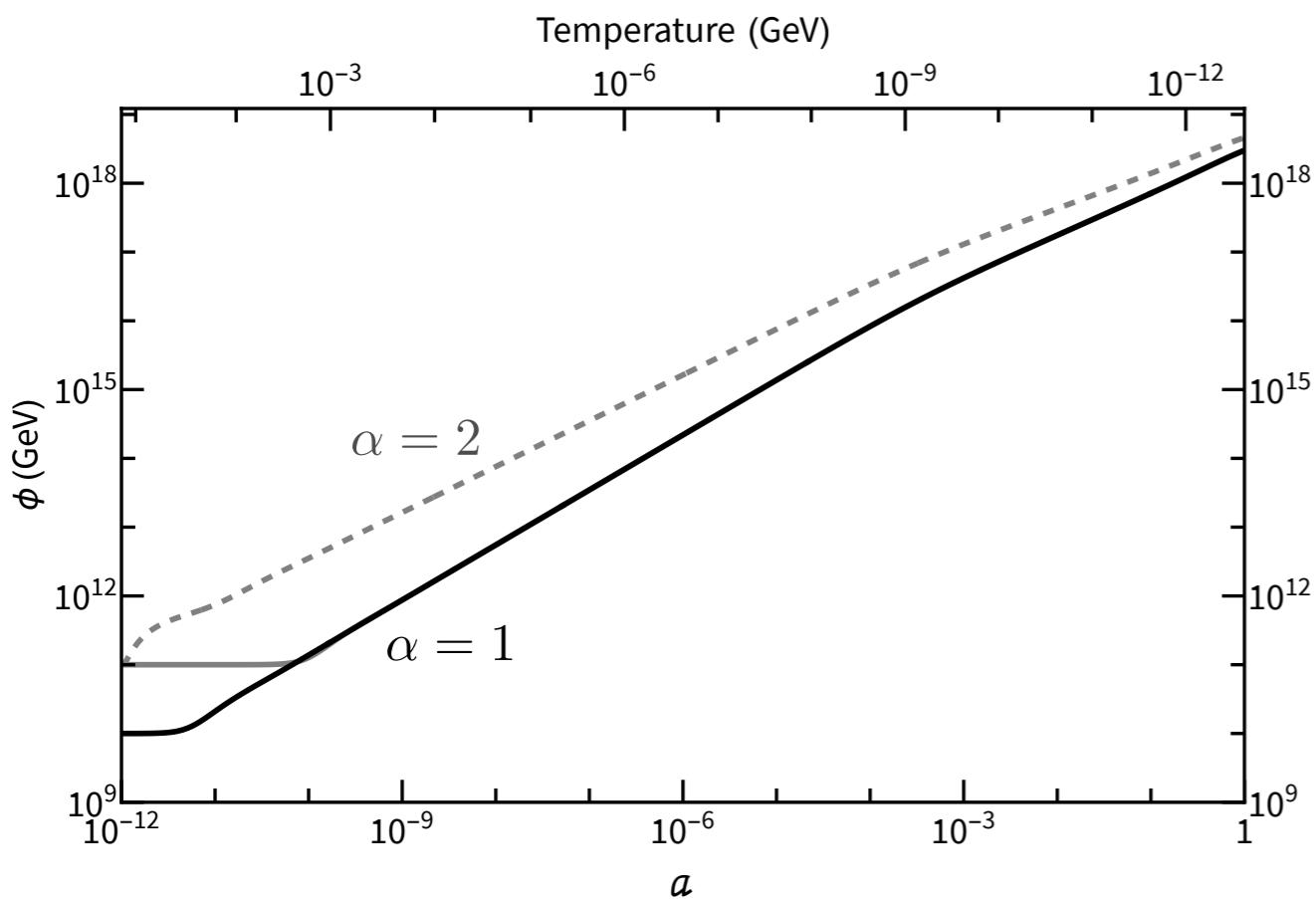


Conditions for the quintessence dark energy

$$V \sim 10^{-123} M_{Pl}^4 \sim 3 \times 10^{-47} \text{ GeV}^4 \quad (\text{present dark energy density})$$

$$m_\phi \lesssim H_0 \sim 10^{-42} \text{ GeV} \quad (\text{slow-roll})$$

# Quintessence dynamics (without a gauge symmetry)



$$\ddot{\phi} + 3H\dot{\phi} + \frac{\partial V}{\partial \phi} = 0$$

$$V(\phi) = \frac{M^{\alpha+4}}{|\phi|^\alpha}$$

Balancing between the potential slope and Hubble friction results in the common tracking solution for the quintessence. The present values are not sensitive to its initial values (quintessence tracking behavior).

# Gauged quintessence

# Gauged Quintessence

We introduce a dark U(1) gauge symmetry to the quintessence scalar.

$$\Phi = \frac{1}{\sqrt{2}} \phi e^{i\eta} \quad : \text{complex scalar under the } U(1)_{\text{dark}} \text{ gauge symmetry}$$

( $\phi$  : quintessence scalar)

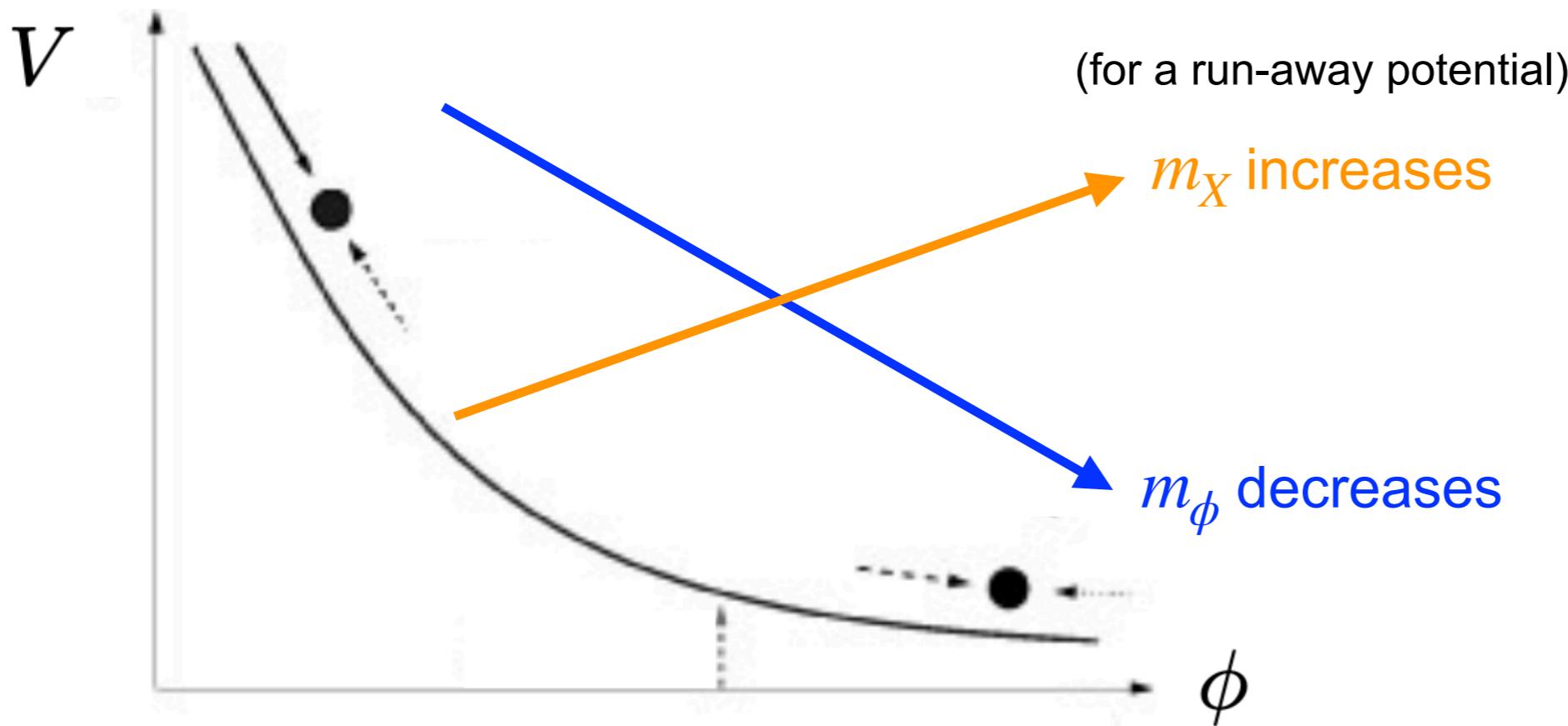
( $\eta$  : longitudinal component of the dark gauge boson  $X$ )

$$\begin{aligned} S &= \int d^4x \sqrt{-g} \left[ \frac{1}{2} m_{Pl}^2 R - |D_\mu \Phi|^2 - V_0(\Phi) - \frac{1}{4} \mathbb{X}_{\mu\nu} \mathbb{X}^{\mu\nu} \right] \quad D_\mu \equiv \partial_\mu + ig_X \mathbb{X}_\mu \\ &= \int d^4x \sqrt{-g} \left[ \frac{1}{2} m_{Pl}^2 R - \frac{1}{2} (\partial_\mu \phi)^2 - V_0(\phi) - \frac{1}{4} X_{\mu\nu} X^{\mu\nu} - \frac{1}{2} g_X^2 \phi^2 X_\mu X^\mu \right] \\ &\quad \text{(in unitary gauge : } \eta = 0, \quad X_\mu = \mathbb{X}_\mu + \frac{1}{g_X} \partial_\mu \eta) \end{aligned}$$

$V_{\text{gauge}}$

$$m_\phi^2|_0 = \frac{\partial^2 V_0}{\partial \phi^2} + \frac{\partial^2 V_{\text{gauge}}}{\partial \phi^2}, \quad m_X^2|_0 = g_X^2 \phi^2 \quad \text{(tree-level masses)}$$

# Masses vary over cosmic evolution



As the quintessence  $\phi$  rolls down the potential,  
both  $m_\phi$  and  $m_X$  change over cosmic evolution.

$$m_\phi^2|_0 = \frac{\partial^2 V_0}{\partial \phi^2} + \frac{\partial^2 V_{\text{gauge}}}{\partial \phi^2}, \quad m_X^2|_0 = g_X^2 \phi^2$$

# Gauged Quintessence

Equations of motion for  $\phi$  and  $X$  (coupled via  $V_{\text{gauge}}$ )

$$\ddot{\phi} + 3H\dot{\phi} + \frac{\partial V_0}{\partial \phi} + g_X^2 X_\mu X^\mu \phi = 0$$

$$\partial_\mu X^{\mu\nu} + 3H X^{0\nu} - g_X^2 \phi^2 X^\nu = 0$$

$$V_{\text{gauge}} = \frac{1}{2} g_X^2 \phi^2 X_\mu X^\mu$$

Energy-momentum tensor

$$T_{\mu\nu} = (\partial_\mu \phi)(\partial_\nu \phi) - \frac{1}{2} g_{\mu\nu} (\partial_\alpha \phi)(\partial^\alpha \phi) - g_{\mu\nu} V_0(\phi)$$

$$- \frac{1}{2} g_{\mu\nu} g_X^2 \phi^2 X_\alpha X^\alpha + g_X^2 \phi^2 X_\mu X_\nu + X_{\mu\alpha} X_\nu^\alpha - \frac{g_{\mu\nu}}{4} X_{\alpha\beta} X^{\alpha\beta}$$

# Boltzmann equations for mass varying $\phi$ and $X$

$$\dot{\rho}_\phi + 3H(\rho_\phi + p_\phi) = -\frac{\dot{m}_X}{m_X}(\rho_X - 3p_X)$$

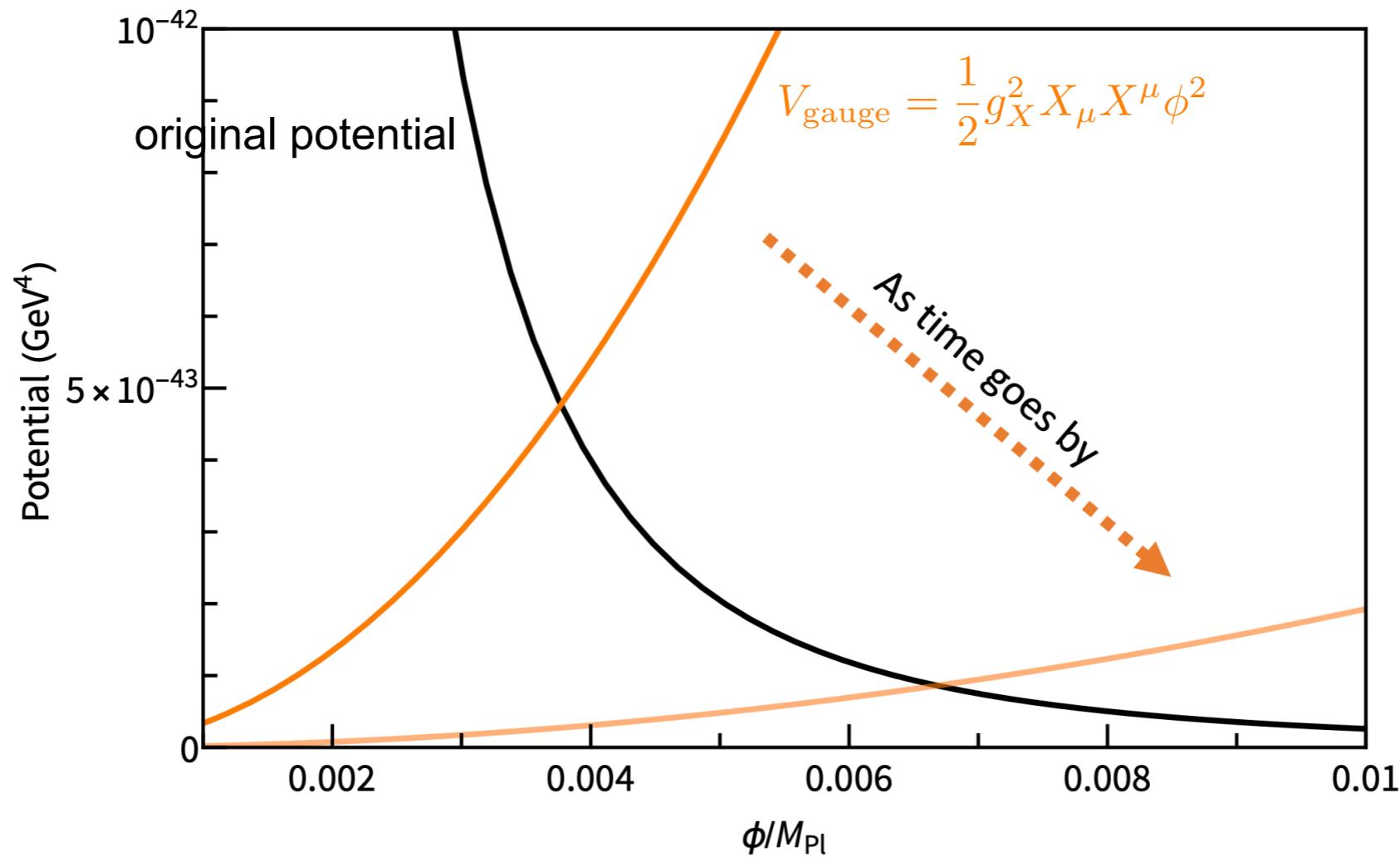
$$\dot{\rho}_X + 3H(\rho_X + p_X) = \frac{\dot{m}_X}{m_X}(\rho_X - 3p_X)$$

The energy flow between the quintessence scalar and the dark gauge boson is proportional to the  $\dot{m}_X$ .

