

1
Introduction



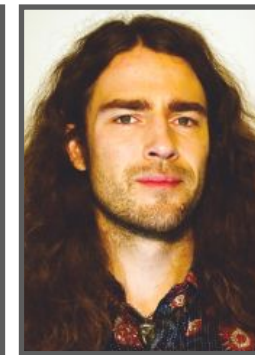
T. Konstandin



H. Rubira



B. Shakya



I. Stomberg



J.v.d.Vis

2
GWs from
sound waves
in FOPT

Gravitational waves from feebly-interacting particles in a first-order phase transition

Ryusuke Jinno (RESCEU, UTokyo)

Jeju workshop, 2023/11/16

3
GWs from
FIPs
in FOPT

4
Summary



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Introduction



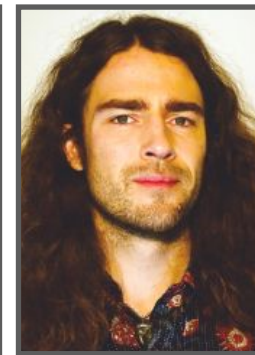
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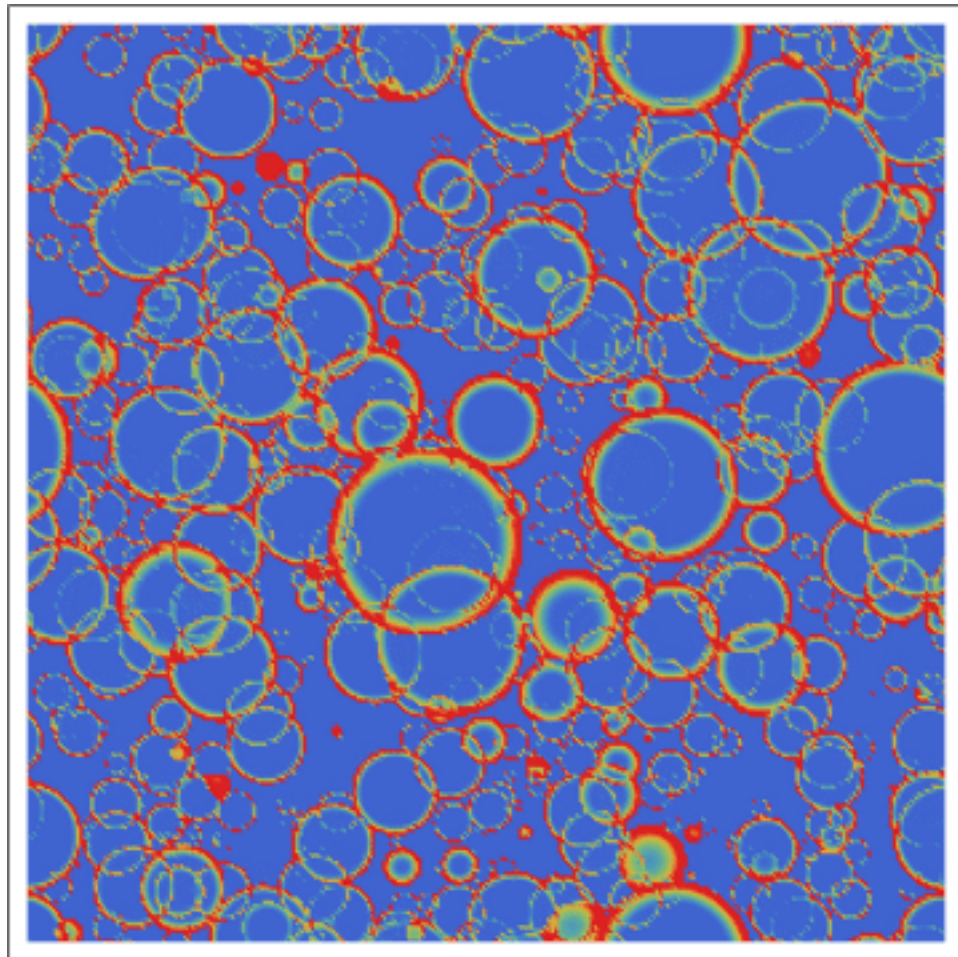
TAKE-HOME MESSAGE

- Feebly-interacting particles are a good target for new physics searches
 - sterile neutrinos - dark photon - axion-like particles - dilaton ...
- If they are produced during a first-order phase transition,
they leave a characteristic imprint on the GW spectrum

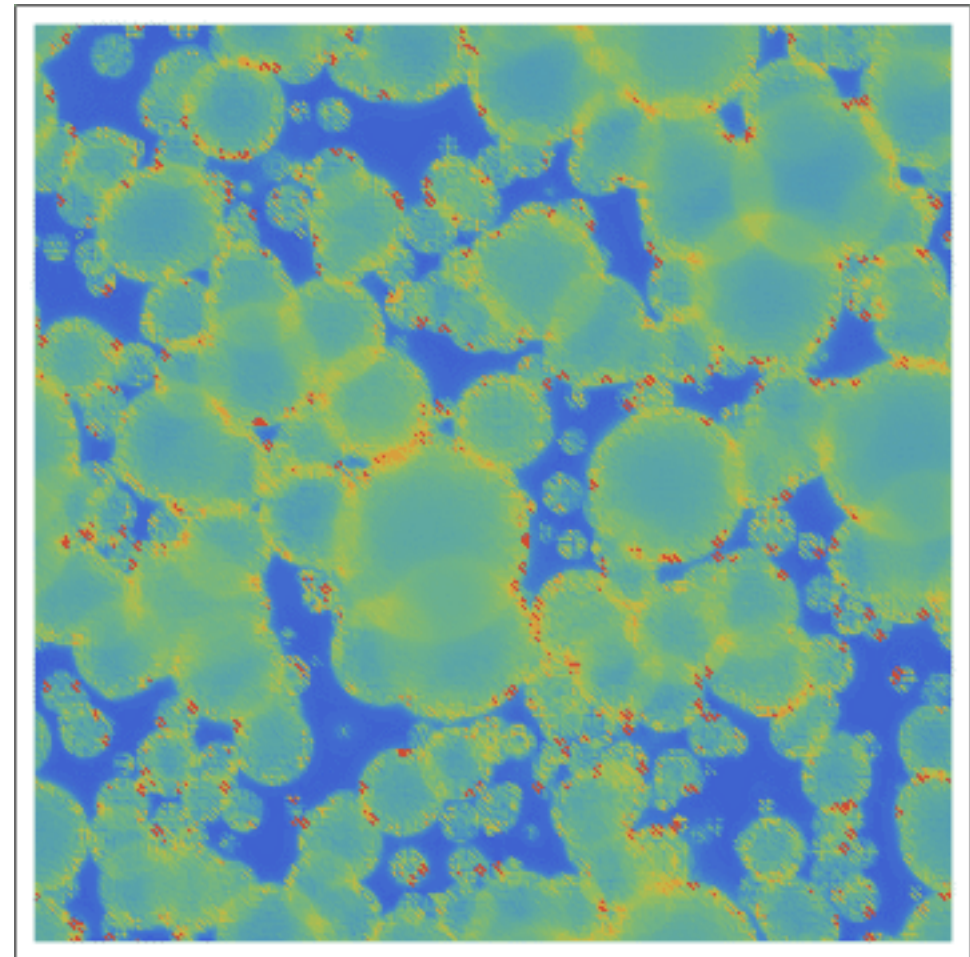
TAKE-HOME MESSAGE

- Fluid vs. Feebly-interacting particles in a first-order phase transition

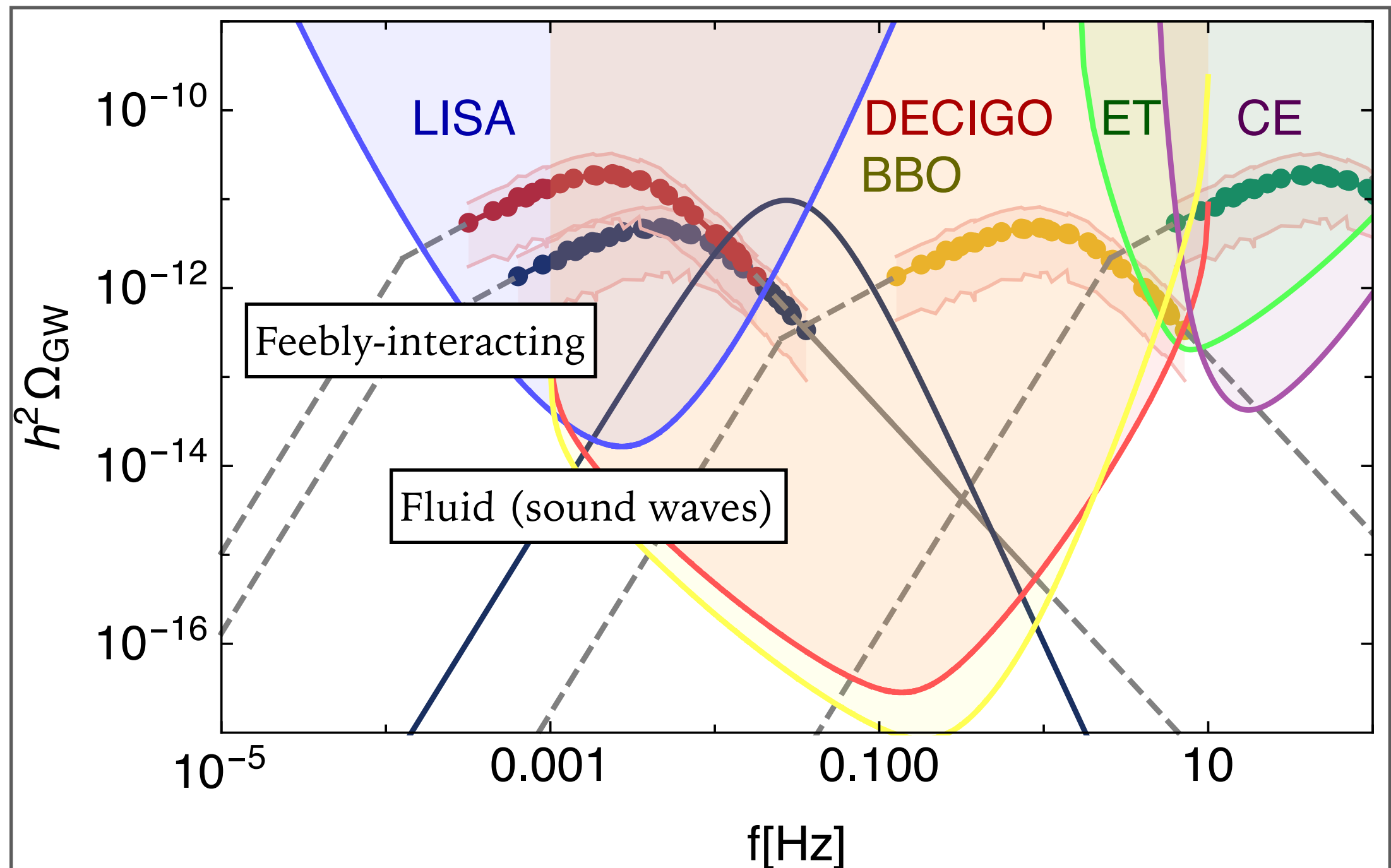
Fluid



Feebly-interacting



TAKE-HOME MESSAGE





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OVERVIEW OF FIRST-ORDER PHASE TRANSITION & BUBBLE DYNAMICS

[Hogan '83] [Witten '84]

