Kazuki Enomoto (KAIST)



Based on

 Hooman Davoudiasl¹, <u>KE²</u>, Hye-Sung Lee², Jiheon Lee², William J. Marciano¹, <u>arXiv:2309.04060 [hep-ph]</u>.

1. BNL, 2. KAIST

Extension of gauge symmetries

Problems in the Standard Model (SM)

- **Unexplained phenomena** ν oscillation, dark matter, baryon asymmetry, ...
- Theoretical problems Unification of gauge interactions, gravity, ...
- Experimental anomalies Muon g-2, B anomaly, W boson mass anomaly, ...

We need new physics!

A new U(1) gauge symmetry

$$SU(3)_C \times SU(2)_L \times U(1)_Y \times U(1)_Y \times U(1)$$
 New force!!
New gauge boson Z'



f carries U(1) charge e.g.) $U(1)_{B-L}$ extension



f does **NOT** carry U(1) charge e.g.) dark photon model

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Extension of gauge symmetries

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A new U(1) gauge symmetry $SU(3)_C \times SU(2)_L \times U(1)_Y \times U(1)$ New force!! New gauge boson Z' This talk f carries U(1) charge e.g.) $U(1)_{B-L}$ extension f does NOT carry U(1) charge e.g.) dark photon model

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Dark photon model

Dark gauge symmetry: $U(1)_d$ (The SM fermions don't carry the dark charge Q_d)

$$\mathcal{L} = -\frac{1}{4}\hat{B}_{\mu\nu}\hat{B}^{\mu\nu} + \frac{\varepsilon}{2c_W}\hat{B}_{\mu\nu}\hat{Z}_d^{\mu\nu} - \frac{1}{4}\hat{Z}_{d\mu\nu}\hat{Z}_d^{\mu\nu}$$
$$c_W = \cos\theta_W$$

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Kinetic mixing



The SM fermions interact with \hat{Z}_d via kinetic mixing Holdom, PLB (1986)

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Kinetic mixing



The SM fermions interact with \hat{Z}_d via kinetic mixing Holdom, PLB (1986)

 $U(1)_d$ symmetry breaking: \hat{Z}_d get the mass term by a singlet VEV Mass eigenstates: γ , Z, and Z_d New physical gauge boson

$$\mathcal{L}_d \simeq -e \varepsilon J^{\mu}_{\mathrm{em}} Z_{d\mu} \ _{(m^2_{Z_d} \ll m^2_Z)} \ Z_d$$
 couples J^{μ}_{em} (Dark photon)

Dark gauge symmetry: $U(1)_d$

Davoudiasl, Lee, Marciano, 1203.2947

Nature of gauge symmetry breaking is quite different

Higgs sector:
$$\Phi_1: (\mathbf{1}, \mathbf{2}, \frac{1}{2}, 0) \quad \Phi_2: (\mathbf{1}, \mathbf{2}, \frac{1}{2}, 1) \quad \Phi_d: (\mathbf{1}, \mathbf{1}, 0, 1)$$

 $U(1)_d$ symmetry breaking: \hat{Z}_d get the mass term by the singlet VEV (v_d) and the doublet VEV (v_2)

Mass matrix of neutral gauge bosons

$$\begin{pmatrix} \tilde{m}_Z^2 & -\tilde{m}_Z^2(\varepsilon_Z + \varepsilon t_W) \\ -\tilde{m}_Z^2(\varepsilon_Z + \varepsilon t_W) & \tilde{m}_{Z_d}^2 \end{pmatrix}$$

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 $\begin{pmatrix} \tilde{m}_{Z}^{2} & -\tilde{m}_{Z}^{2}(\varepsilon_{Z} + \varepsilon t_{W}) \\ -\tilde{m}_{Z}^{2}(\varepsilon_{Z} + \varepsilon t_{W}) & \tilde{m}_{Z_{d}}^{2} \end{pmatrix} \begin{array}{l} \text{New source of mixing} \\ \text{Mass mixing} \\ \text{independent of } \varepsilon \end{array} \varepsilon_{Z} = \frac{2g_{d}}{g_{Z}} \frac{v_{2}^{2}}{v^{2}} \end{array}$