$\dot{m}_X > 0$  : Energy flows from  $\phi$  to  $X$

$\dot{m}_X < 0$  : Energy flows from  $X$  to  $\phi$

# Potential modified by the gauge symmetry



$$V = V_0 + \frac{1}{2} g_X^2 X_\mu X^\mu \phi^2$$

# Quantum corrections in the gauged quintessence

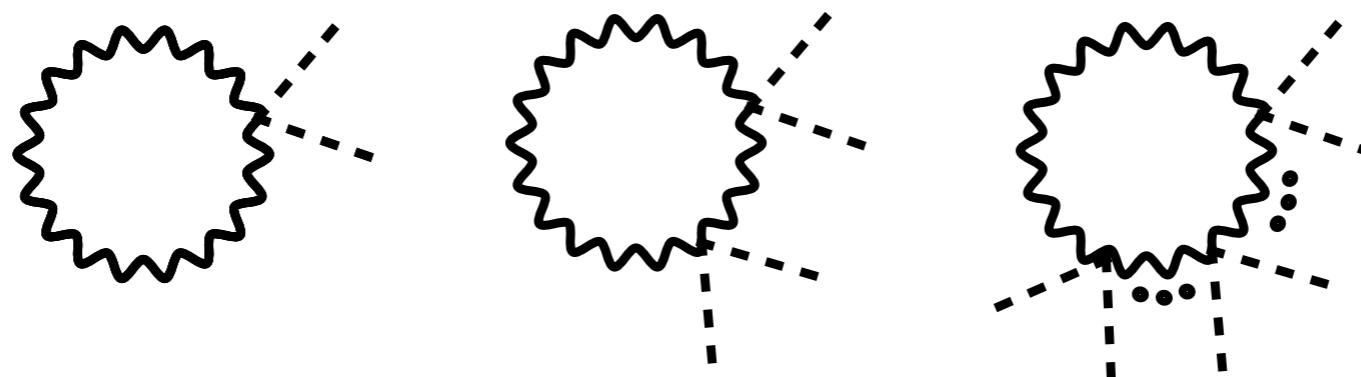
1-loop effective potential in the gauged quintessence model

$$V_{\text{eff}} = V_0 + \frac{1}{2} g_X^2 X_\mu X^\mu \phi^2 + \frac{\Lambda^2}{32\pi^2} V_0'' + \frac{(V_0'')^2}{64\pi^2} \left( \ln \frac{V_0''}{\Lambda^2} - \frac{3}{2} \right) + \frac{3(m_X^2|_0)^2}{64\pi^2} \left( \ln \frac{m_X^2|_0}{\Lambda^2} - \frac{5}{6} \right)$$



1-loop correction of the quintessence

Additional 1-loop correction due to the  $X$ -boson



# Quantum corrections in the gauged quintessence

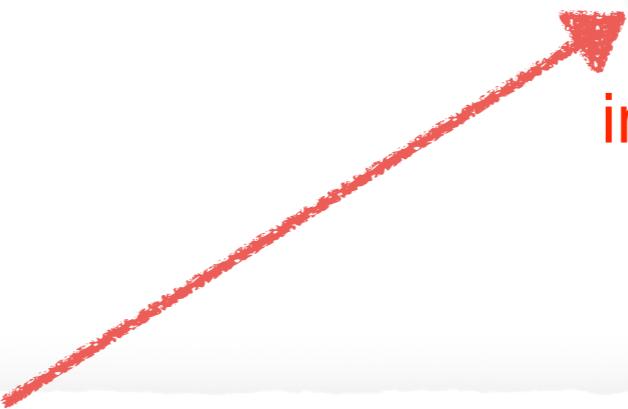
1-loop effective potential in the gauged quintessence model

$$V_{\text{eff}} = V_0 + \frac{1}{2} g_X^2 X_\mu X^\mu \phi^2 + \frac{\Lambda^2}{32\pi^2} V_0'' + \frac{(V_0'')^2}{64\pi^2} \left( \ln \frac{V_0''}{\Lambda^2} - \frac{3}{2} \right) + \frac{3(m_X^2|_0)^2}{64\pi^2} \left( \ln \frac{m_X^2|_0}{\Lambda^2} - \frac{5}{6} \right)$$

$$m_\phi^2 = \frac{\partial^2 V_{\text{eff}}}{\partial \phi^2} = V_0'' + g_X^2 X_\mu X^\mu + \frac{\Lambda^2}{32\pi^2} V_0''' + \frac{V_0'' V_0'''}{32\pi^2} \left( \ln \frac{V_0''}{\Lambda^2} - 1 \right) + \frac{9g_X^2 m_X^2|_0}{16\pi^2} \left( \ln \frac{m_X^2|_0}{\Lambda^2} + \frac{1}{3} \right)$$

$$m_X^2 = g_X^2 \left( \phi^2 + \frac{V_0''}{32\pi^2} \ln \frac{V_0''}{\Lambda^2} \right)$$

independent of potential  $V_0$

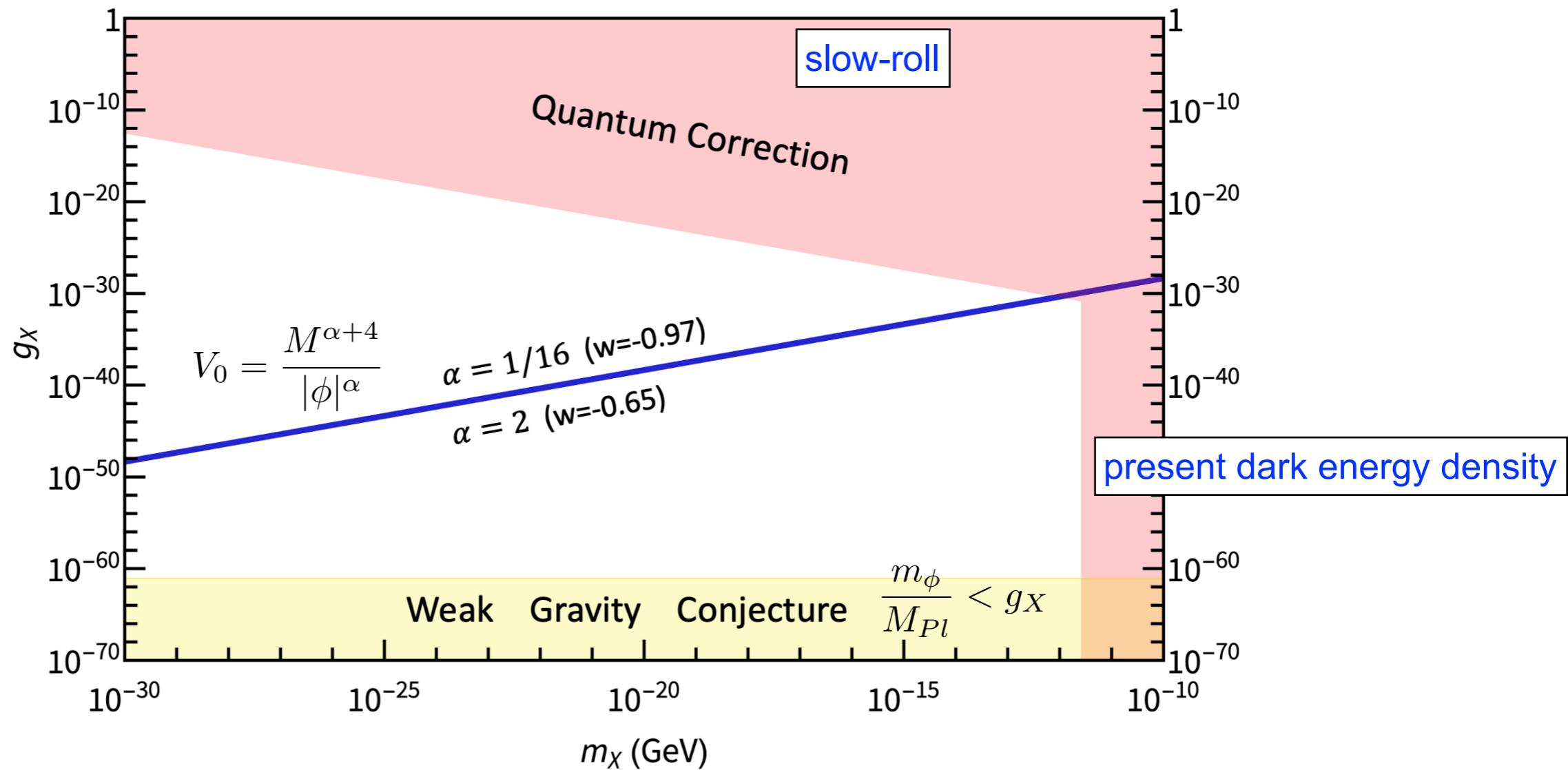


Conditions for the quintessence dark energy

$$V \sim 10^{-123} M_{Pl}^4 \sim 3 \times 10^{-47} \text{ GeV}^4 \quad (\text{present dark energy density})$$

$$m_\phi \lesssim H_0 \sim 10^{-42} \text{ GeV} \quad (\text{slow-roll})$$

# Potential-independent constraints (at present universe)



(Blue band: Ratra-Peebles potential case with the tracking behavior.)

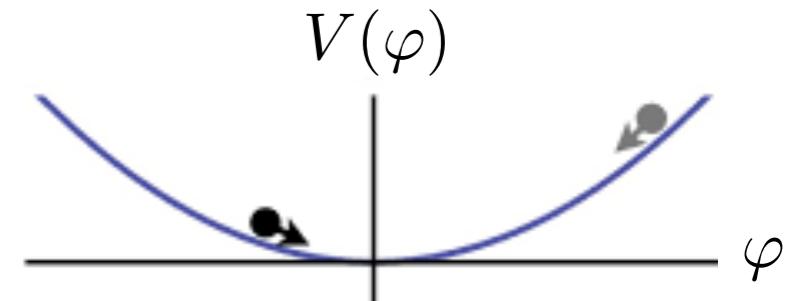
# Coherent dark gauge boson

# Misalignment mechanism for coherent scalar oscillation

[Preskill, Wise, Wilczek (1983)] [Abbott, Sikivie (1983)] [Dine, Fischler (1983)]

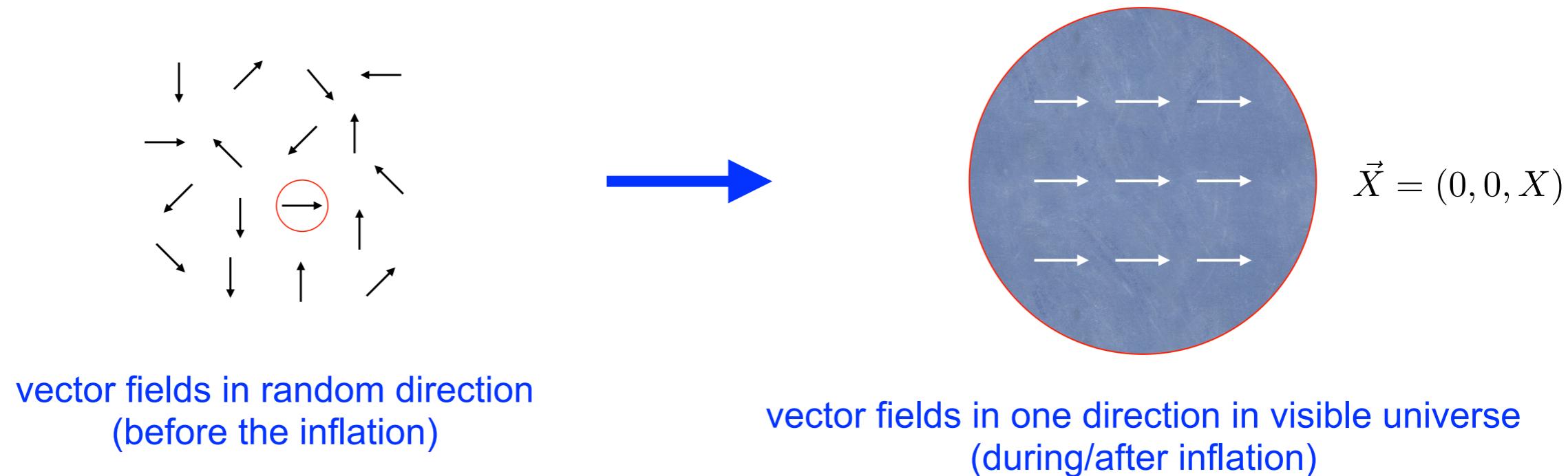
Misalignment mechanism is a popular production mechanism of a coherent scalar field (such as QCD axion DM).