microphysics

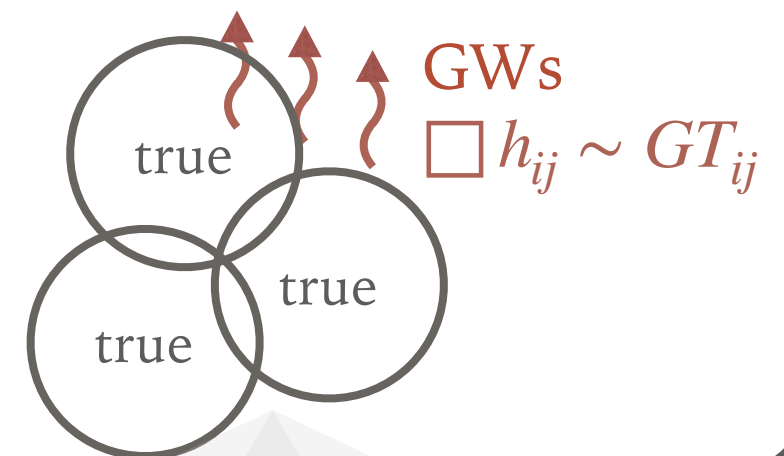
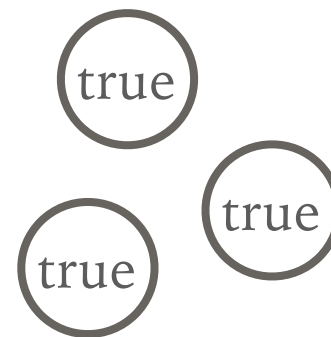
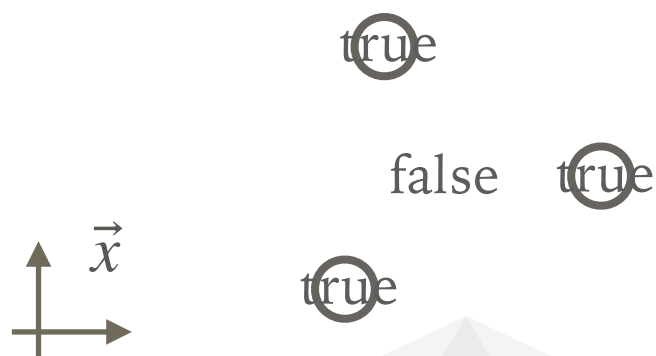
macrophysics

time or scale →

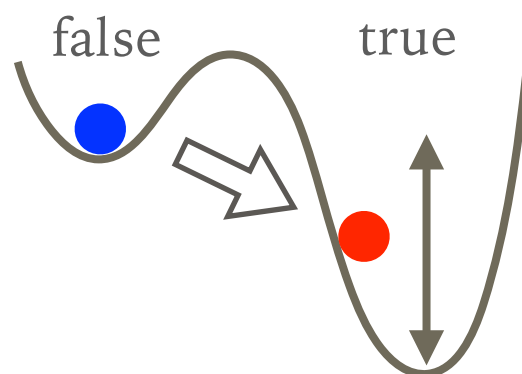
(1) nucleation (核生成)

(2) expansion (拡大)

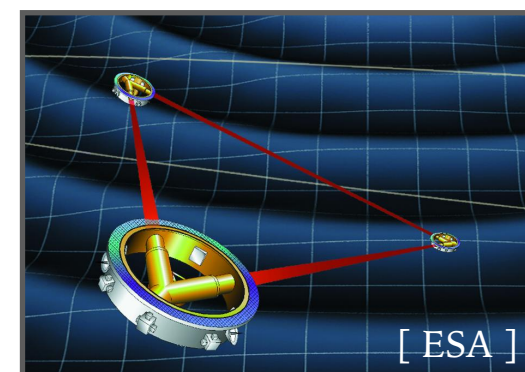
(3) collision (衝突)



Physics of the Higgs sector



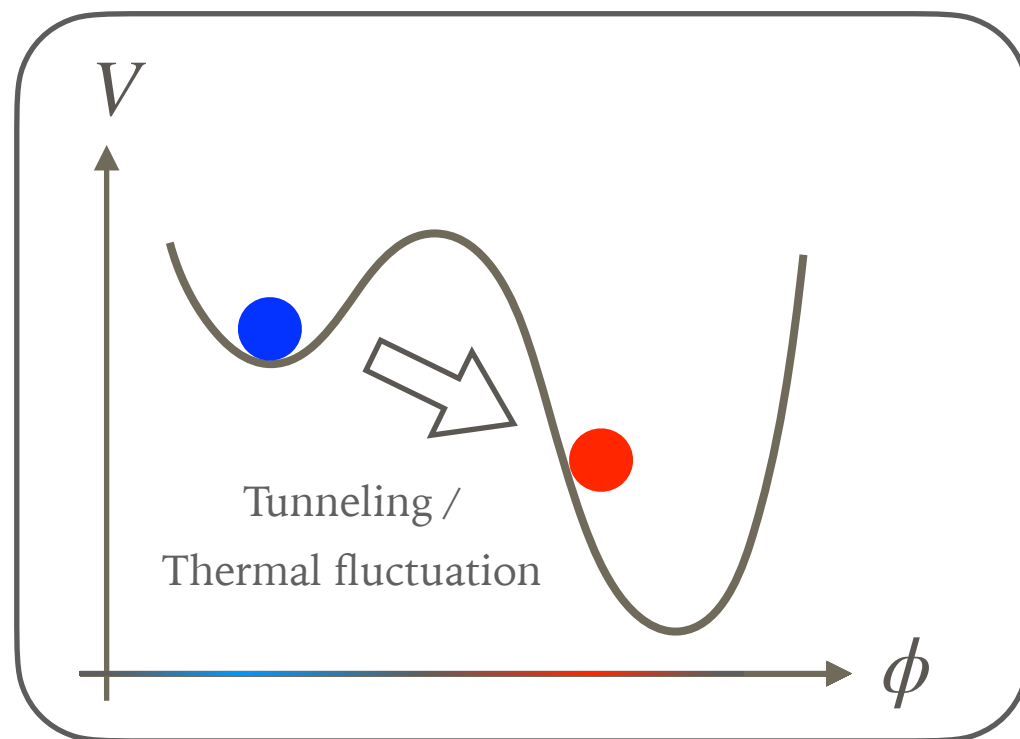
GW observations



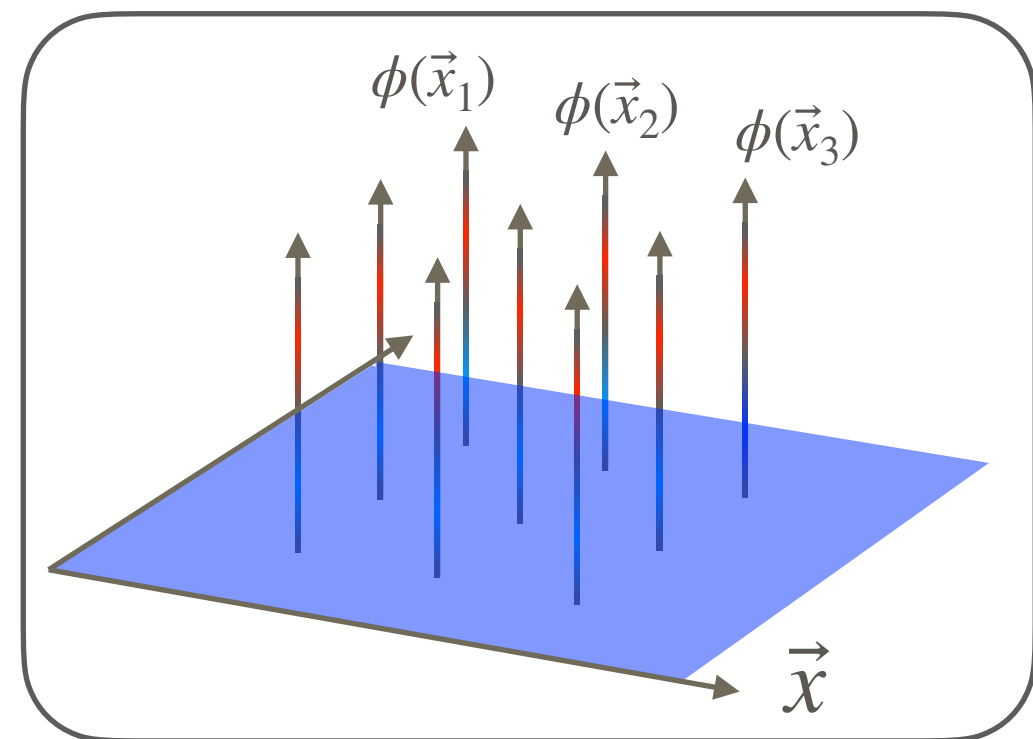
STEP 1 : NUCLEATION

.....