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 New source of mixing!
Mass mixing independent of ε $\varepsilon_{Z} = \frac{2g_{d}}{g_{Z}}\frac{v_{Z}^{2}}{v^{2}}$
 $\mathcal{L}_{d} \simeq -\left(e\varepsilon J_{em}^{\mu} + \frac{g}{2c_{W}}\varepsilon_{Z}J_{NC}^{\mu}\right)Z_{d\mu}$ Z_{d} couples to J_{NC}^{μ}
 $(m_{Z_{d}}^{2} \ll m_{Z}^{2})$ Dark Z boson
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$$\mathcal{L}_d \simeq -\left(e\varepsilon J_{\rm em}^{\mu} + \frac{g}{2c_W}\varepsilon_Z J_{\rm NC}^{\mu}\right) Z_{d\mu}$$

 Z_d predicts various distinctive phenomena

- Parity violation @ low energies
- Rare meson decays
- Higgs exotic decays
- Collider signals

In this talk,

The W boson mass anomaly in the dark Z boson

W boson mass (m_W) anomaly

W boson mass measurements $pp(p\bar{p}) \rightarrow W \rightarrow \ell \nu, e^+e^- \rightarrow W^+W^-$ Before Apr. 2022, $m_W^{World-ave.} = 80.377(12)$ $m_W^{SM} = 80.356(06) \text{ PDG (2022)}$ Good agreement CDF, Science (2022)



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W boson mass (m_W) anomaly





 m_W anomaly and new physics

New physics effect: S, T, U parameters <u>Peskin, Takeuchi, PRL (1990)</u>

$$\Delta m_W^2 \equiv m_W^2 - (m_W^{\text{SM}})^2 = m_Z^2 c_W^2 \left(-\frac{\alpha S}{2(c_W^2 - s_W^2)} + \frac{\alpha T}{1 - t_W^2} + \frac{\alpha U}{4s_W^2} \right)$$

$$\Delta m_W^2 = (m_W^{\text{CDF-II}})^2 - (m_W^{\text{SM}})^2 \simeq 12.5 \text{GeV}^2$$

$$\longrightarrow -0.93S + 1.4T + 1.1U \simeq 0.25$$

New physics effect: *S*, *T*, *U* parameters Peskin, Takeuchi, PRL (1990)

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EW global fit (w/ the CDF-II result) Lu et al, 2204.03796

S = 0.06(10) T = 0.11(12) U = 0.14(09)

The dark photon model CANNOT explain the anomaly under this constraint. <u>Cheng et al, 2204.10156</u> <u>Thomas, Wang, 2205.01911</u> <u>Asagi et al, 2204.05283</u>

In the dark Z model, couplings & mass of Z boson deviates from the SM ones because of kinetic & mass mixing

$$\mathcal{L}_{\text{gauge}} = \frac{1}{2} \tilde{m}_Z^2 (1 + \Delta_1) Z^{\mu} Z_{\mu} - \frac{g}{2c_W} (1 + \Delta_2) J_{\text{NC}}^{\mu} Z_{\mu} - e \Delta_3 J_{\text{EM}}^{\mu} Z_{\mu} + \cdots$$

 $\tilde{m}_Z^2 = g^2 v^2 / (4c_W^2)$

Other terms are the same in the SM

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New physics effect in 4 fermion processes



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$$\tilde{n}_Z^2 = g^2 v^2 / (4c_W^2)$$