$$\ddot{\varphi} + 3H\dot{\varphi} + m_\varphi^2\varphi = 0 \quad \rho_\varphi = \frac{1}{2}\dot{\varphi}^2 + \frac{1}{2}m_\varphi^2\varphi^2$$



- (i) Inflation makes  $\varphi$  spatially homogeneous:  $\varphi(t, \vec{x}) = \varphi(t)$ .
- (ii) Initially, Hubble friction is large ( $H > m_\varphi$ ), which makes  $\varphi$  frozen and  $\rho_\varphi$  constant.
- (iii) When Hubble friction decreases sufficiently ( $H \lesssim m_\varphi$ ), a coherent  $\varphi$  oscillation begins around the potential minimum.
- (iv) The oscillator has  $p_\varphi = 0$ , behaving as non-relativistic matter ( $\rho_\phi \propto a^{-3}$ );  $\varphi$  is a CDM despite of lightness. (QCD axion DM:  $m_a \sim 10^{-6} - 10^{-2}$  eV)

# Misalignment mechanism for coherent vector boson oscillation



$$\partial_\mu X^{\mu\nu} + 3H X^{0\nu} - m_X^2 X^\nu = 0$$

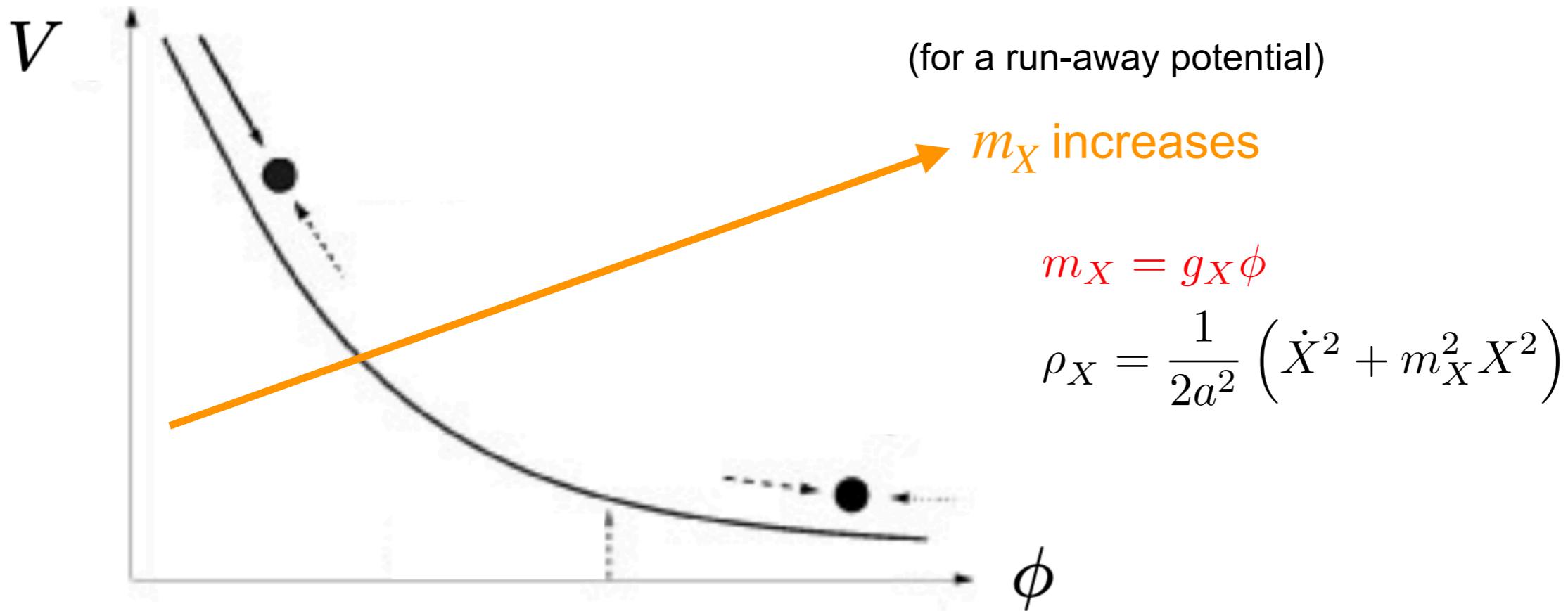
zero mode (spatially homogeneous):  $X_\mu(t, \vec{x}) = X_\mu(t) = (X_0(t), \vec{X}(t))$

$$X_0 = 0 \quad \ddot{X} + H\dot{X} + m_X^2 X = 0 \quad \rho_X = \frac{1}{2a^2} (\dot{X}^2 + m_X^2 X^2)$$

Unlike the scalar case, the  $\rho_X$  is highly suppressed by the scale factor, and it is hard to retain the  $\rho_X$  through the inflation. (Typical inflation e-folding is 60.)

Naive misalignment does not really work for a sizable vector boson production.

# Vector misalignment in the gauged quintessence model

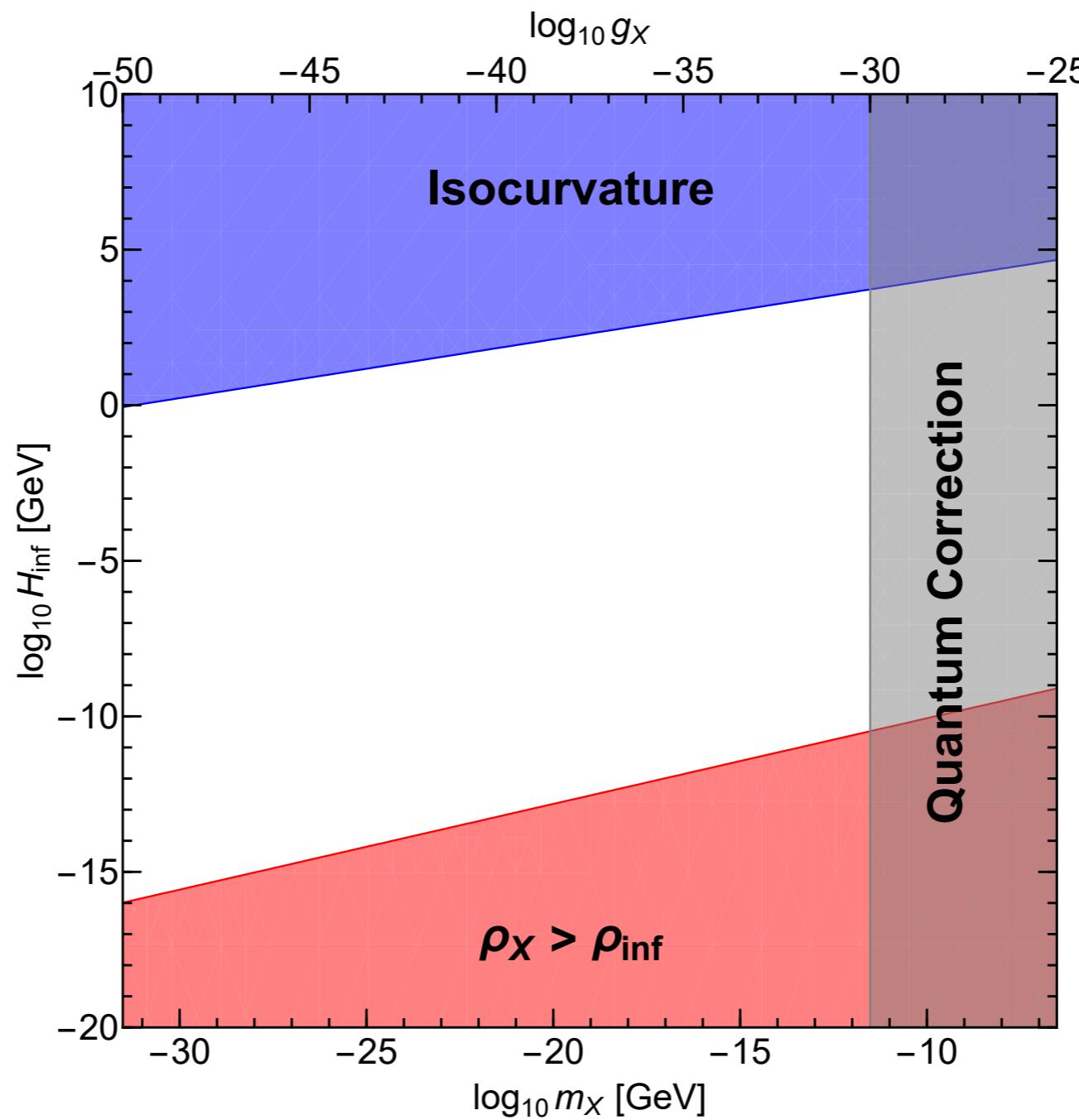


As  $\phi$  may increase by many orders of magnitude,  $m_X$  may increase by many orders of magnitude overcoming the suppression by the scale factor.

Preliminary

Misalignment mechanism with a mass-varying vector boson may work to produce a sizable vector boson energy density.

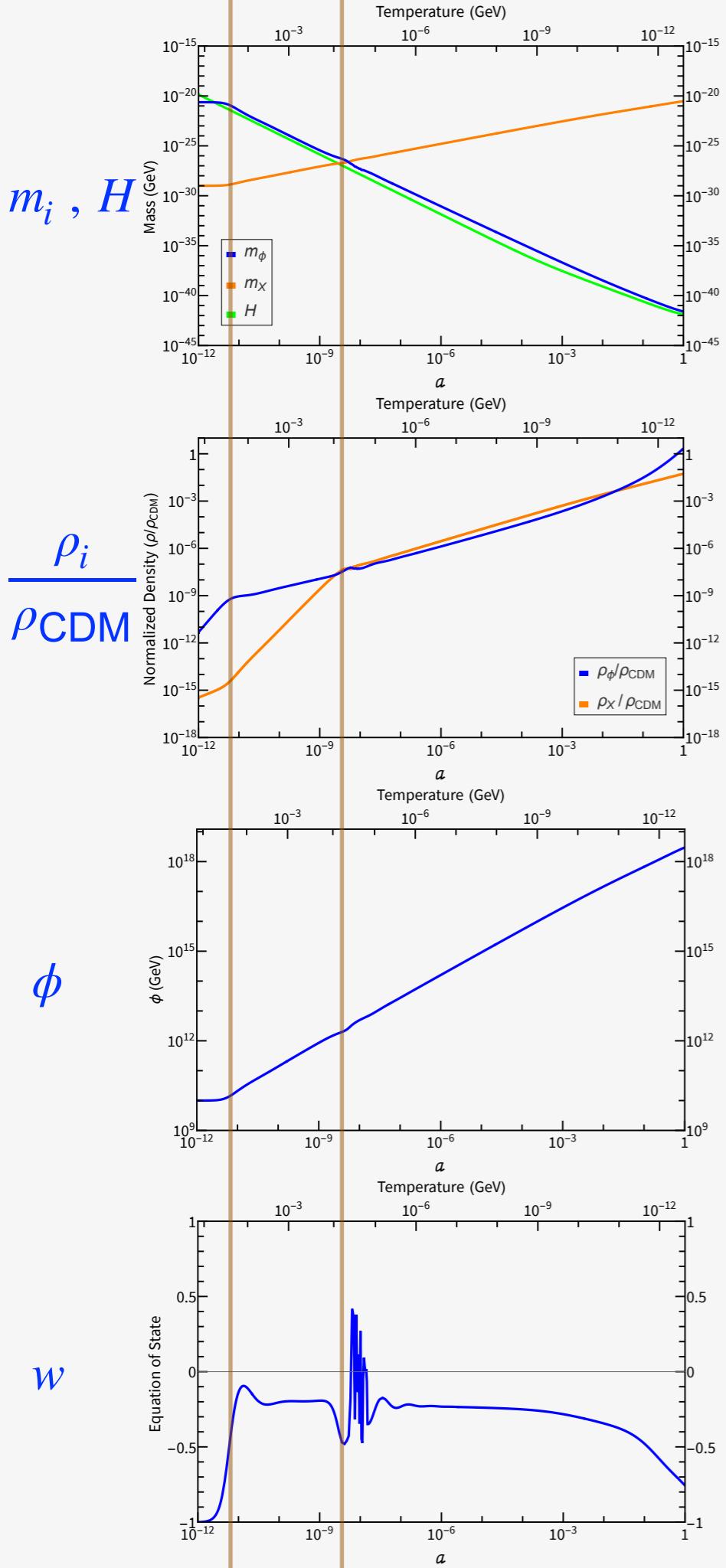
# Vector misalignment in the gauged quintessence model



Preliminary

Misalignment mechanism with a mass-varying vector boson may work to produce a sizable vector boson energy density.

# Evolution of the universe



$X$  may have a sizable relic density, but we assume it is a subdominant DM (less than 10% relic density of the dominant CDM).