Field space



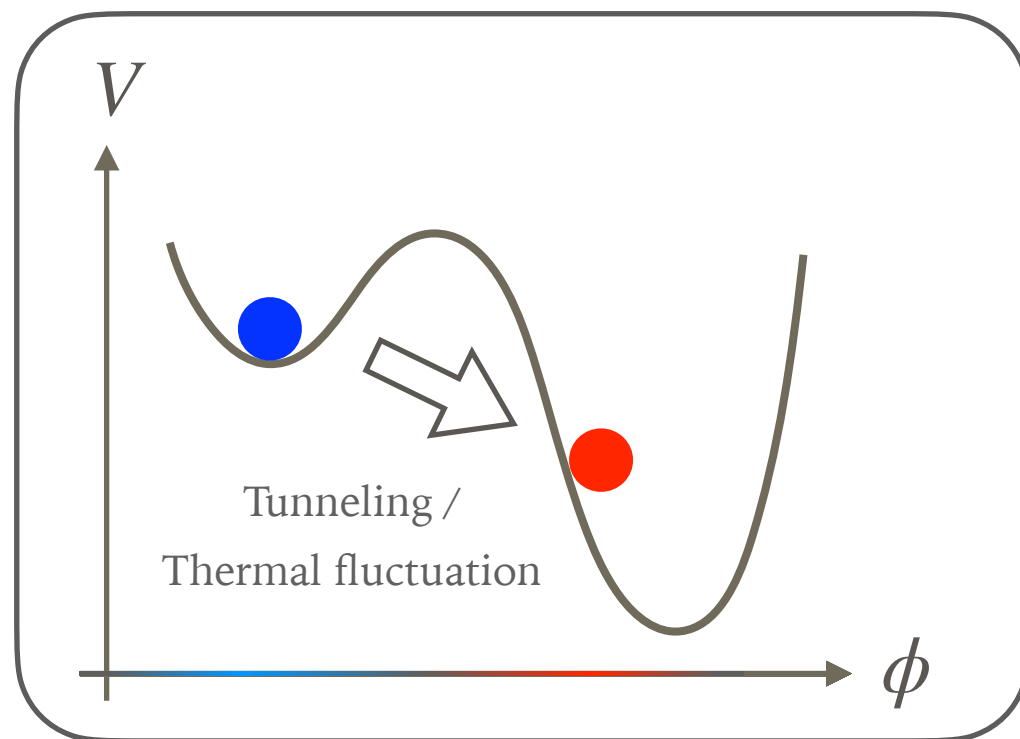
Position space



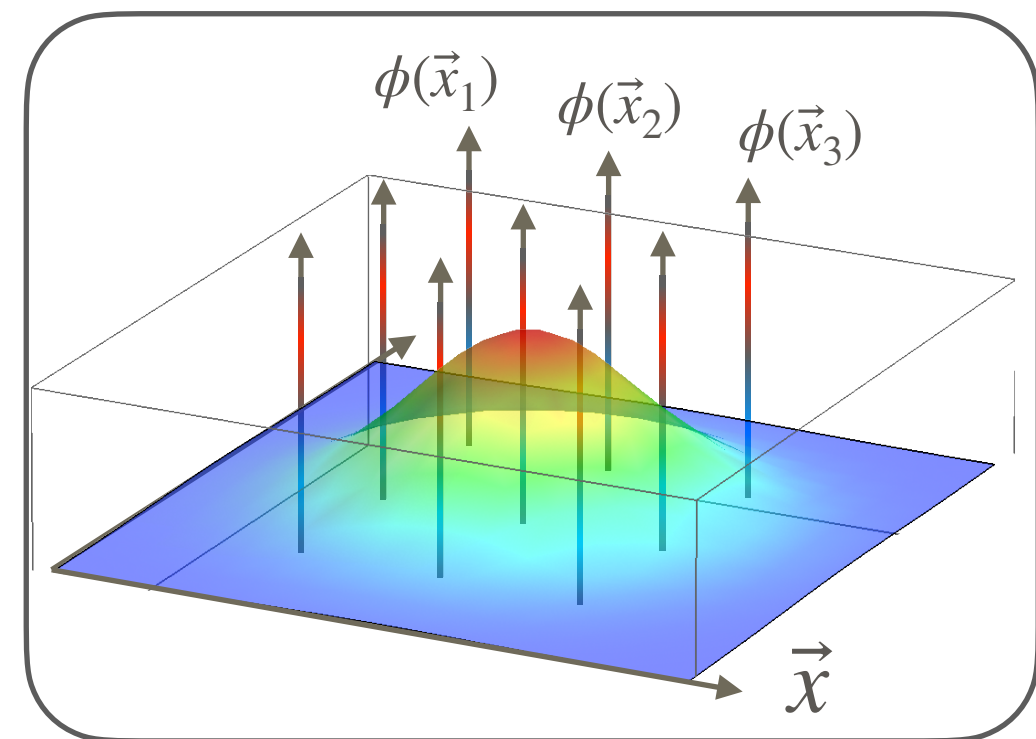
STEP 1 : NUCLEATION

.....

Field space



Position space



nucleation (核生成)

STEP 2 : BUBBLE EXPANSION

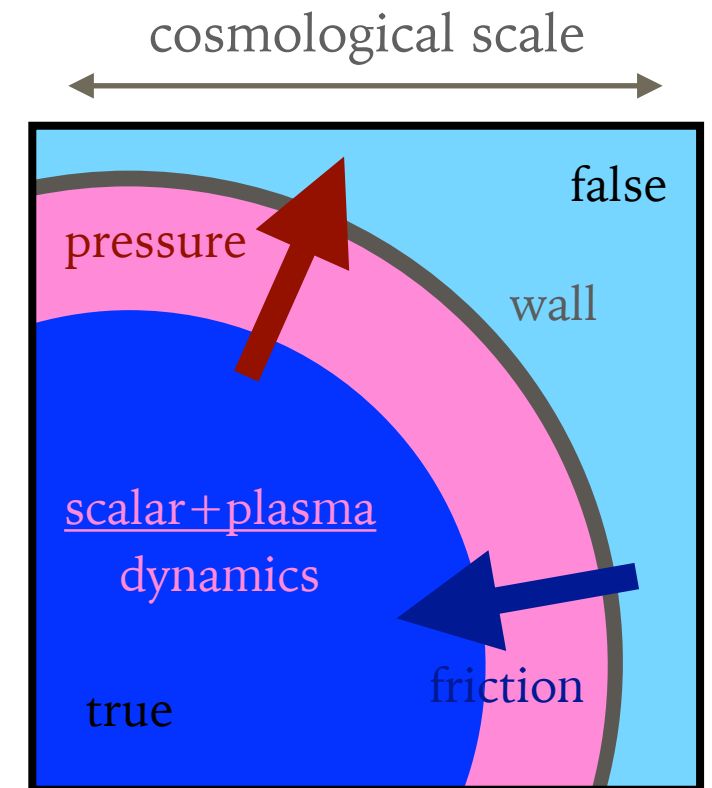
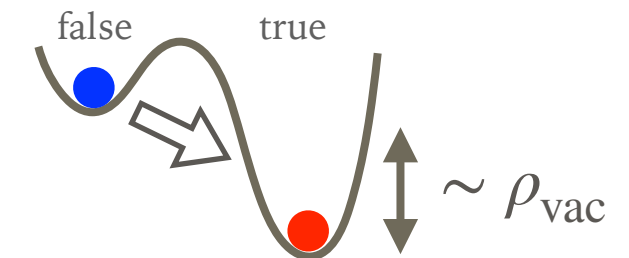
➤ "Pressure vs. Friction" determines the behavior:

(1) **Pressure**: wall is pushed by the released energy

Determined by $\alpha \equiv \rho_{\text{vac}}/\rho_{\text{plasma}}$

see e.g. [Espinosa et al. '10, Hindmarsh et al. '15, Giese et al. '20, Giese et al. '21]

(2) **Friction**: wall is pushed back by plasma particles



STEP 2 : BUBBLE EXPANSION

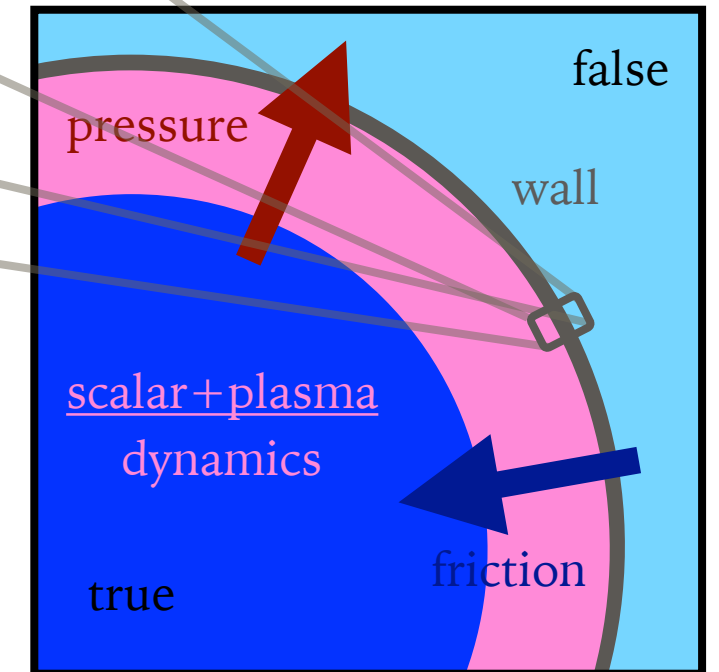
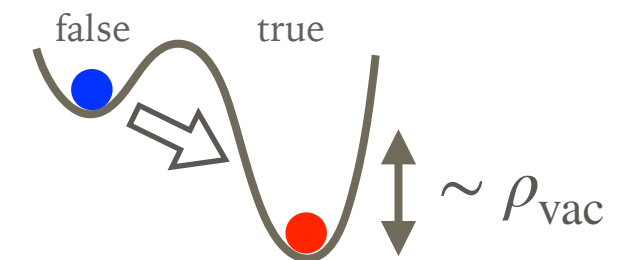
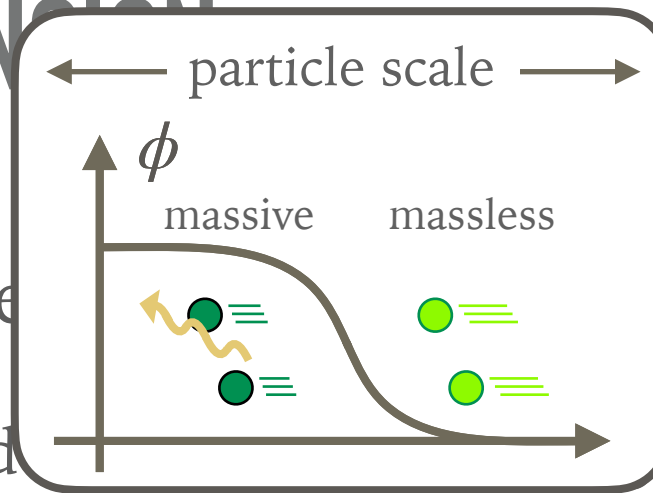
➤ "Pressure vs. Friction" diagram

(1) **Pressure**: wall is pushed

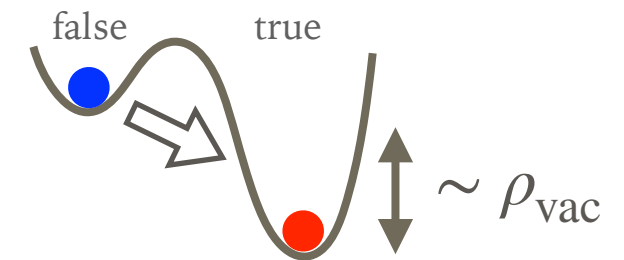
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see e.g. [Espinosa et al. '10, Hindmarsh et al. '15, Giese et al. '20, Giese et al. '21]