Other terms are the same in the SM

New physics effect in 4 fermion processes



The effect of the deviations can be described by S, T, and U parameters

$$\alpha S = -4s_W c_W \left(\frac{\varepsilon_Z + \varepsilon t_W}{1 - r^2}\right) \left(s_W c_W \frac{\varepsilon_Z + \varepsilon t_W}{1 - r^2} - \varepsilon\right) \qquad r = m_{Z_d} / m_Z$$

$$\alpha T = -\left(\frac{\varepsilon_Z + \varepsilon t_W}{1 - r^2}\right) \left(\frac{(2 - r^2)\varepsilon_Z + r^2\varepsilon t_W}{1 - r^2}\right) \qquad EW \text{ global fit}$$

$$\alpha U = 4s_W^2 c_W^2 \left(\frac{\varepsilon_Z + \varepsilon t_W}{1 - r^2}\right) \qquad U = 0.11(12)$$

$$U = 0.14(09)$$

$$Lu \text{ et al, } 2204.03796$$

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$$\alpha U = 4s_W^2 c_W^2 \left(\frac{\varepsilon_Z + \varepsilon t_W}{1 - r^2}\right) \qquad W = 0.14(09)$$

Deviation in m_W^2

$$\Delta m_W^2 = -m_Z^2 \left(\frac{c_W^2}{c_W^2 - s_W^2}\right) \left(\frac{1}{1 - r^2}\right) \left(\varepsilon_Z + \varepsilon t_W\right)^2$$

 $m_{Z_d} < m_Z (r < 1) \longrightarrow \Delta m_W^2 < 0$ $m_{Z_d} > m_Z (r > 1) \longrightarrow \Delta m_W^2 > 0$

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The effect of the deviations can be described by S, T, and U parameters

$$\alpha S = -4s_W c_W \left(\frac{\varepsilon_Z + \varepsilon t_W}{1 - r^2}\right) \left(s_W c_W \frac{\varepsilon_Z + \varepsilon t_W}{1 - r^2} - \varepsilon\right) \qquad r = m_{Z_d} / m_Z$$

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Deviation in
$$m_W^2$$

$$\Delta m_W^2 = -m_Z^2 \left(\frac{c_W^2}{c_W^2 - s_W^2}\right) \left(\frac{1}{1 - r^2}\right) \left(\varepsilon_Z + \varepsilon t_W\right)^2$$

$$m_{Z_d} < m_Z (r < 1) \longrightarrow \Delta m_W^2 < 0$$
Favored by the CDF-II result
$$m_{Z_d} > m_Z (r > 1) \longrightarrow \Delta m_W^2 > 0$$

$$\Delta m_W^2 \simeq 12.5 \text{GeV}^2$$

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S, T, U parameters in the dark photon limit

2

In the dark photon (DP) limit ($\varepsilon_Z = 0$),

$$\alpha S_{\rm DP} = 4s_W^2 (c_W^2 - r^2) \left(\frac{\varepsilon}{1 - r^2}\right)^2$$
$$\alpha T_{\rm DP} = -t_W^2 r^2 \left(\frac{\varepsilon}{1 - r^2}\right)^2$$
$$\alpha U_{\rm DP} = 4s_W^2 \left(\frac{\varepsilon}{1 - r^2}\right)^2$$

When $r \gg 1$,

$$\begin{split} |S_{\rm DP}|\,, |T_{\rm DP}| \gg |U_{\rm DP}|\,, \\ \text{and} \; S_{\rm DP} = (4/c_W^2) T_{\rm DP} \simeq 3.0 T_{\rm DP} \end{split}$$



S, T, U parameters in the dark photon limit

2

1

0

S_{DP}

 $T_{\rm DP}$

alized S, T, and U

2

Dark photon limit (ε_Z =0)

Normalized by $\alpha^{-1} \varepsilon^2 (1 - r^2)^{-2}$

 $U_{\rm DP}$

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In the dark photon (DP) limit ($\varepsilon_{Z} = 0$),