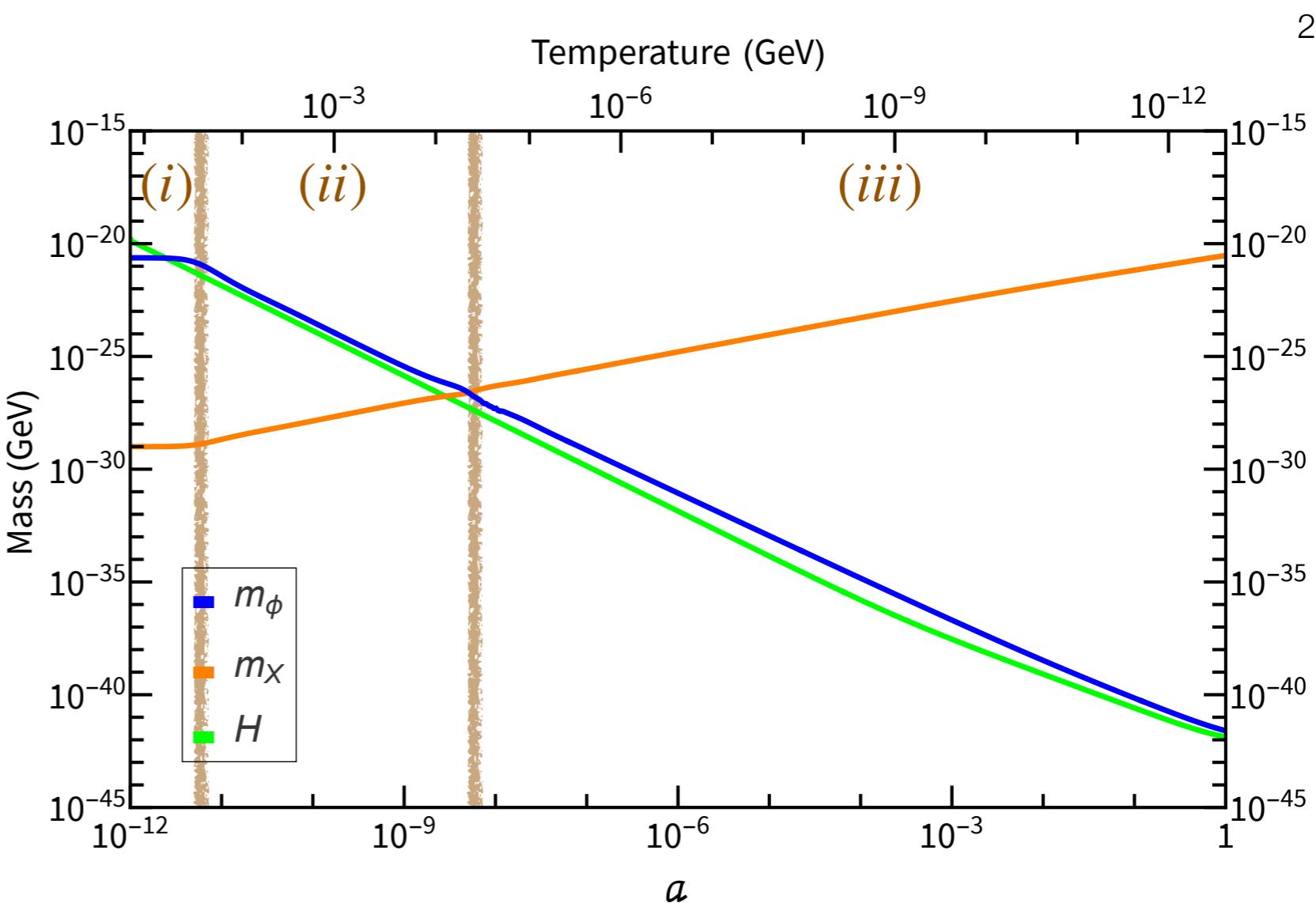
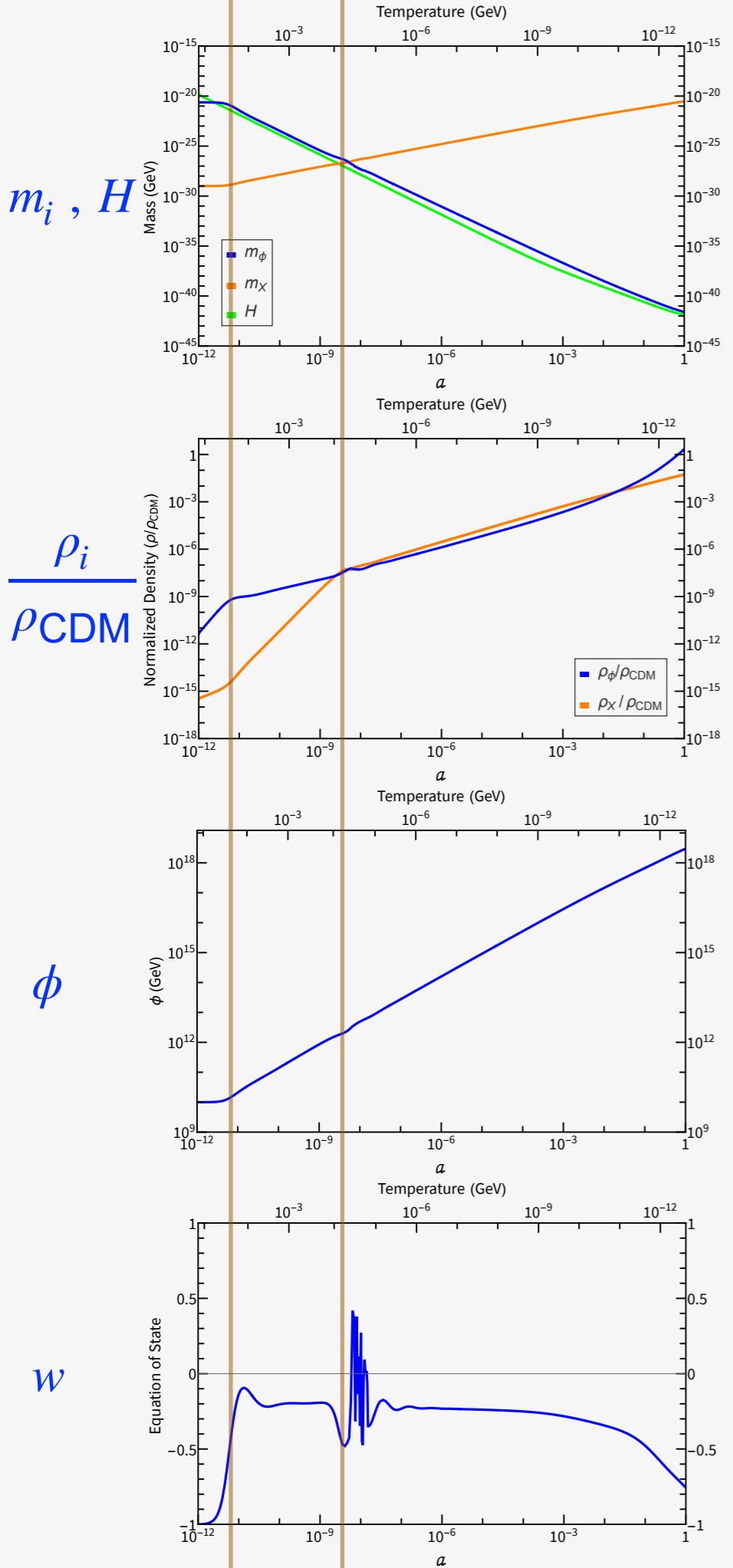
The dynamics of  $\phi$  and  $X$  change drastically when the hierarchy between  $m_\phi$ ,  $m_X$  and  $H$  change over time.

- (i)  $H > m_\phi, m_X$
- (ii)  $m_\phi > H > m_X$
- (iii)  $m_X, m_\phi > H$

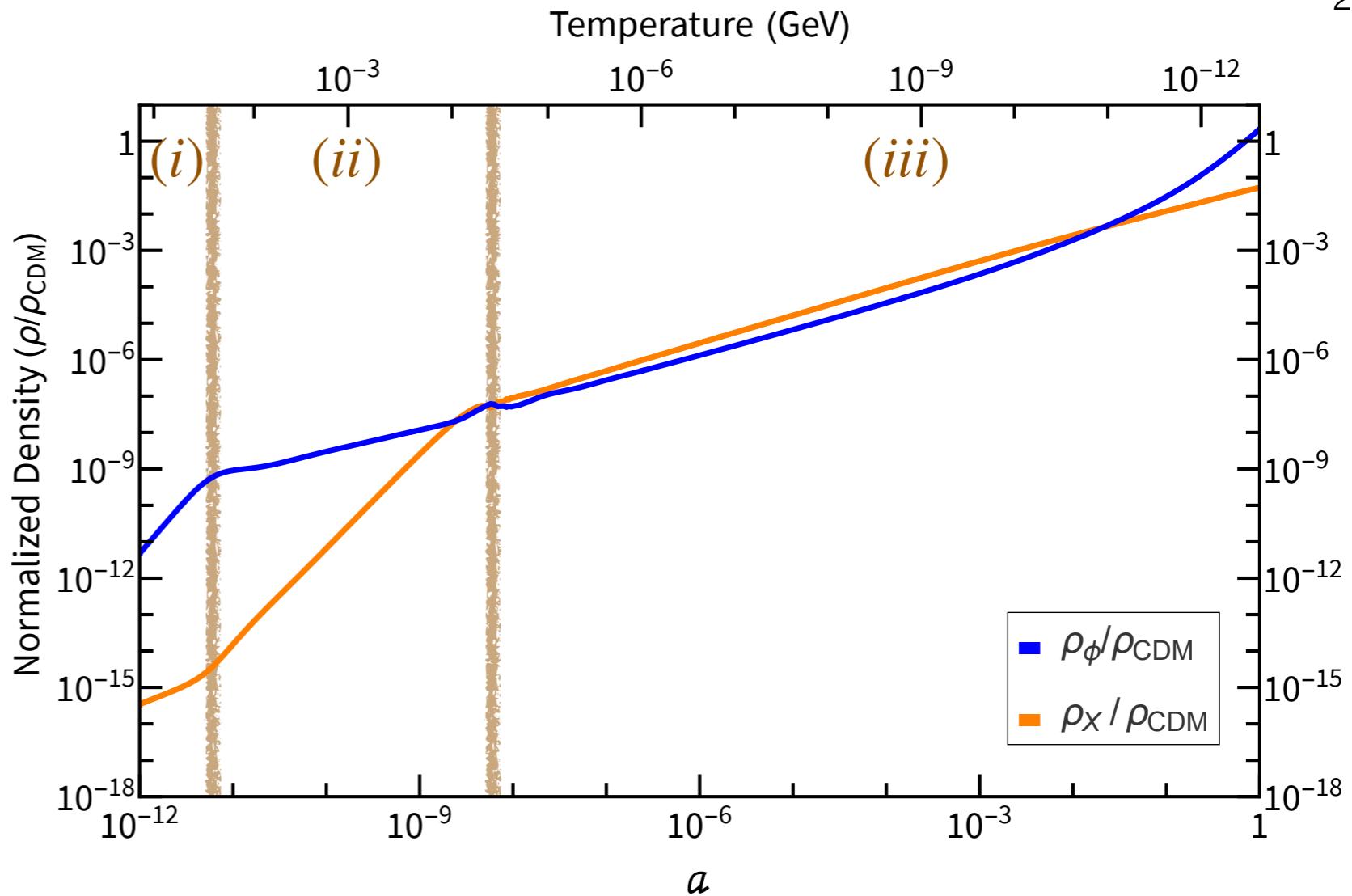
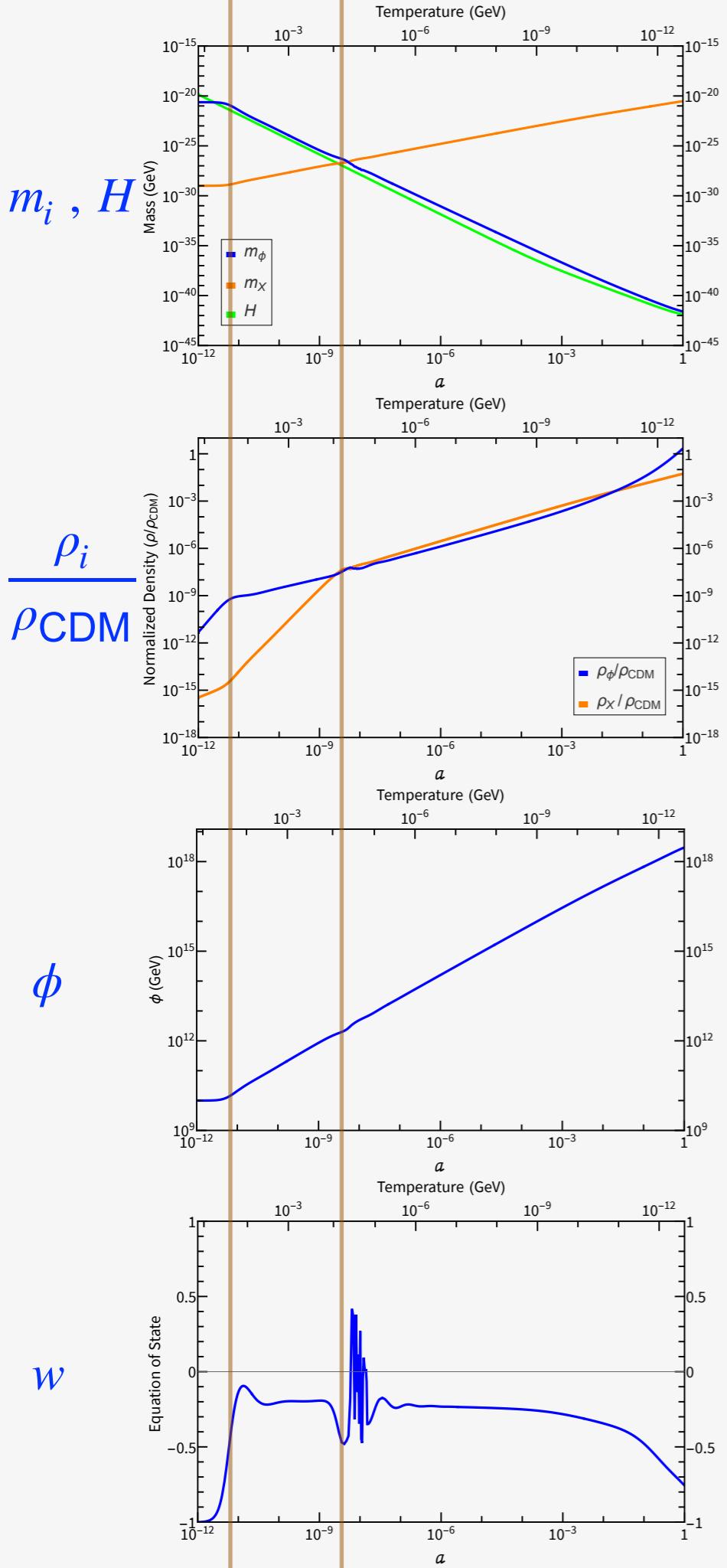
$$\ddot{\phi} + 3H\dot{\phi} + \frac{\partial V_0}{\partial \phi} + g_X^2 X_\mu X^\mu \phi = 0$$

$$\partial_\mu X^{\mu\nu} + 3H X^{0\nu} - g_X^2 \phi^2 X^\nu = 0$$

Benchmark parameters:  $\alpha = 1$ ,  $M = 2.2 \times 10^{-6}$  GeV,  $g_X = 10^{-39}$ ,  $\dot{X} = 0$ ,  $\dot{\phi} = 0$  (at  $a = 10^{-12}$ )