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STEP 2 : BUBBLE EXPANSION



➤ "Pressure vs. Friction" determines the behavior:

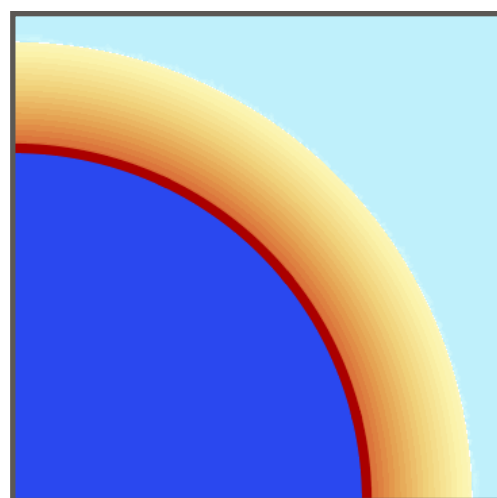
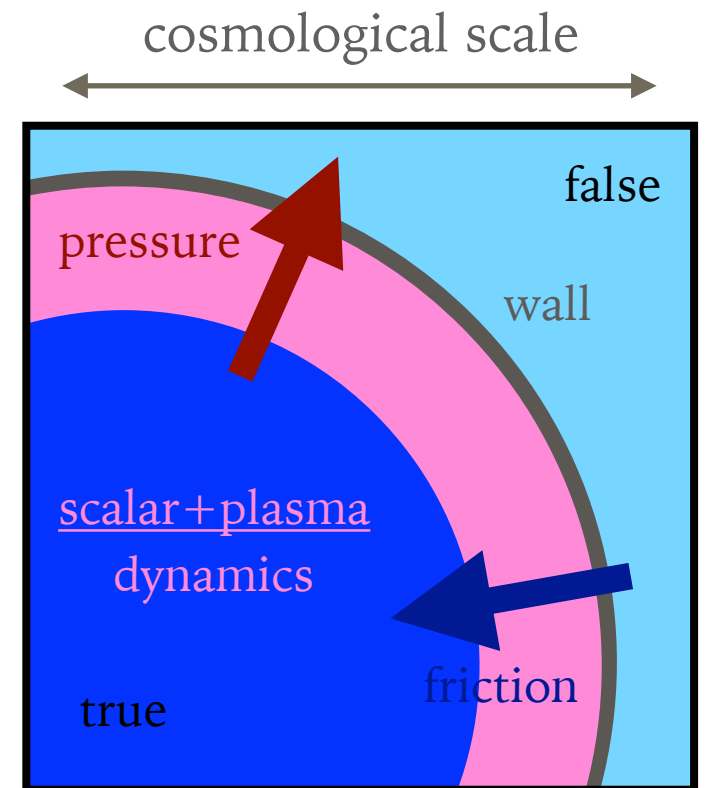
(1) **Pressure**: wall is pushed by the released energy

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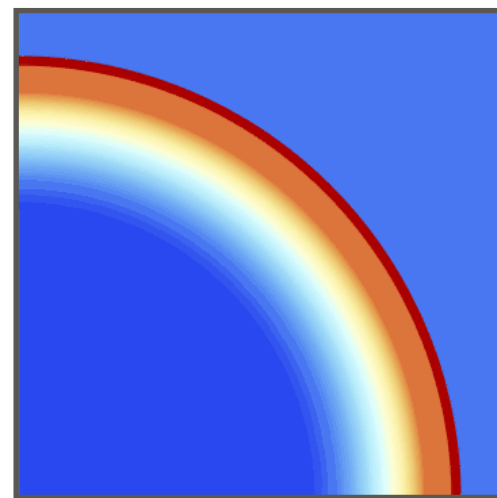
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(2) **Friction**: wall is pushed back by plasma particles

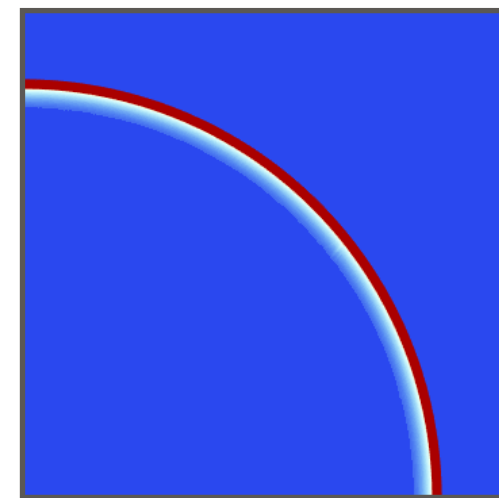
➤ Different types of bubble expansion



deflagration



detonation



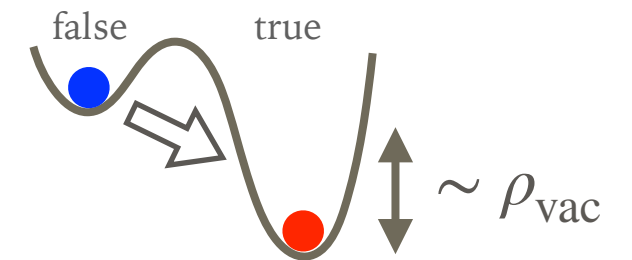
~ 1 relativistic detonation $\gg 1$



runaway

α

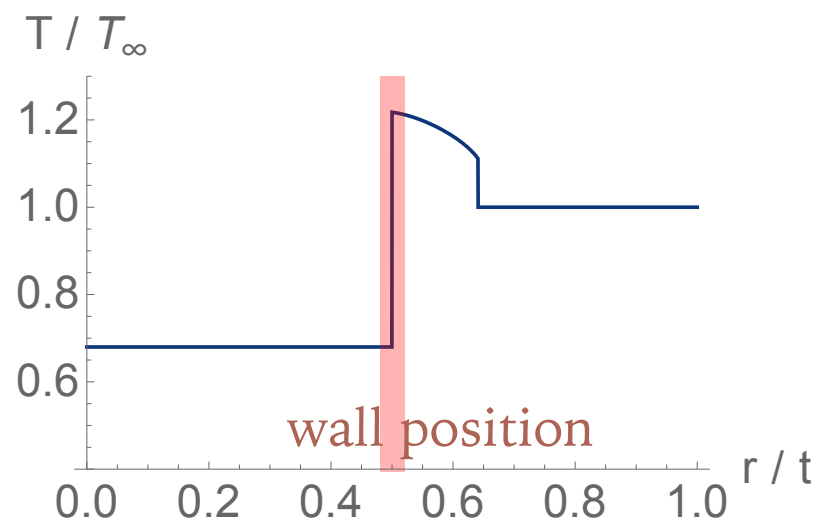
STEP 2 : BUBBLE EXPANSION



➤ "Pr

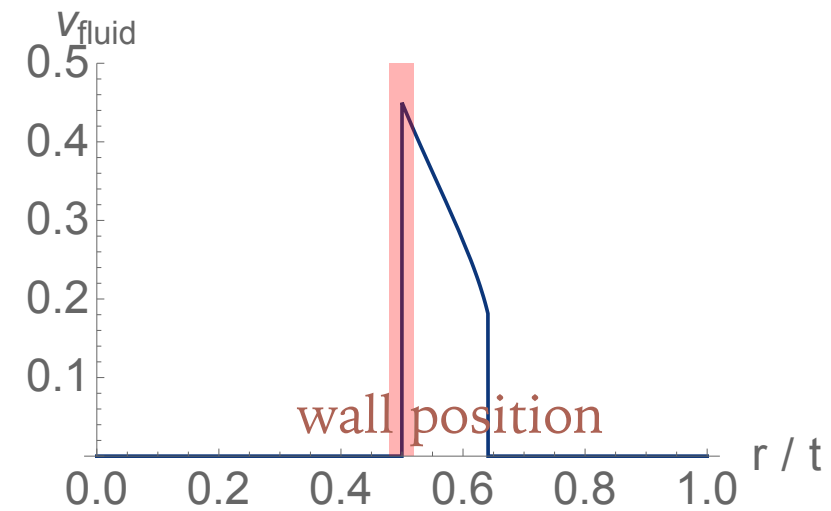
(1)

Temperature

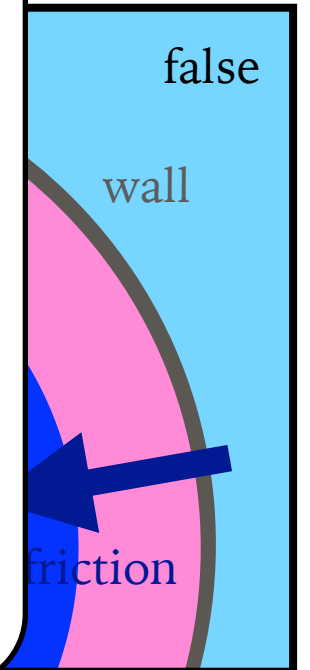


(2)