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$$\alpha U_{\rm DP} = 4s_W^2 \left(\frac{\varepsilon}{1-r^2}\right)$$
When $r \gg 1$,

$$|S_{\rm DP}|, |T_{\rm DP}| \gg |U_{\rm DP}|,$$
and $S_{\rm DP} = (4/c_W^2)T_{\rm DP} \simeq 3.0T_{\rm DP}$

$$\downarrow$$

$$\Delta m_W^2 \simeq -S_{\rm DP} \times (35 {\rm GeV}^2)$$

$$S = 0.06(10)$$

$$\int_{z=1}^{$$

S, T, U parameters in the pure dark Z limit

In the pure dark Z (DZ) limit ($\varepsilon = 0$), $\alpha S_{\text{DZ}} = -4s_W^2 c_W^2 \left(\frac{\varepsilon_Z}{1-r^2}\right)^2$ $\alpha T_{\text{DZ}} = (r^2 - 2) \left(\frac{\varepsilon_Z}{1-r^2}\right)^2$ $\alpha U_{\text{DZ}} = 4s_W^2 c_W^2 \left(\frac{\varepsilon_Z}{1-r^2}\right)^2$

 $S_{DZ} = -U_{DZ}$ for all ε_Z and rWhen $r \gg 1$, $|T_{DZ}| \gg |S_{DZ}| = |U_{DZ}|$



<u>S, T, U parameters in the pure dark Z limit</u>

In the pure dark Z (DZ) limit ($\varepsilon = 0$),

$$\alpha S_{\rm DZ} = -4s_W^2 c_W^2 \left(\frac{\varepsilon_Z}{1-r^2}\right)^2$$
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 $S_{\rm DZ} = -U_{\rm DZ}$ for all $\varepsilon_{\rm Z}$ and r When $r \gg 1$, $|T_{DZ}| \gg |S_{DZ}| = |U_{DZ}|$

 $\Delta m_W^2 \simeq T_{\rm DZ} \times (35 {\rm GeV}^2)$



CDF-II result ($\Delta m_W^2 \simeq 12.5 \text{GeV}^2$) requires $T_{\rm DZ}\simeq 0.18$

Within 2σ region T = 0.11(12)

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 $(\sim 0.6\sigma)$









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Heavy $Z_d (m_{Z_d} = O(100) \text{GeV})$ and relatively large $|\varepsilon_Z| (\gtrsim 0.03)$

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Constraint from direct searches

 $m_{Z_d} = O(100) \text{ GeV}$ $|\varepsilon_Z| = 0.03 - O(0.1)$

Dilepton resonant search @ LHC ATLAS, 1903.06248

 $pp \rightarrow Z_d \rightarrow \ell^+ \ell^-$ (225 GeV $\leq m_{Z_d} \leq 6000$ GeV)





Dijet resonant search is not effective in the relevant mass range <u>CMS, 1911.03947</u>

ATLAS, 1903.06248

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Constraint from direct searches

The constraint depends on $Br[Z_d \rightarrow \ell^+ \ell^-]$

Case 1: Only the SM fermions (Dashed lines) **Case 2**: Including a dark fermion [$m_{\psi} = 50$ GeV, $g_d = 0.1$] (Solid lines)



Colored regions: CDF-II result & EW global fit within 2σ

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Summary

New U(1) gauge symmetry is an attractive candidate for new physics.

- The dark Z model includes mass mixing ε_Z independent of kinetic mixing ε and provides richer phenomenology.
- Heavy dark Z bosons with relatively large ε_Z can reproduce the CDF-II result of m_W and the result of EW global fit.
- Such a parameter region is strongly constrained by dilepton resonant searches unless m_{Z_d} is quite small or large.

Considering dark decay channels, this constraint is relaxed.

Thank you for listening!