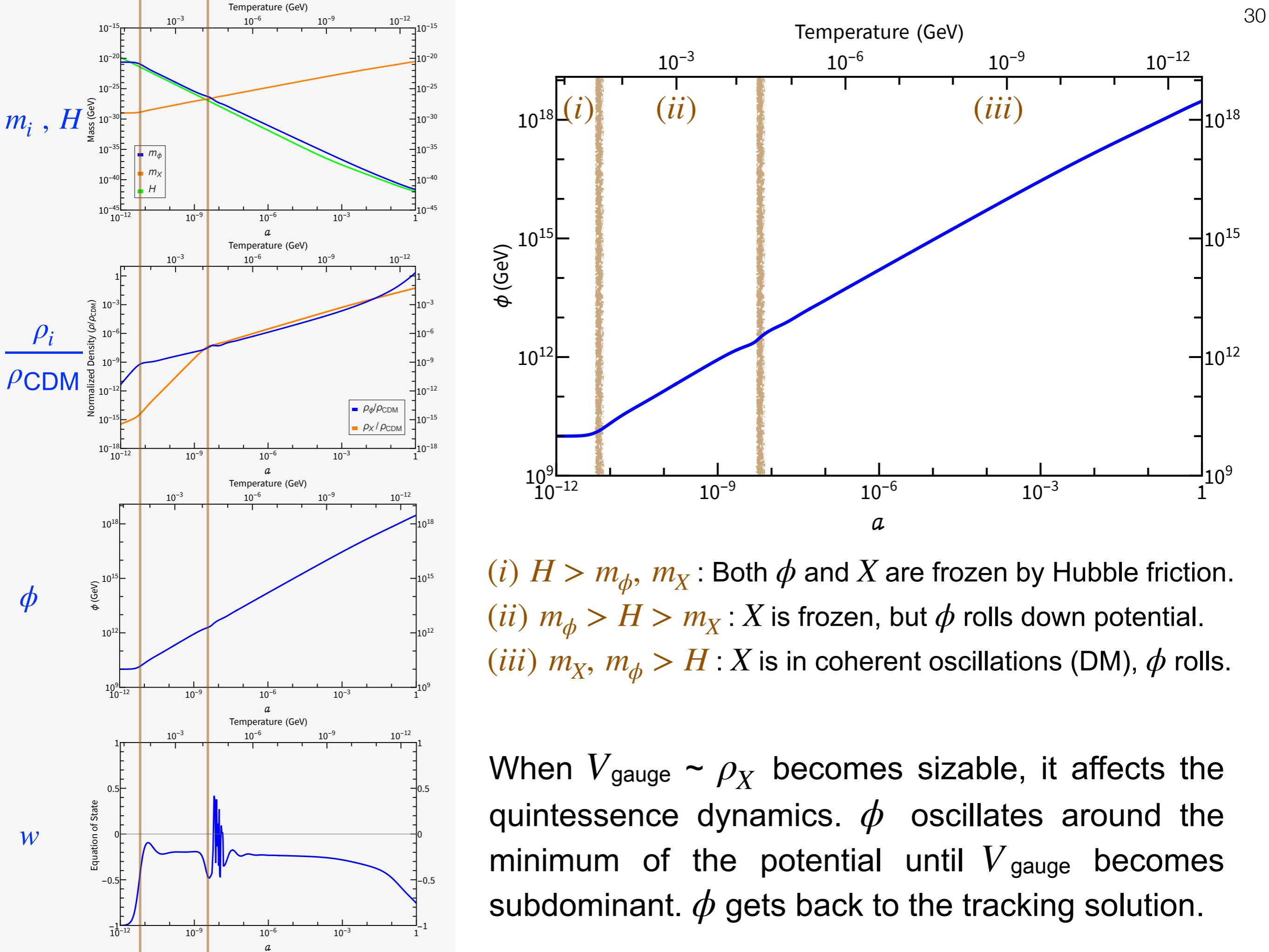


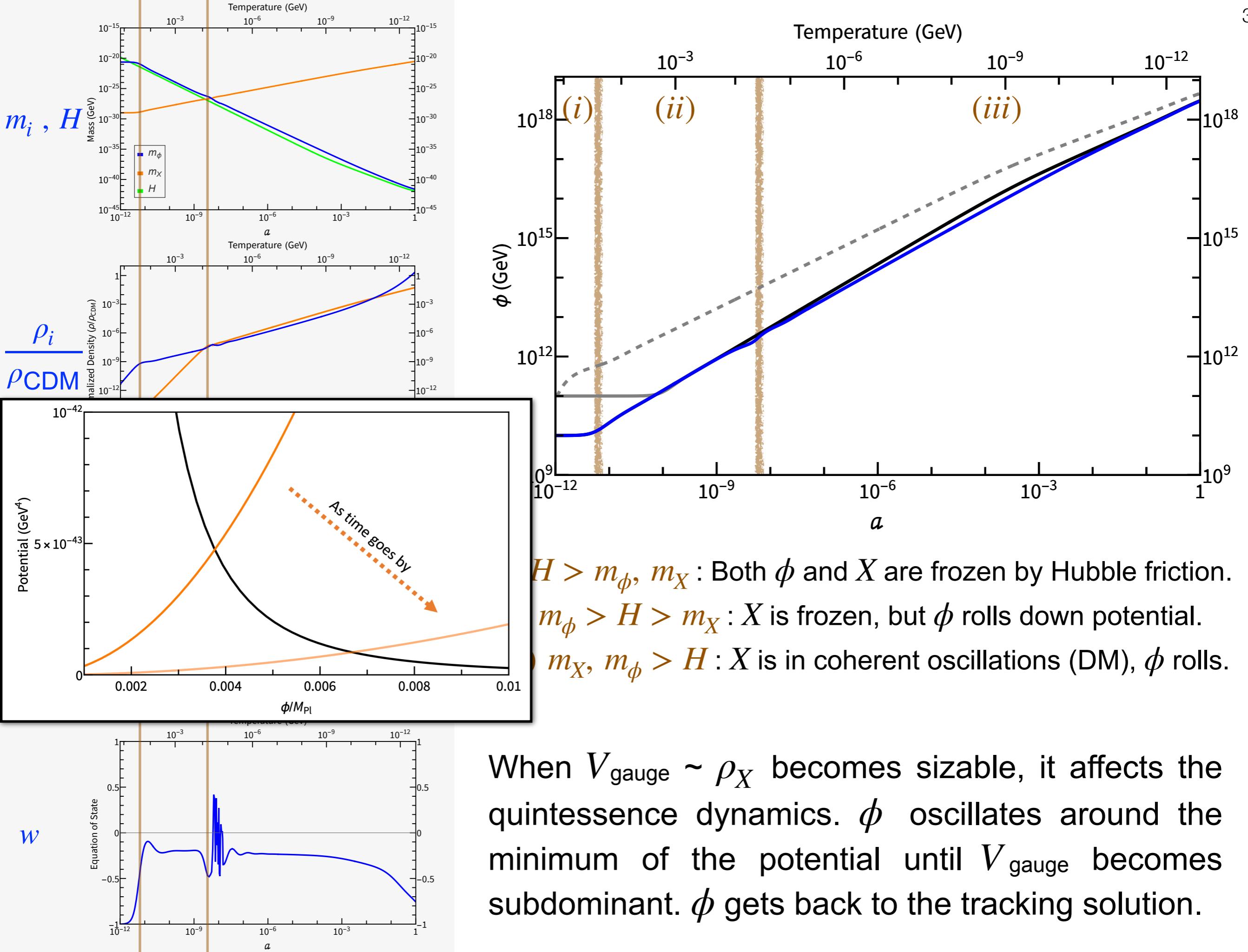
- (i)  $H > m_\phi, m_X$ : Both  $\phi$  and  $X$  are frozen by Hubble friction.
- (ii)  $m_\phi > H > m_X$ :  $X$  is frozen, but  $\phi$  rolls down potential.
- (iii)  $m_X, m_\phi > H$ :  $X$  is in coherent oscillations (DM),  $\phi$  rolls.

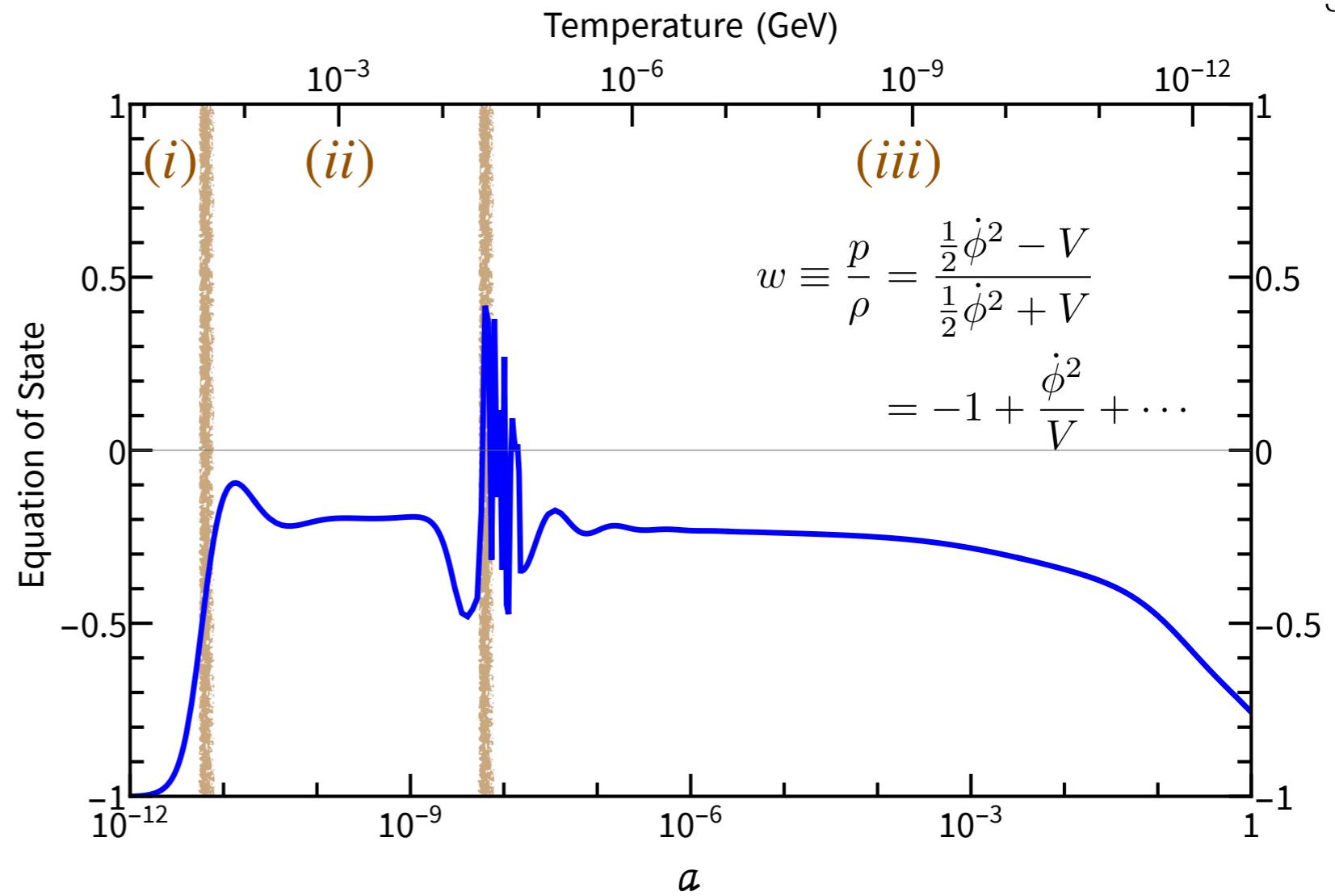
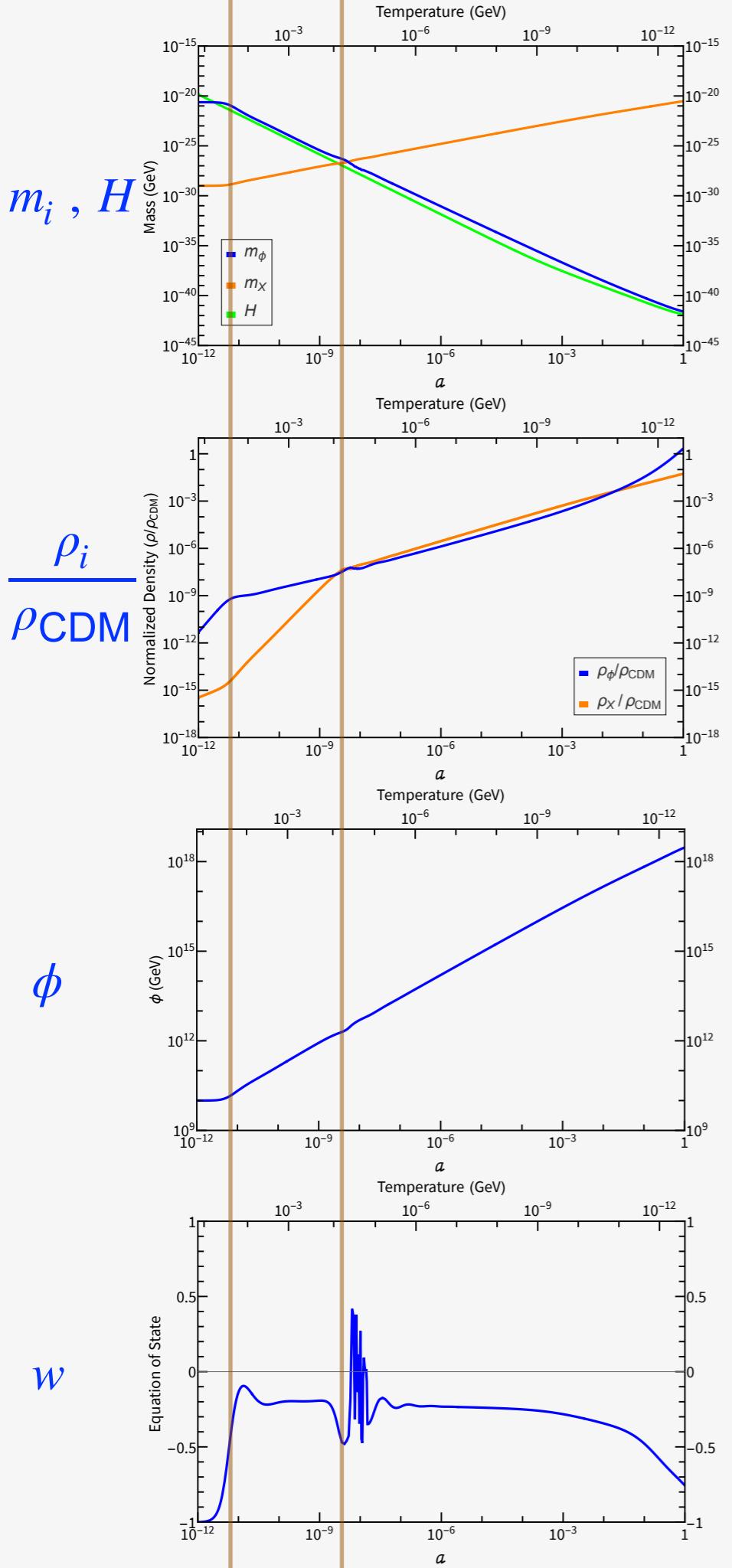