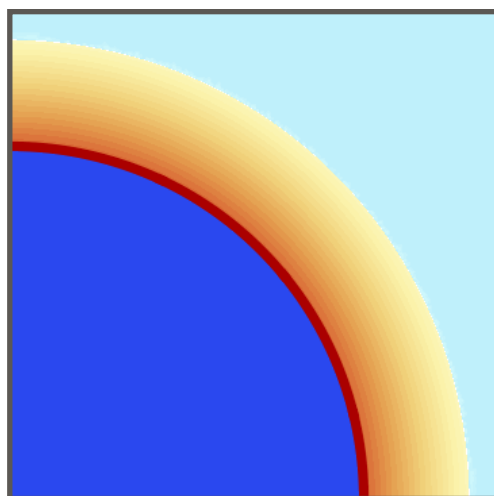
Fluid outward velocity



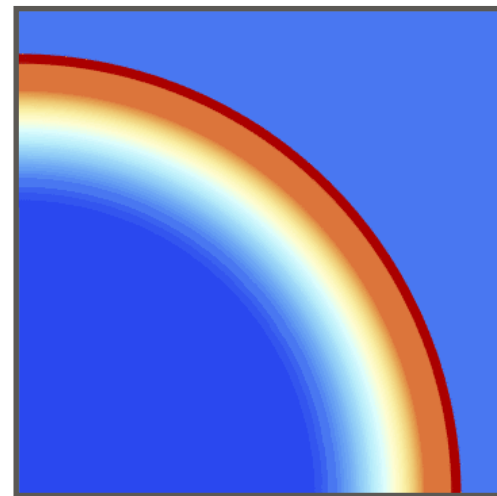
al scale



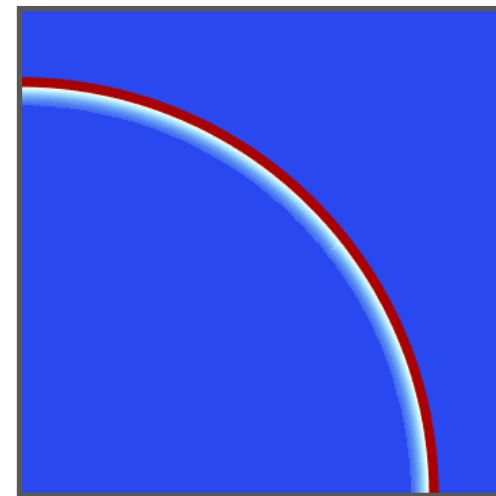
➤ Dis



deflagration



detonation



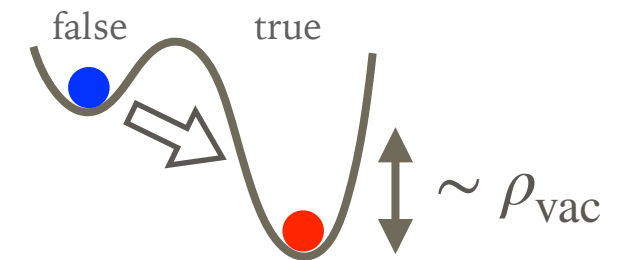
~ 1 relativistic detonation $\gg 1$



runaway

α

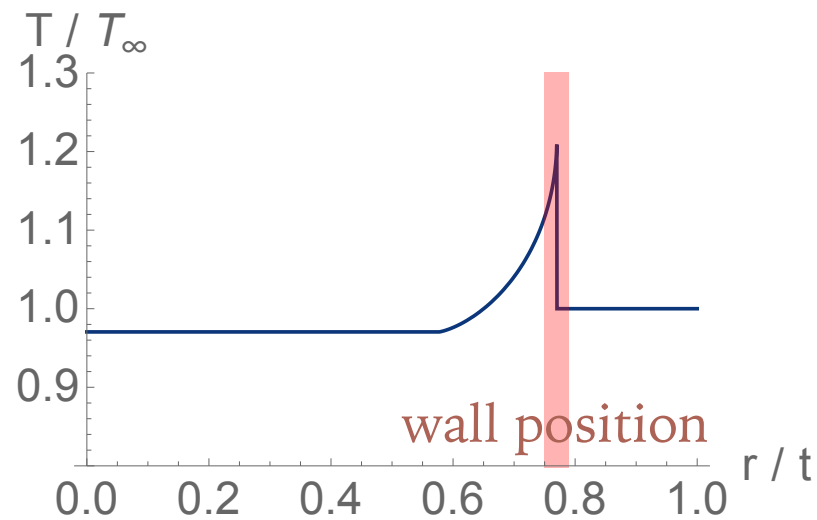
STEP 2 : BUBBLE EXPANSION



➤ "Pr

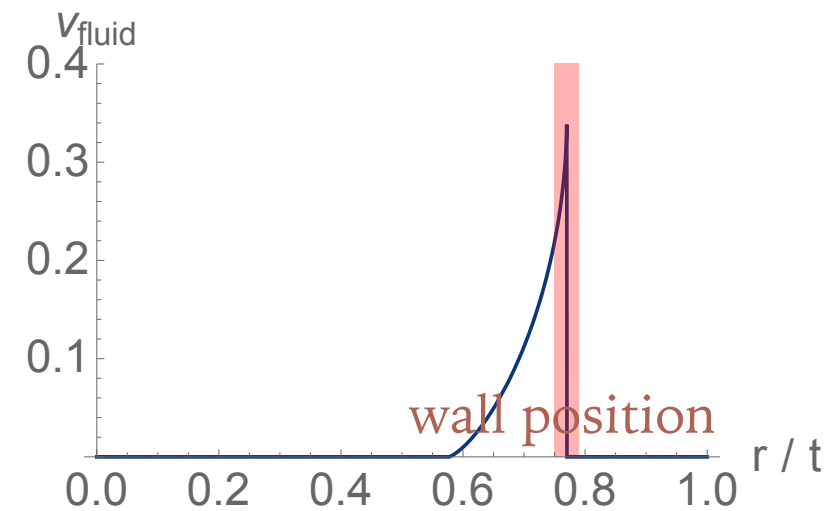
(1)

Temperature

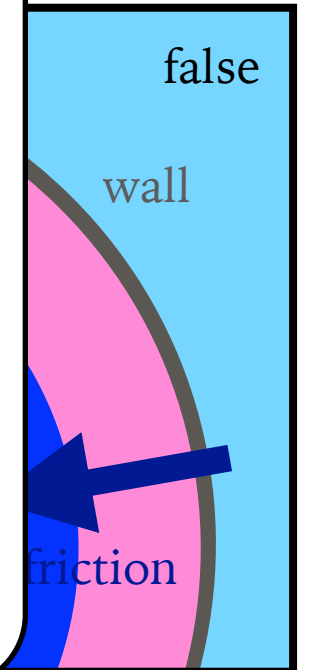


(2)

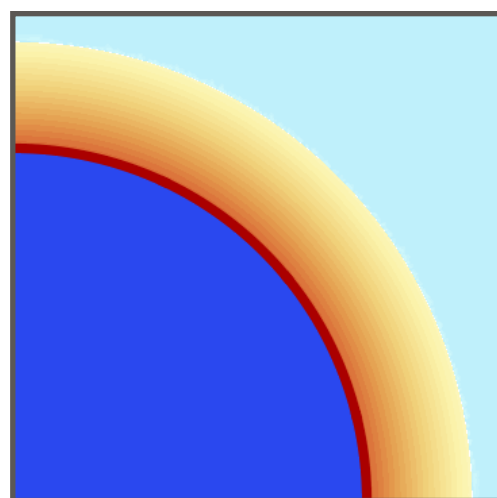
Fluid outward velocity



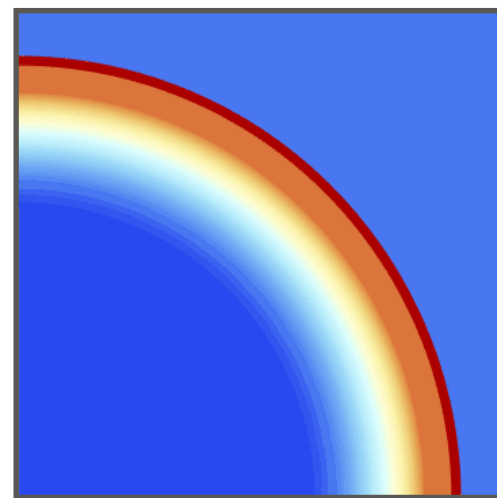
al scale



➤ Dis

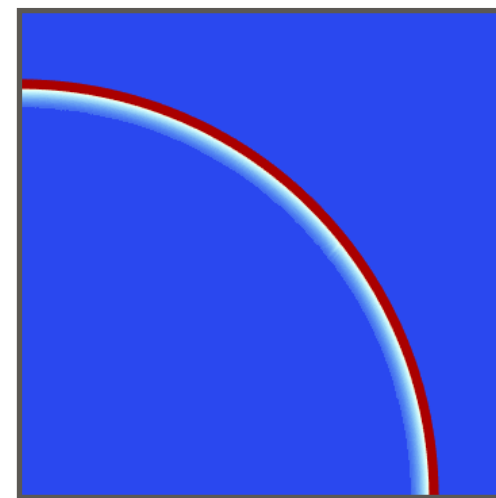


deflagration



detonation

~ 1



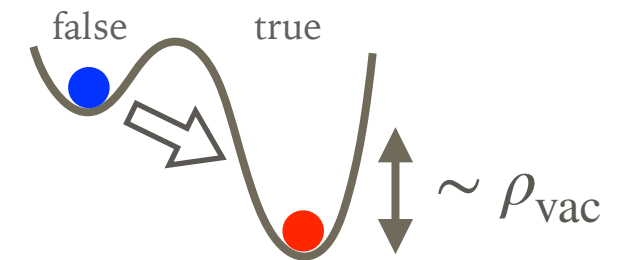
relativistic detonation $\gg 1$



runaway

α

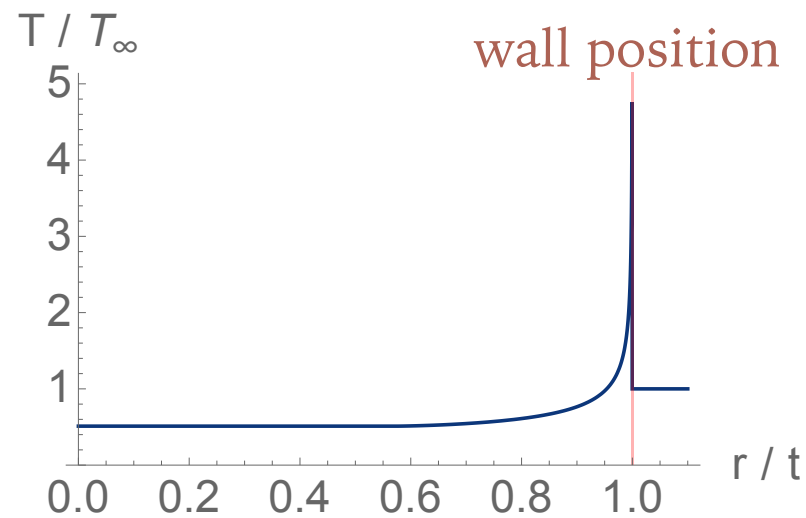
STEP 2 : BUBBLE EXPANSION



➤ "Pr

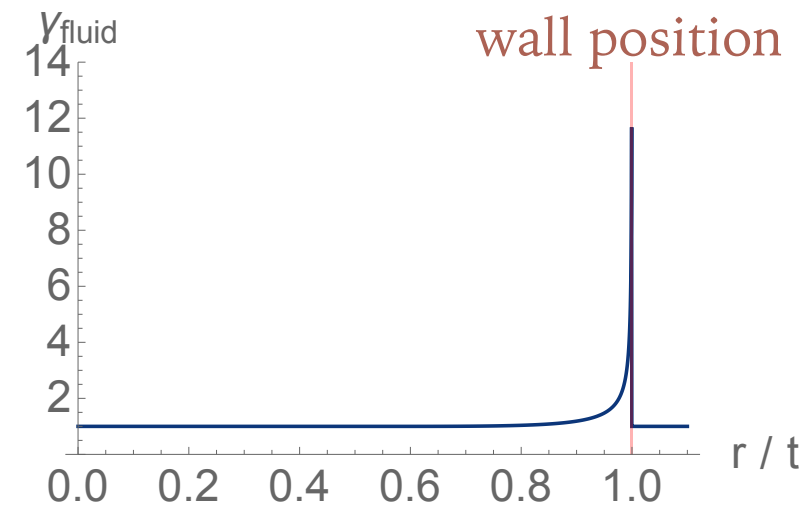
(1)