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Mass eigenstate of neutral gauge bosons

$$\mathcal{L}_{\rm kin} = -\frac{1}{4} \hat{B}^{\mu\nu} \hat{B}_{\mu\nu} + \frac{\varepsilon}{2\cos\theta_W} \hat{B}^{\mu\nu} \hat{Z}_{d\mu\nu} - \frac{1}{4} \hat{Z}^{\mu\nu}_d \hat{Z}_{d\mu\nu},$$

Digonalize the kinetic term

$$\begin{pmatrix} \tilde{B}_{\mu} \\ \tilde{Z}_{d\mu} \end{pmatrix} = \begin{pmatrix} 1 & -\varepsilon/c_W \\ 0 & \sqrt{1 - \varepsilon^2/c_W^2} \end{pmatrix} \begin{pmatrix} \hat{B}_{\mu} \\ \hat{Z}_{d\mu} \end{pmatrix}$$

Mass matrix for \tilde{B}_{μ} and $\tilde{Z}_{d\mu}$

1

$$\mathcal{L}_{\text{mass}} = m_W^2 W_{\mu}^+ W^{-\mu} + \frac{1}{2} (\tilde{Z}^{\mu}, \tilde{Z}_d^{\mu}) M_V^2 \begin{pmatrix} \tilde{Z}_\mu \\ \tilde{Z}_{d\mu} \end{pmatrix},$$

$$\tilde{Z}_\mu = -\sin \theta_W \tilde{B}_\mu + \cos \theta_W \hat{W}_\mu^3, \quad \tan \theta_W = g'/g$$

$$M_V^2 = \begin{pmatrix} \tilde{m}_Z^2 & -\tilde{m}_Z^2 \eta (\varepsilon_Z + \varepsilon t_W) \\ -\tilde{m}_Z^2 \eta (\varepsilon_Z + \varepsilon t_W) & \tilde{m}_{Z_d}^2 \end{pmatrix} \quad \eta = \frac{1}{\sqrt{1 - \varepsilon^2/c_W^2}}$$

/

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Mass eigenstate of neutral gauge bosons

Mass eigenstates Z_{μ} and $Z_{d\mu}$

$$\begin{pmatrix} Z_{\mu} \\ Z_{d\mu} \end{pmatrix} = \begin{pmatrix} \cos \xi & -\sin \xi \\ \sin \xi & \cos \xi \end{pmatrix} \begin{pmatrix} \tilde{Z}_{\mu} \\ \tilde{Z}_{d\mu} \end{pmatrix}$$

Mixing matrix

Mass eigenvalues

$$\sin \xi \simeq \frac{\varepsilon_Z + \varepsilon t_W}{1 - r^2},$$
$$\cos \xi \simeq 1 - \frac{1}{2} \left(\frac{\varepsilon_Z + \varepsilon t_W}{1 - r^2} \right)^2,$$

$$r = m_{Z_d} / m_Z$$

$$\begin{split} m_Z^2 &\simeq \tilde{m}_Z^2 \left(1 + \frac{(\varepsilon_Z + \varepsilon t_W)^2}{1 - \tilde{r}^2} \right), \\ m_{Z_d}^2 &\simeq \tilde{m}_{Z_d}^2 \left(1 - \frac{\varepsilon_Z^2}{\tilde{r}^2(1 - \tilde{r}^2)} - \frac{\varepsilon^2 t_W^2 + 2\varepsilon_Z \varepsilon t_W}{1 - \tilde{r}^2} \right), \end{split}$$

$$\tilde{r} = \tilde{m}_{Z_d} / \tilde{m}_Z$$

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The covariant derivative in mass eigenstate basis

$$D_{\mu} = \partial_{\mu} + igT^{a}\hat{W}_{\mu} + ig'Y\hat{B}_{\mu} + ig_{d}Q_{d}\hat{Z}_{d\mu} + (\text{QCD term})$$