- (i)  $H > m_\phi, m_X$ : Both  $\phi$  and  $X$  are frozen by Hubble friction.  
 (ii)  $m_\phi > H > m_X$ :  $X$  is frozen, but  $\phi$  rolls down potential.  
 (iii)  $m_X, m_\phi > H$ :  $X$  is in coherent oscillations (DM),  $\phi$  rolls.

- (i)  $\rho_X \propto a^{-2}$  : frozen,  
 (ii)  $\rho_X \propto m_X^2 a^{-2}$  : frozen.  $m_X$  changes.  
 (iii)  $\rho_X \propto m_X a^{-3}$  :  $m_X$  changes.







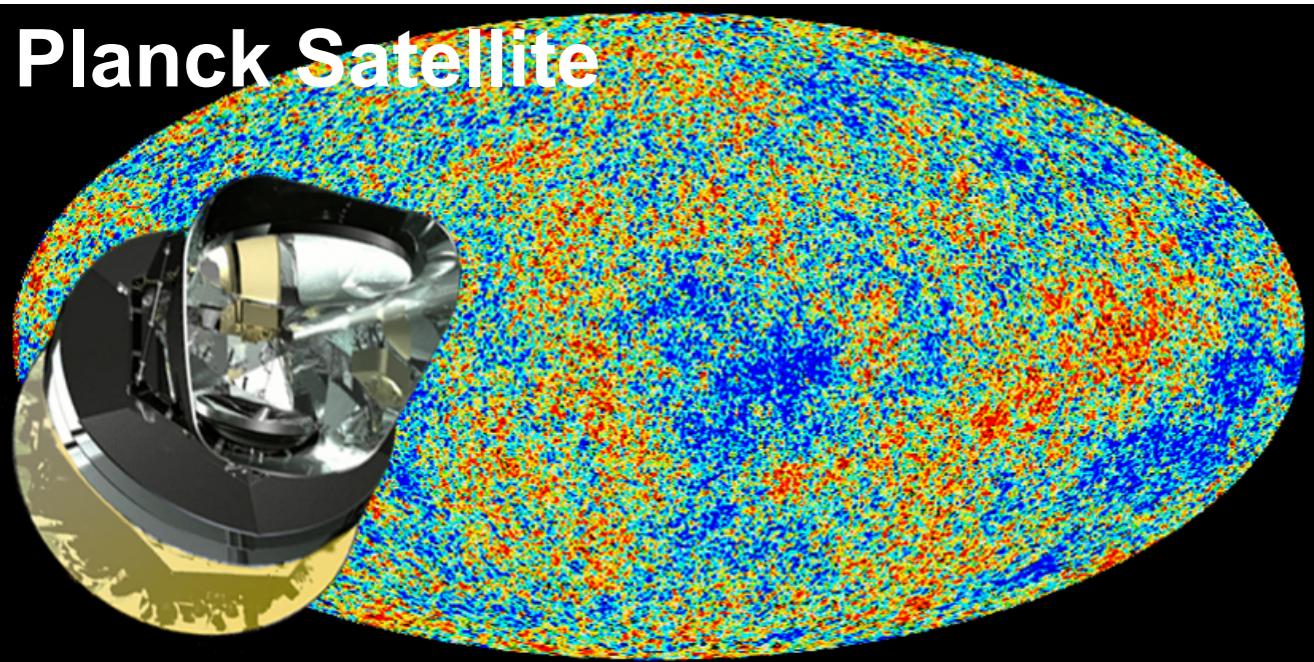
- (i)  $H > m_\phi, m_X$ : Both  $\phi$  and  $X$  are frozen by Hubble friction.
- (ii)  $m_\phi > H > m_X$ :  $X$  is frozen, but  $\phi$  rolls down potential.
- (iii)  $m_X, m_\phi > H$ :  $X$  is in coherent oscillations (DM),  $\phi$  rolls.

The oscillation in the  $\phi$  equation of state reflects the  $\phi$  oscillation around the minimum of the potential. After  $V_{\text{gauge}}$  becomes subdominant, it restores tracking solution.

# Hubble tension

# Modern measurements of the Hubble constant

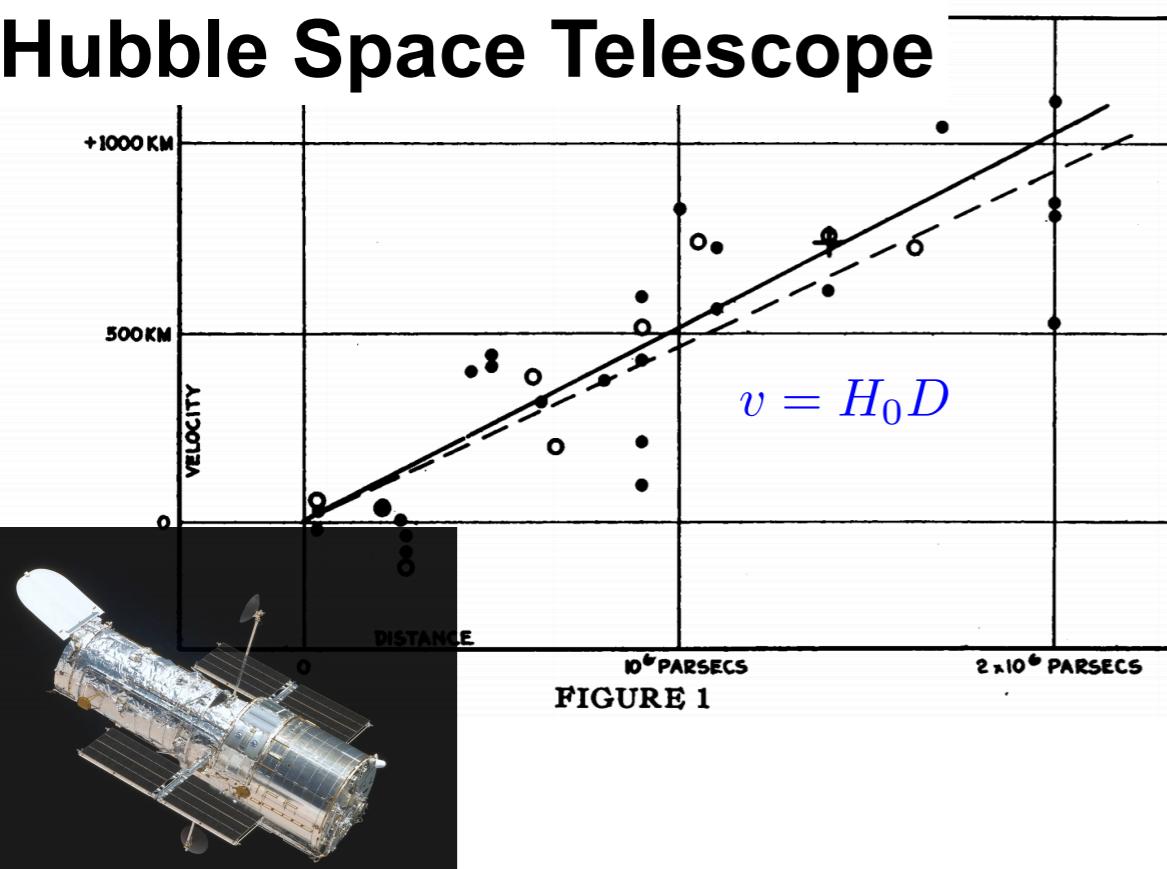
Planck Satellite



(early Universe)

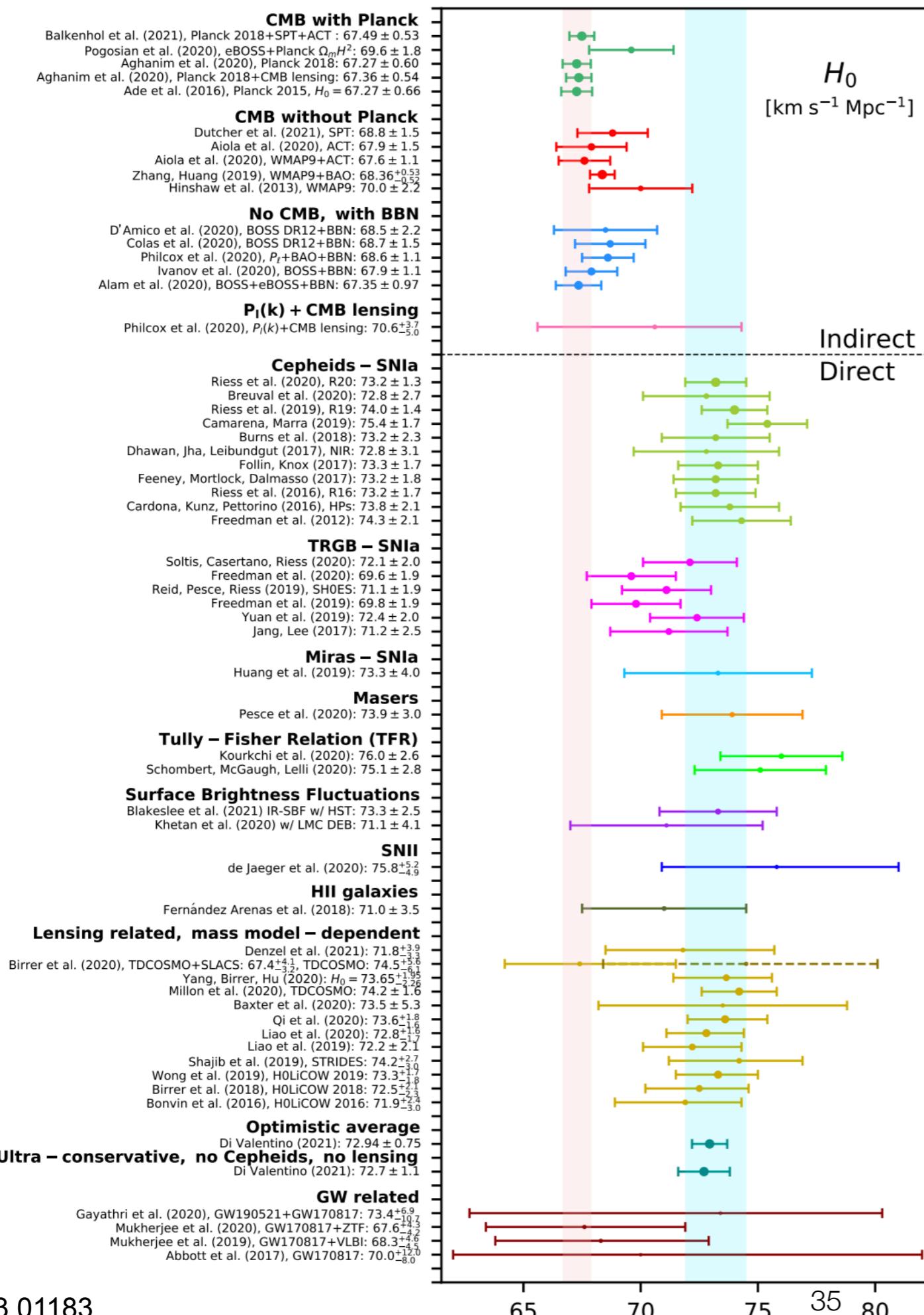
- (i) By fitting CMB data to the  $\Lambda$ -CDM model

Hubble Space Telescope



(late Universe)

- (ii) With the observation of the expansion (standard candles: Cepheid variables + Supernovae)