Temperature

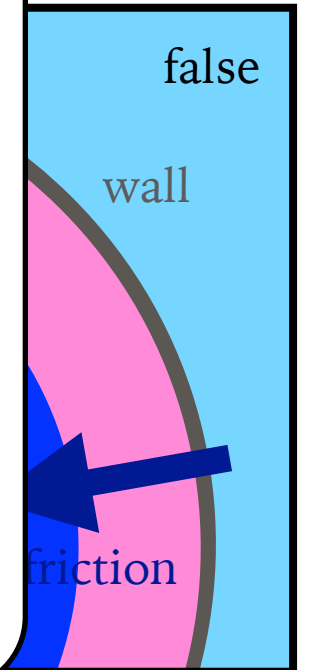


(2)

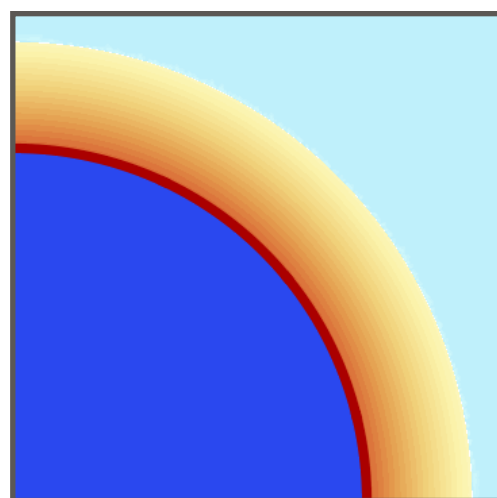
Fluid outward velocity



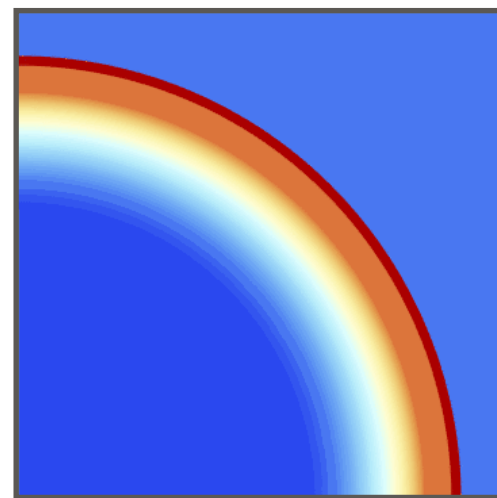
al scale



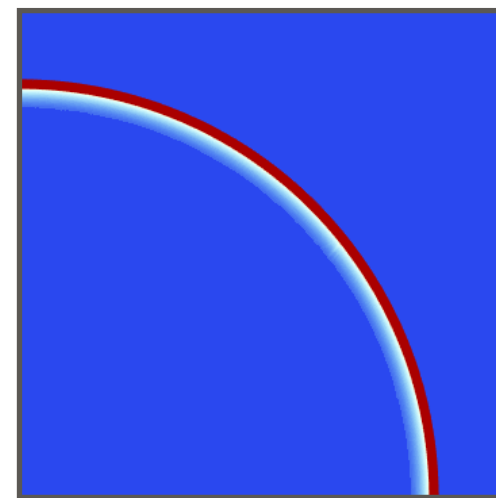
➤ Dis



deflagration



detonation



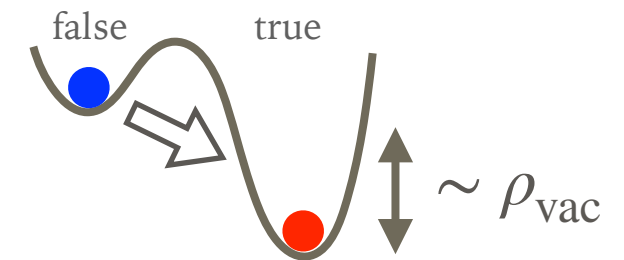
~ 1 relativistic detonation $\gg 1$



runaway

α

STEP 2 : BUBBLE EXPANSION



➤ "Pr

(1)

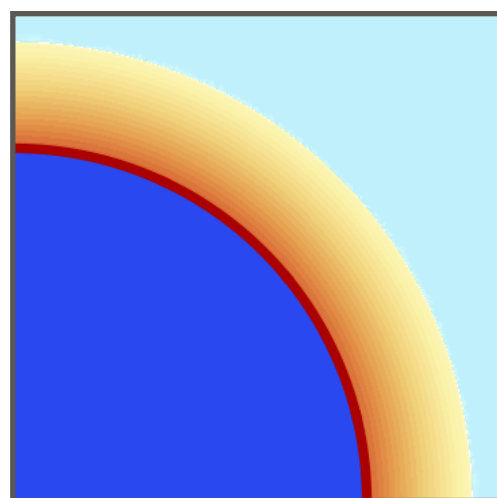
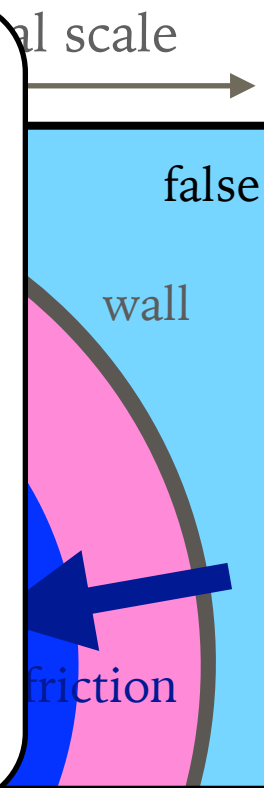
Plasma particles cannot stop the acceleration of the walls:
walls continue to accelerate until they collide with others

(2)

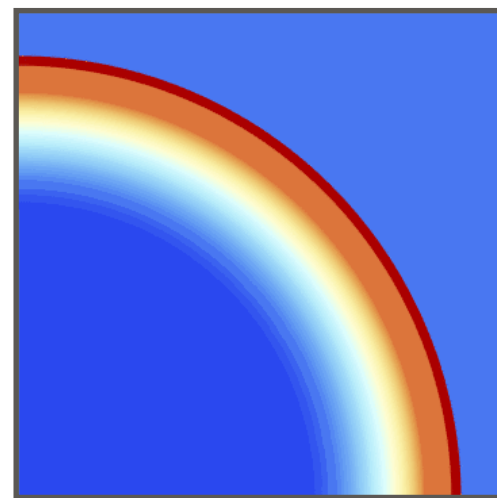
[Bodeker & Moore '09, '17] [Azatov & Vanvlasselaer '20] [Höche, Kozaczuk, Long, Turner, Wang '20]

[Gouttenoire, RJ, Sala '21] [Azatov, Barni, Petrossian-Byrne, Vanvlasselaer '23] ...

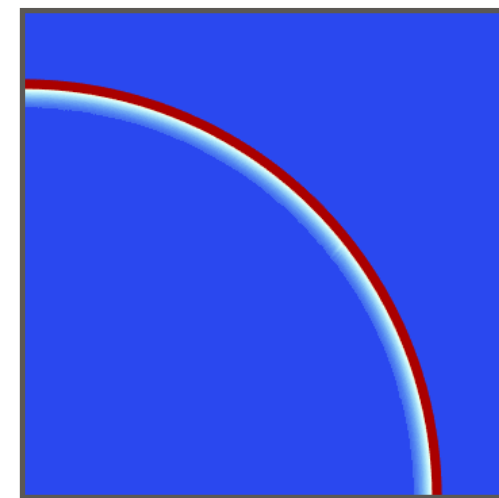
➤ Dis



deflagration



detonation



~ 1 relativistic detonation $\gg 1$



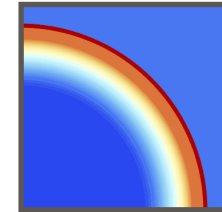
runaway

α

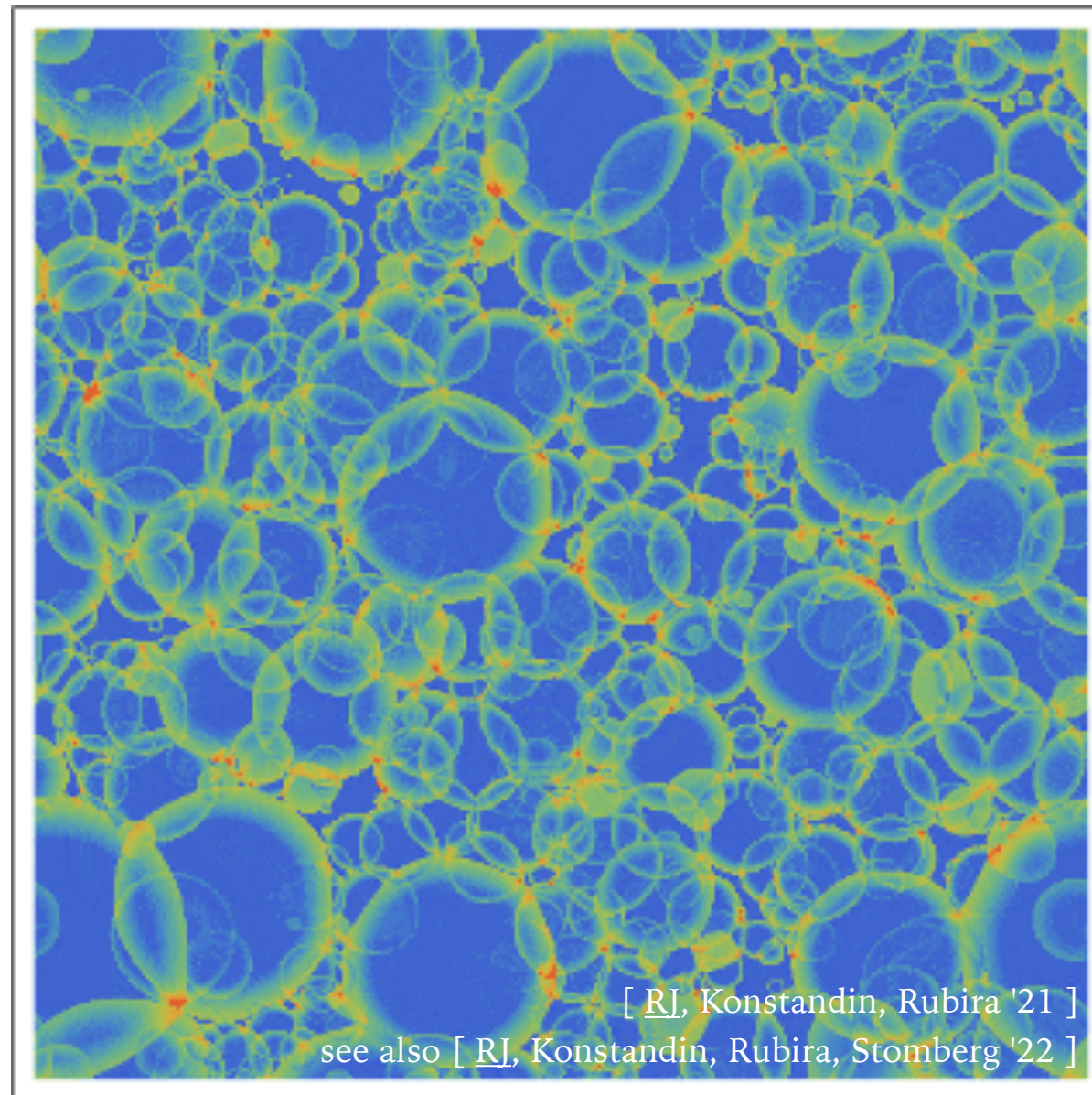


STEP 3: BUBBLE COLLISION & FLUID DYNAMICS

- Bubbles collide, and fluid dynamics sets in (example for)



[Hindmarsh, Huber, Rummukainen, Weir '14, '15, '17] [Hindmarsh '15, +Hijazi '19]



[[R](#)], Konstandin, Rubira '21]

see also [[R](#)], Konstandin, Rubira, Stomberg '22]

STEP 3: BUBBLE COLLISION & FLUID DYNAMICS

.....