After diagonalization of kinetic terms and mass terms,

$$D_{\mu} = \dots + \frac{ig}{c_{W}}(c_{\xi} + \eta s_{\xi}\varepsilon t_{W})(T^{3} - s_{W}^{2}Q)Z_{\mu} - ie\eta s_{\xi}\varepsilon QZ_{\mu} - ig_{d}\eta s_{\xi}Q_{d}Z_{\mu}$$
$$+ \frac{ig}{c_{W}}(s_{\xi} - \eta c_{\xi}\varepsilon t_{W})(T^{3} - s_{W}^{2}Q)Z_{d\mu} + ie\eta c_{\xi}\varepsilon Z_{d\mu} + ig_{d}\eta c_{\xi}Q_{d}Z_{d\mu}$$
$$ig_{\omega}\pi^{3} - 2\cos \pi - \cos \left(\frac{\varepsilon_{Z} + \varepsilon t_{W}}{\varepsilon_{Z}}\right)\pi$$

$$\simeq \dots + \frac{\iota g}{c_W} (T^3 - s_W^2 Q) Z_\mu - i g_d Q_d \left(\frac{c_Z + c \iota_W}{1 - r^2}\right) Z_\mu$$

$$+\frac{ig}{c_W(1-r^2)}(r^2\varepsilon t_W + \varepsilon_Z)Z_{d\mu} + ie\varepsilon QZ_{d\mu} + ig_d Q_d Z_{d\mu}$$
$$\to 0 \quad (m_{Z_d}/m_Z \to 0)$$

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$$\Delta \mathcal{L}_{\text{gauge}} = \frac{1}{2} \tilde{m}_Z^2 \Delta_1 Z^\mu Z_\mu - \frac{g}{2c_W} \Delta_2 J_{\text{NC}}^\mu Z_\mu - e \Delta_3 J_{\text{EM}}^\mu Z_\mu$$
$$\tilde{m}_Z^2 = g^2 v^2 / (4c_W^2)$$

In the pure dark Z limit ($\varepsilon = 0$), $\Delta_3 = -\eta \varepsilon \sin \xi = 0 \qquad \eta = 1/\sqrt{1 - \varepsilon^2/c_W^2}$

 $\alpha S = 8s_W^2 c_W^2 \Delta_2 - 4s_W c_W (c_W^2 - s_W^2) \Delta_3 = 8s_W^2 c_W^2 \Delta_2$ $\alpha U = -8s_W^2 c_W (c_W \Delta_2 + s_W \Delta_3) = -8s_W^2 c_W^2 \Delta_2$ $\blacktriangleright S = -U$

Backup

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 S_{DZ} , T_{DZ} , U_{DZ} parameters in the decoupling limit

In the decoupling limit of $Z_d (r \to \infty)$, the generated dimension-six operator is only

 $O_{\varphi}^{\prime(6)} = O_{2}^{\mu}O_{2\mu} \qquad O_{2}^{\mu} = \Phi_{2}^{\dagger}D^{\mu}\Phi_{2} - (D^{\mu}\Phi_{2})^{\dagger}\Phi_{2}$ This induces the deviation of $\mathcal{O}(m_{Z_{d}}^{-2})$ $\Delta_{1} = \varepsilon_{Z}^{2}r^{-2}, \quad \Delta_{2} = 0, \quad \Delta_{3} = 0.$ $\blacktriangleright \alpha S = 8s_{W}^{2}c_{W}^{2}\Delta_{2} - 4s_{W}c_{W}(c_{W}^{2} - s_{W}^{2})\Delta_{3} = 0$ *S* is not generated by the *d* = 6 oeprator.

 S_{DZ} and U_{DZ} is generated by $\mathscr{O}_{\varphi}^{\prime(8)} = \frac{1}{2} O_{2\mu\nu} O_{2}^{\mu\nu}$ $d = 8 \text{ operator} \quad (O_{2}^{\mu\nu} = \partial^{\mu}O_{2}^{\nu} - \partial^{\nu}O_{2}^{\mu})$

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