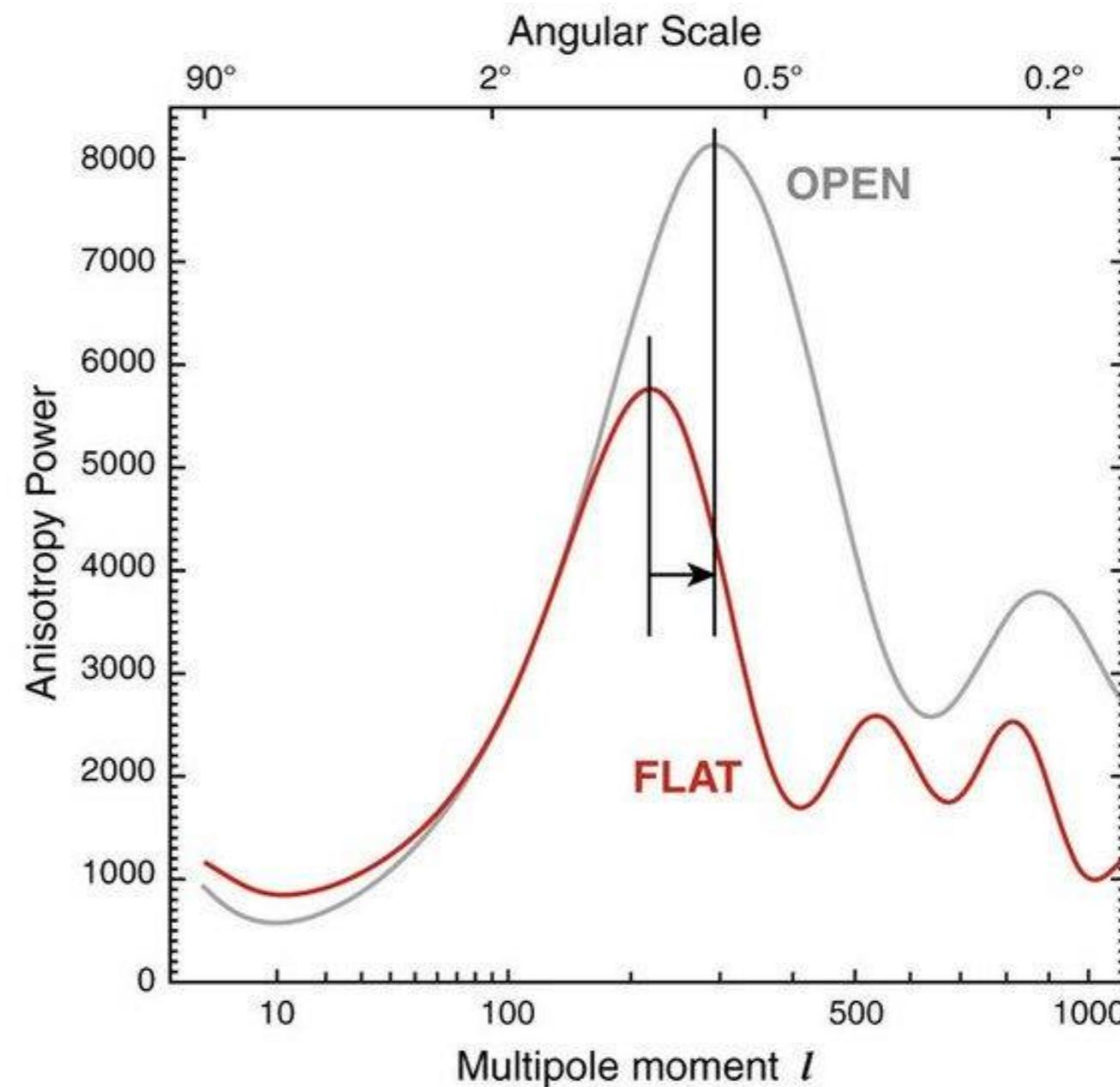
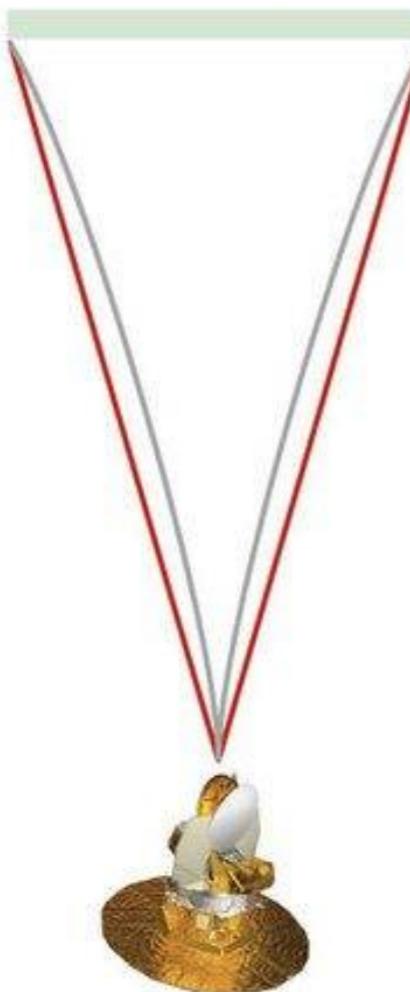
(early Universe).  $H_0 \sim 67$

(late Universe).  $H_0 \sim 73$

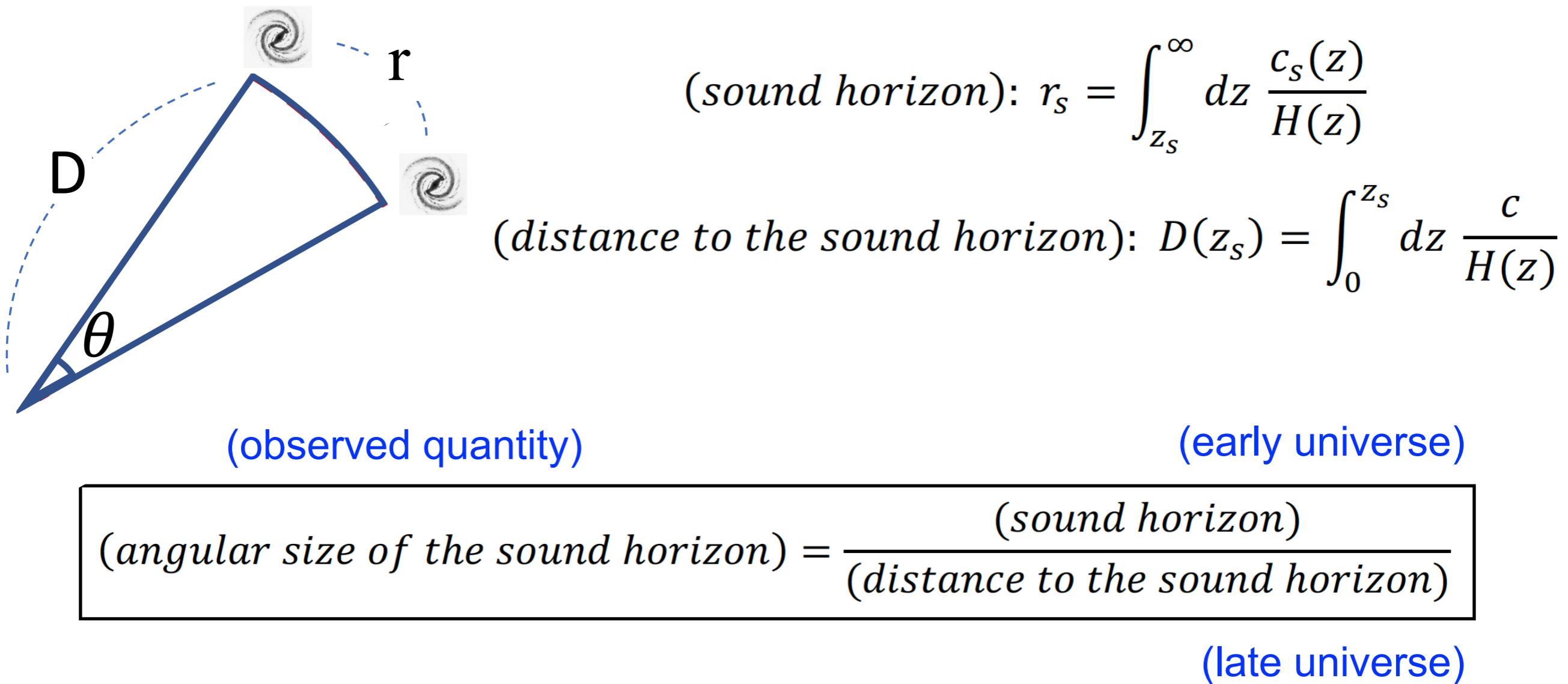
Hubble tension:  
about  $5\sigma$  difference in  $H_0$  between the  
early and late Universe values.  
(Potential hint of the new cosmology.)

# Sound horizon in CMB

Standard Ruler:  
1° arc measurement of  
dominant energy spike



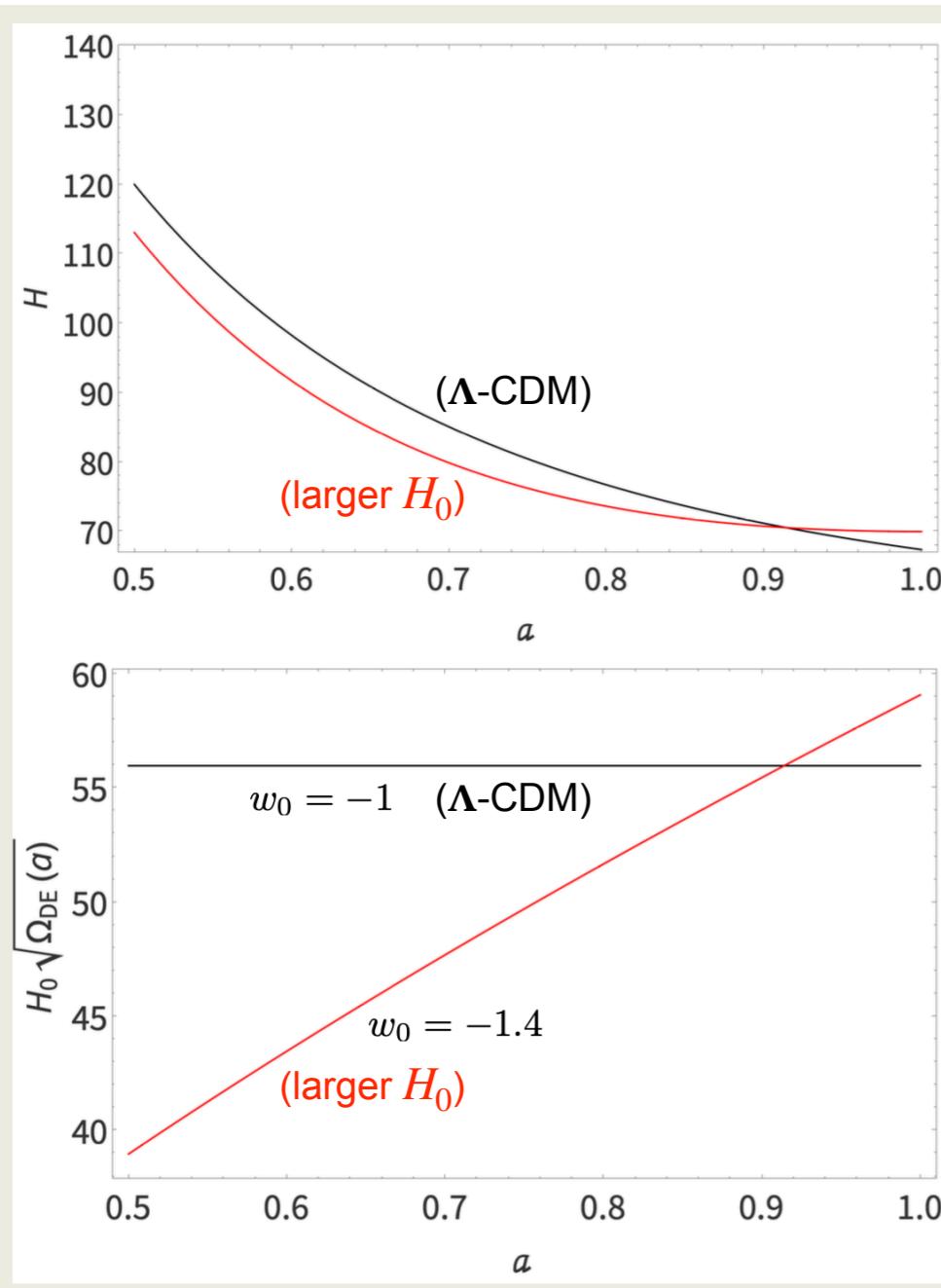
# Baryon Acoustic Oscillations



DE becomes dominant only in the late universe.

Assuming no change in the sound horizon (early universe physics), the comoving distance to the last scattering ( $D$ ) should remain intact with a new DE model.

# Hubble tension



$$D(z_s) = \int_0^{z_s} dz \frac{c}{H(z)}$$

$$H^2 = \left(\frac{\dot{a}}{a}\right)^2 = H_0^2 (\Omega_{\text{DE}} + \Omega_{\text{matter}})$$

$$\rho \propto a^{-3(1+w)}$$

To keep  $D$  unchanged, a larger  $H_0$  (resolving Hubble tension) should be compensated by a smaller  $H$  in the recent past  
: It demands  $w(\text{DE}) < -1$  ( $\Lambda\text{-CDM}$  value).

In the uncoupled quintessence model,  
 $w(\text{DE}) > -1$  (worsening Hubble tension).