- We are developing a new simulation scheme for GW production from sound waves

"The Higgsless scheme"

[[R](#)], Konstandin, Rubira '21] [[R](#)], Konstandin, Rubira, Stomberg '22]



T. Konstandin



H. Rubira



I. Stomberg

- Advantages:

- less artifact (from scalar walls), better resolution for shock waves, ...

GRAVITATIONAL WAVE SOURCES

see e.g. [Caprini et al. '16] [Caprini et al. '20]

➤ Bubble collision

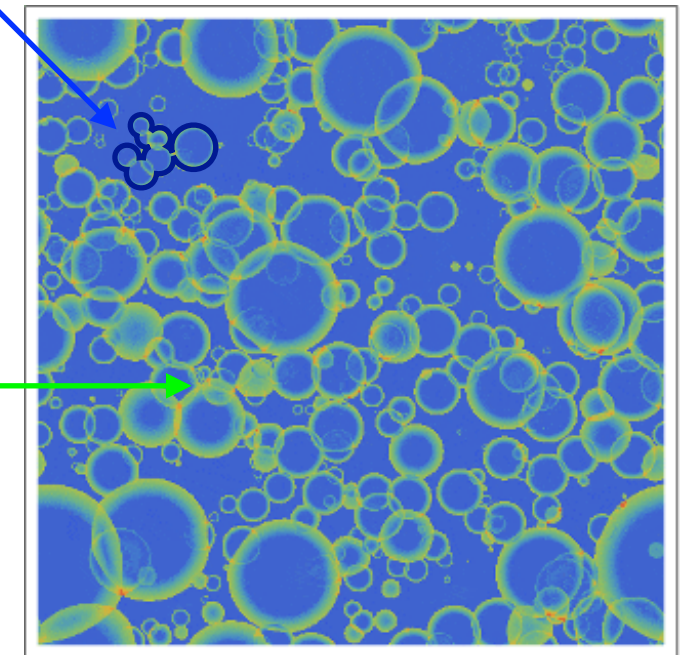
- Kinetic & gradient energy of the scalar field
(= order parameter field)
- Dominant when the transition is extremely strong
and the walls runaway

➤ Sound waves

- Compression mode of the fluid motion
- Dominant unless the transition is extremely strong

➤ Turbulence

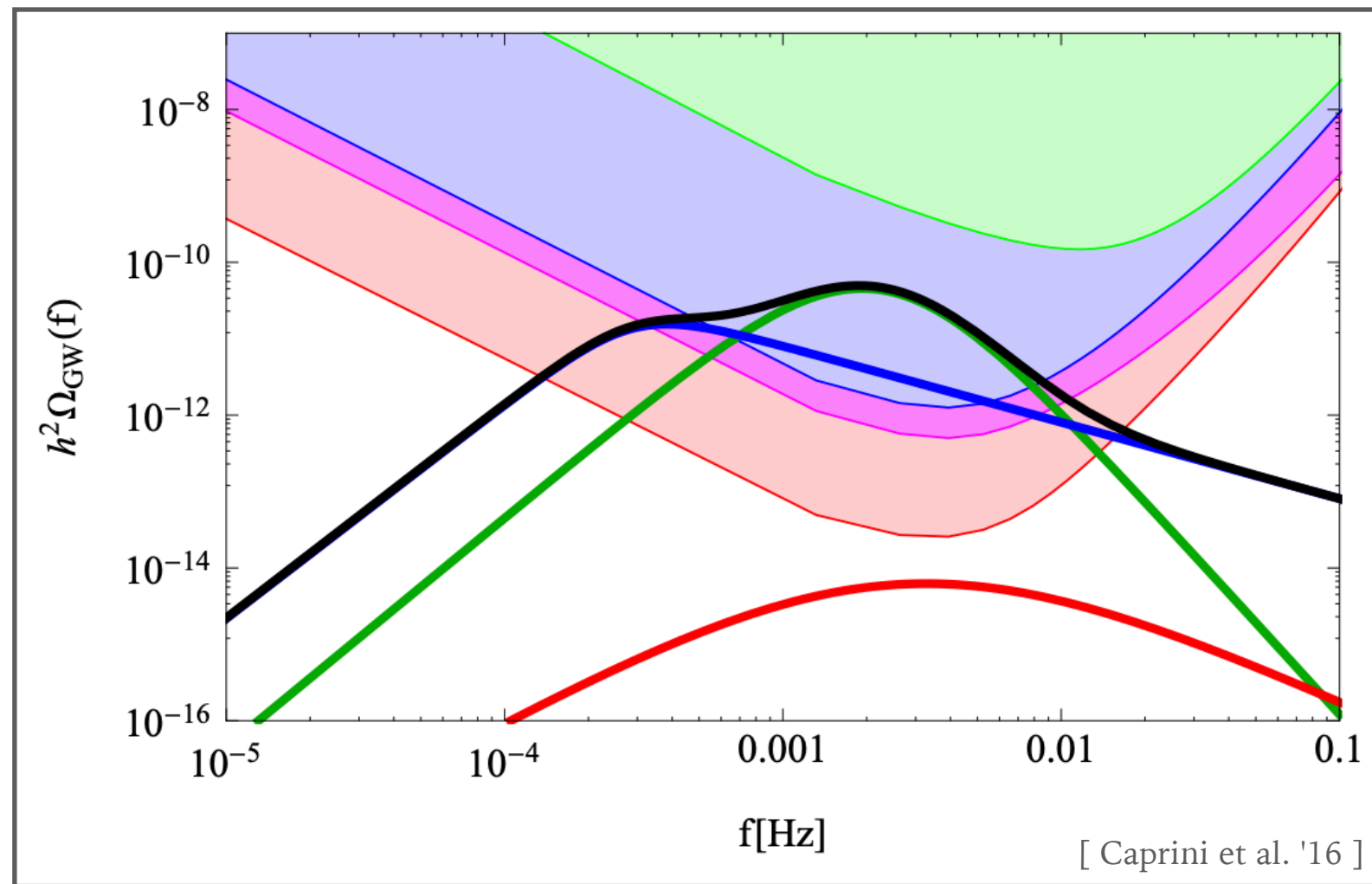
- Turbulent motion caused by fluid nonlinearity
- Expected to develop at a later stage



important at later stage

GRAVITATIONAL WAVE SPECTRUM

.....





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GW PRODUCTION: THE STANDARD LORE & BEYOND

➤ GW sources e.g. [Caprini et al. '16] [Caprini et al. '20]

Bubble walls [Kosowsky, Turner, Watkins '92] [Kosowsky, Turner '92] ...

Energy released accumulates in the walls (= scalar field kinetic & gradient)

Fluid = Sound waves & Turbulence [Kamionkowski, Kosowsky, Turner '93] ...
[Hindmarsh, Huber, Rummukainen, Weir '14] ...

Particles in the broken phase frequently interact and can be described by fluid picture.

Aren't we missing one possibility?

GW PRODUCTION: THE STANDARD LORE & BEYOND

➤ GW sources e.g. [Caprini et al. '16] [Caprini et al. '20]

Bubble walls [Kosowsky, Turner, Watkins '92] [Kosowsky, Turner '92] ...

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[Hindmarsh, Huber, Rummukainen, Weir '14] ...

Particles in the broken phase frequently interact and can be described by fluid picture.

Feebly-interacting particles

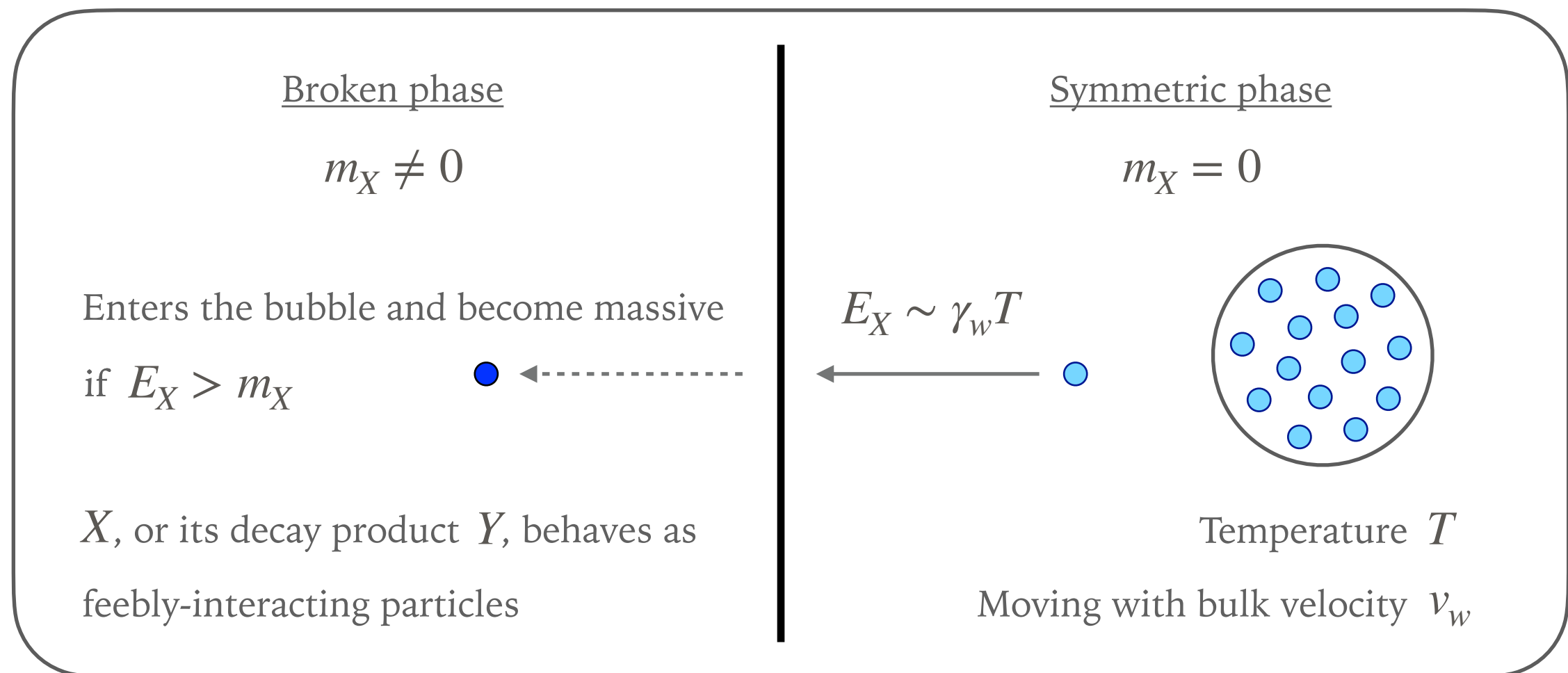
Particles in the broken phase are only feebly interacting and free-stream.