If an interacting DE model can provide effective  $w < -1$ , it may alleviate Hubble tension.

$$\text{(quintessence)} \quad w \equiv \frac{p}{\rho} = \frac{\frac{1}{2}\dot{\phi}^2 - V}{\frac{1}{2}\dot{\phi}^2 + V} = -1 + \frac{\dot{\phi}^2}{V} + \dots$$

[Valentino, Melchiorri, Mina (2017)]  
[Lee, Lee, Colgain, Sheikh-Jabbari, Thakur (2022)]

# Effective DE density

$$w_{\text{eff}}(\widetilde{DE}) = -1 + \frac{1}{\rho_{\widetilde{DE}}} \left( (1+w_0)\rho_\phi + \left( \frac{m_X}{m_X^0} - 1 \right) \frac{\rho_X^0}{a^3} \right)$$

$\dot{\rho} + 3H(1+w)\rho = 0$

: effective  $w$  for the effective DE density in the gauged quintessence

Developed in the DE-DM interaction model. [Das, Corasaniti, Khouri (2006)]

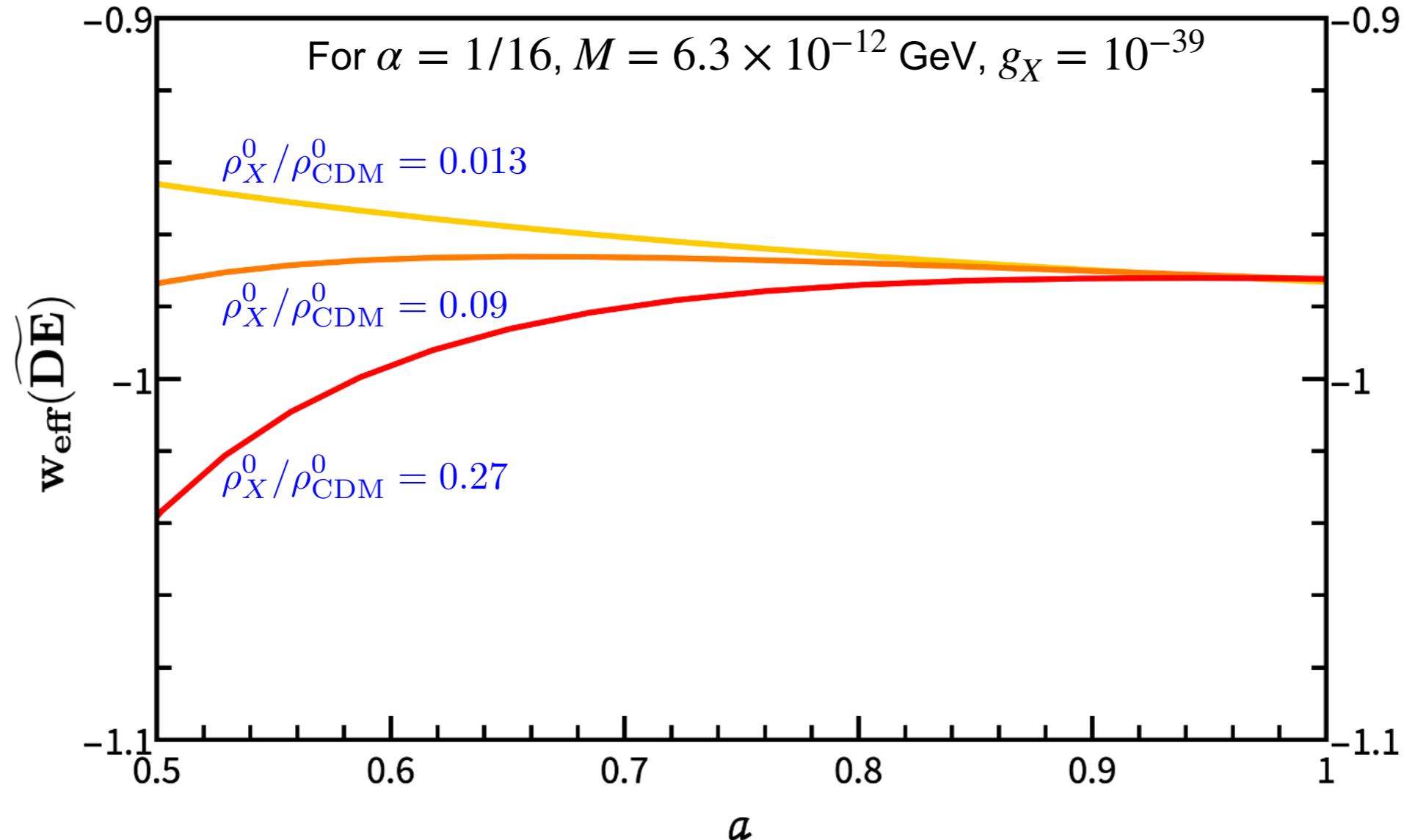
Take the effective DM density ( $\widetilde{\rho_{CDM}}$ ) for the constant mass with  $a^{-3}$  scaling part.

The remaining mass-varying part is absorbed in the effective DE density ( $\widetilde{\rho_{DE}}$ ).

$$\begin{aligned} \rho_{\text{CDM}} + \rho_X + \rho_\phi &= \rho_{\text{CDM}}^0 a^{-3} + \frac{m_X}{m_X^0} \rho_X^0 a^{-3} + \rho_\phi & \frac{a^3 \rho_X}{m_X} = \frac{\rho_X^0}{m_X^0} \\ &= \left[ (\rho_{\text{CDM}}^0 + \rho_X^0) a^{-3} \right] + \left[ \left( \frac{m_X}{m_X^0} - 1 \right) \rho_X^0 a^{-3} + \rho_\phi \right] \\ &= \widetilde{\rho_{CDM}} + \widetilde{\rho_{DE}} & \color{blue}{\rho_{\widetilde{DE}}} \end{aligned}$$

# Effective DE density

$$w_{\text{eff}}(\widetilde{DE}) = -1 + \frac{1}{\rho_{\widetilde{DE}}} \left( (1+w_0)\rho_\phi + \left( \frac{m_X}{m_X^0} - 1 \right) \frac{\rho_X^0}{a^3} \right)$$



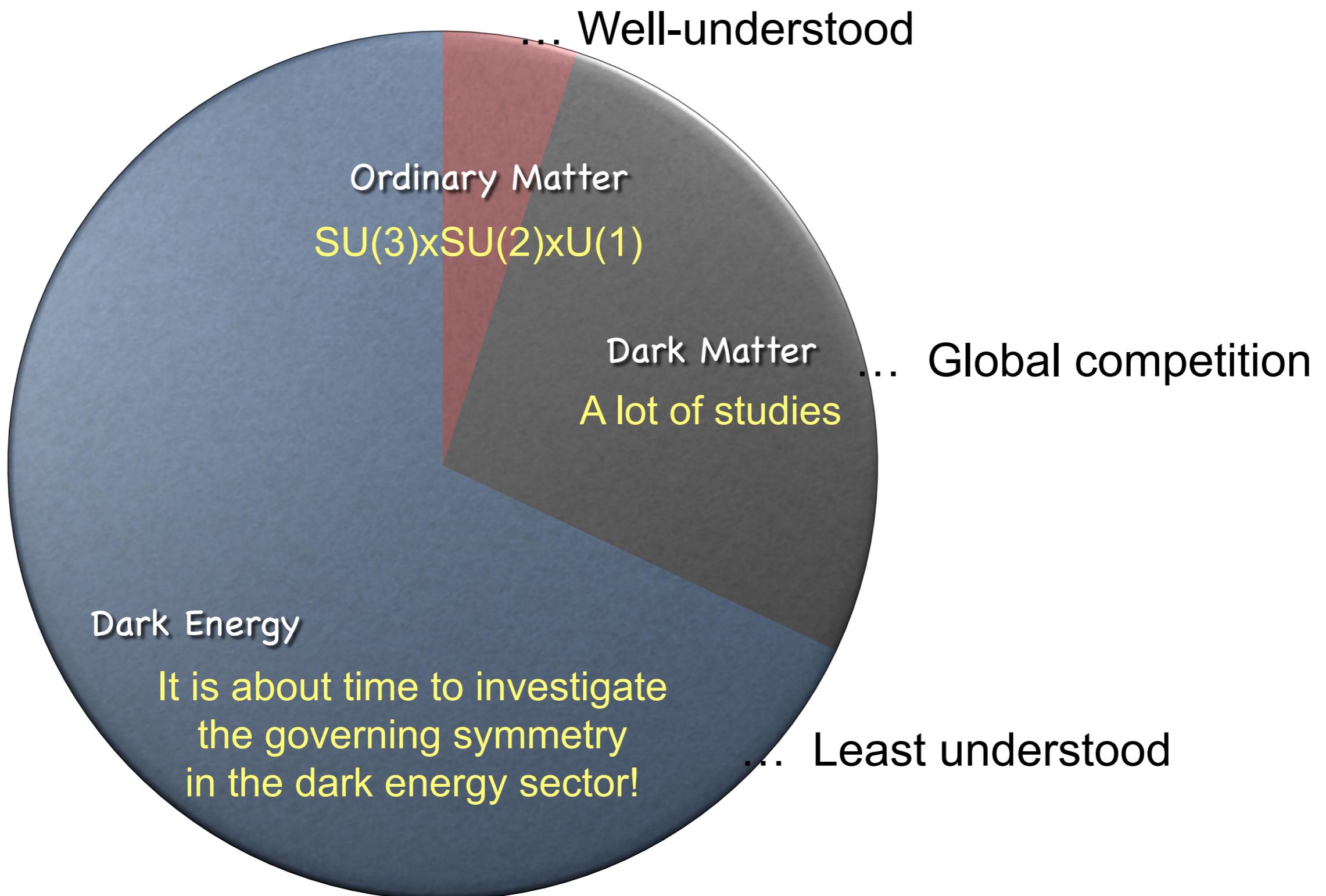
For  $\dot{m}_X > 0$ ,  $w_{\text{eff}}(\widetilde{DE})$  is lower than the uncoupled quintessence.  
It can be even lower than the  $\Lambda$ -CDM ( $w=-1$ ).

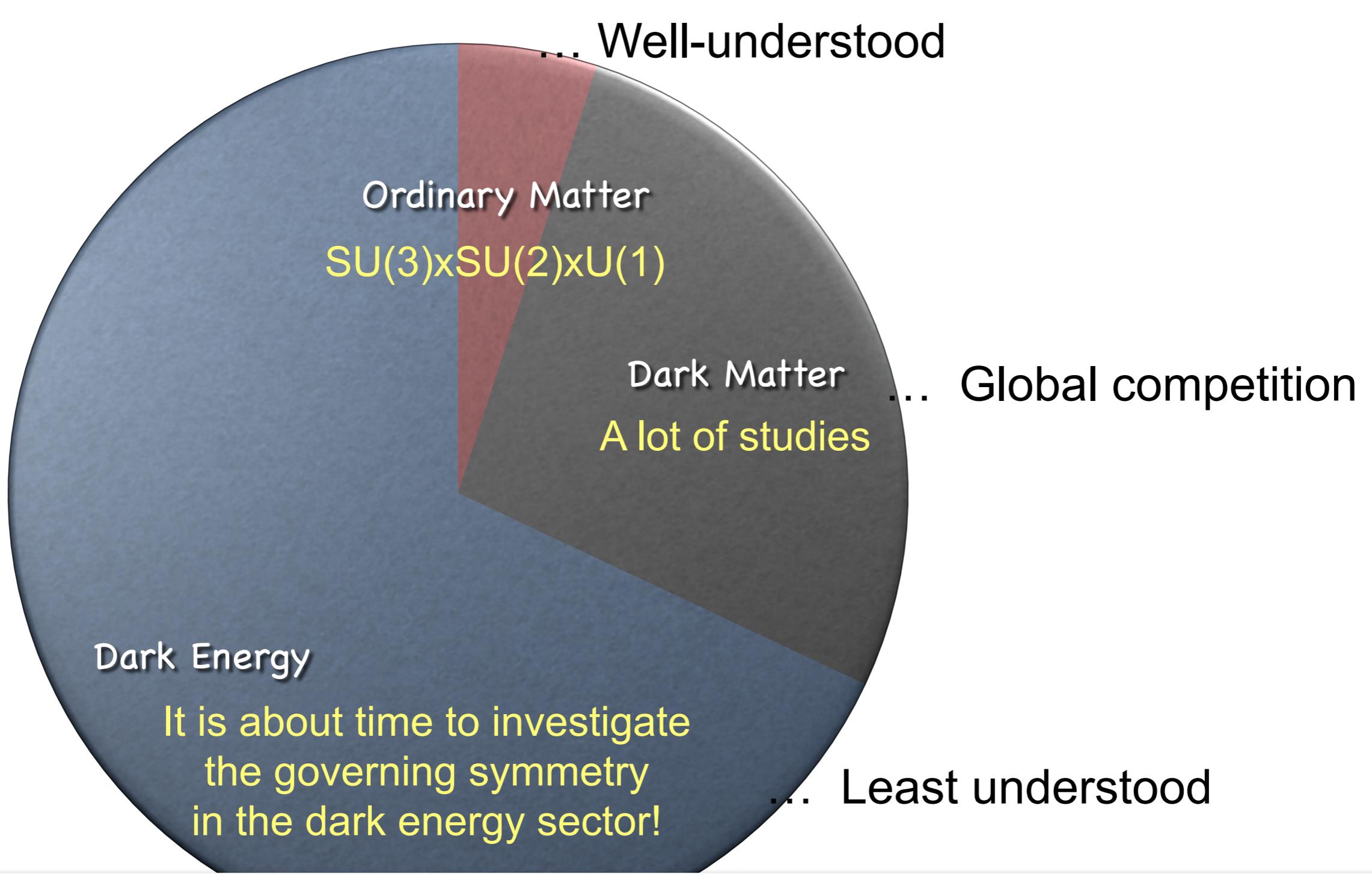
Possibility of alleviating the Hubble tension. (It requires numerical fitting study.)

# Concluding remarks

# Summary

1. We introduced the first gauge symmetry model for a popular quintessence dark energy scalar field.
3. The interaction between the quintessence and the gauge boson ( $V_{\text{gauge}} = \frac{1}{2}g_X^2\phi^2X_\mu X^\mu$ ) brings many interesting features to the universe evolution.
4. The mass-varying effect of the  $X$  gauge boson may overcome the problem of the vector boson misalignment mechanism (scaling factor suppression). [Preliminary result]
6. Hubble tension may be alleviated. (Need quantitative study.)
8. Our study serves as a proof of concept that the dark energy sector can be studied using a gauge symmetry. (Gauge interaction with the dark energy!)





The universe is an enormous direct product of representations of symmetry groups.

- Steven Weinberg -

Thank you