PARTICLE PHYSICS FRAMEWORK

► Setup:

In the broken phase, particles or their decay product free-stream

Wall rest frame



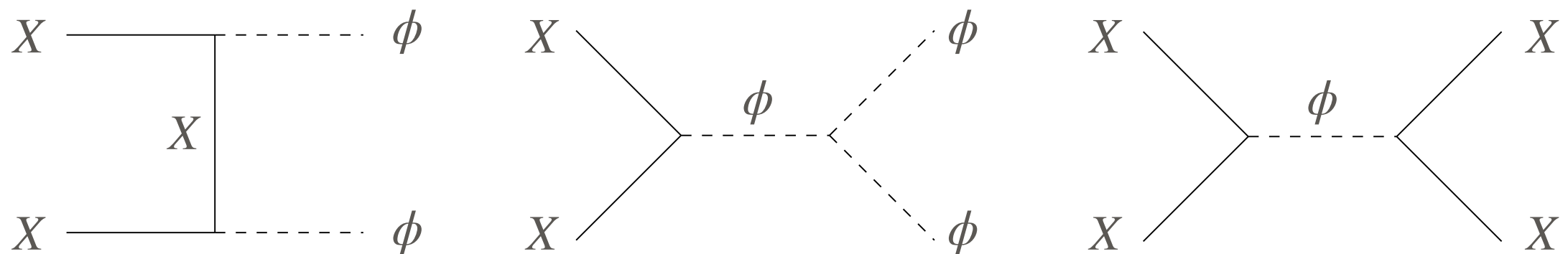
PARTICLE PHYSICS FRAMEWORK

- Consider a dark-sector thermal bath, with temperature T
- ...that undergoes a first-order phase transition
 - scalar field ϕ drives the transition
 - bubble walls reach a terminal velocity v_w (or equivalently $\gamma_w = 1/\sqrt{1 - v_w^2}$)
due to the coupling to particle X or others
- ...and also produces feebly-interacting particles
 - particle X becomes massive when crossing the wall
 - either X or its decay product behaves as feebly-interacting particles

CONDITIONS FOR FEEBLE INTERACTION

► How do X particles interact?

- couplings that gives rise to the mass of X also give rise to interactions



► Can $X = Z'$ boson free-stream? \rightarrow yes, but a bit difficult

- condition to free-stream over a typical bubble size R_*

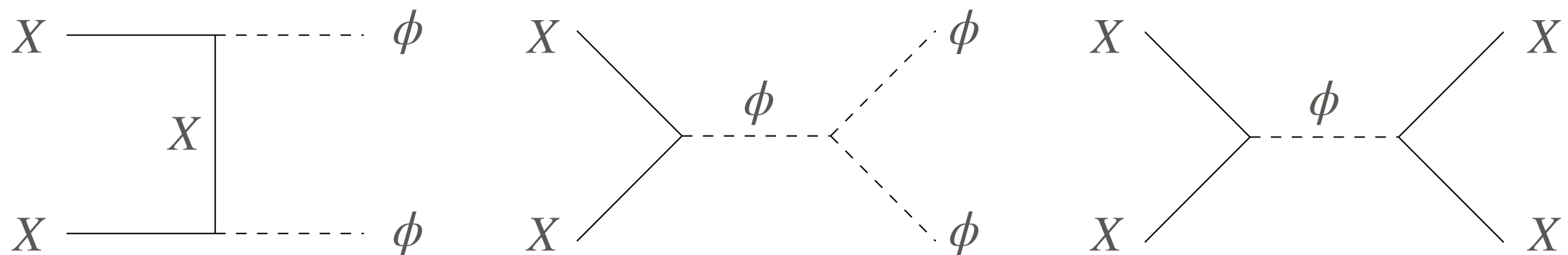
$$n_X \sigma R_* \sim T^3 \frac{g'^4}{(4\pi)^2} \frac{m_{Z'}^2}{m_\phi^4} \frac{1}{\beta} \sim \frac{1}{(4\pi)^2} \frac{g'^6}{\lambda_\phi^2} \frac{\overset{\text{large}}{TM_P} H}{\langle \phi \rangle^2 \beta} \lesssim 1$$

- you can just suppress g' , but then X particles become a subcomponent

CONDITIONS FOR FEEBLE INTERACTION

► How do X particles interact?

- couplings that gives rise to the mass of X also give rise to interactions



- ## ► Can $X = Z'$ boson freeze out? e.g. $\langle \phi \rangle \sim 10T \sim 10^{11} \text{ GeV}$ difficult
- condition to free-stream $g' \sim 0.3, \lambda_\phi \sim 1, \beta/H \sim 100$

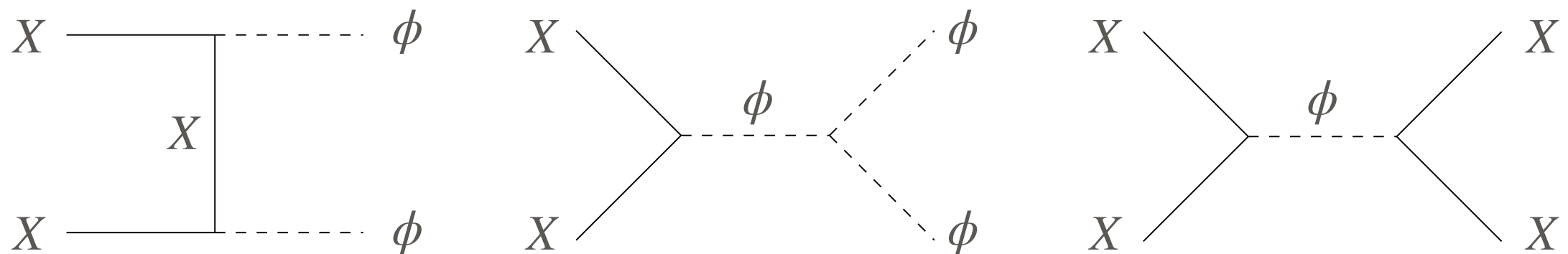
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- you can just suppress g' , but then X particles become a subcomponent

CONDITIONS FOR FEEBLE INTERACTION

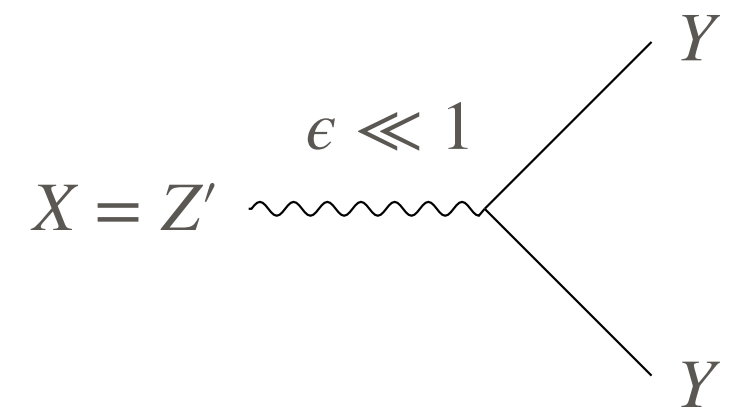
➤ How do X particles interact?

- couplings that gives rise to the mass of X also give rise to interactions



➤ Can $X = Z'$ boson free-stream? \rightarrow yes, but a bit difficult

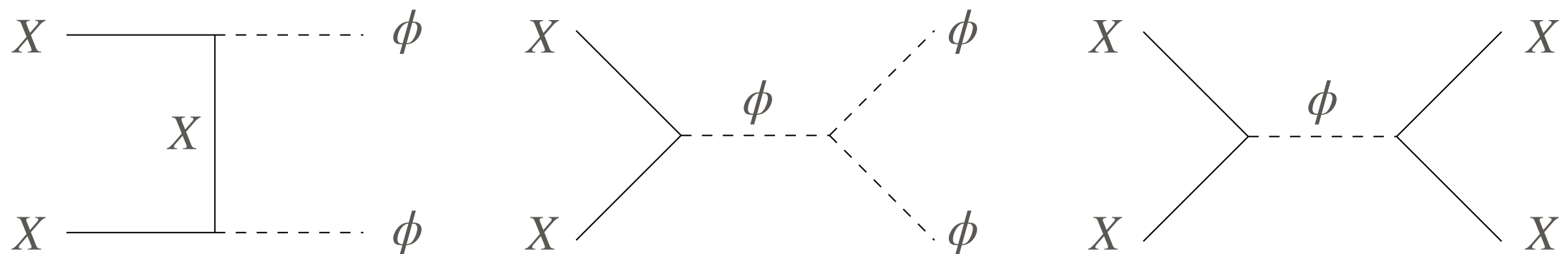
➤ Can a decay product of X free-stream? \rightarrow yes



CONDITIONS FOR FEEBLE INTERACTION

➤ How do X particles interact?

- couplings that gives rise to the mass of X also give rise to interactions



- Can $X = Z'$ boson free-stream? \rightarrow yes, but a bit difficult
- Can a decay product of X free-stream? \rightarrow yes
- In the following, we assume that the feebly-interacting particles form a dominant component in the broken phase

SINGLE-BUBBLE PROFILE

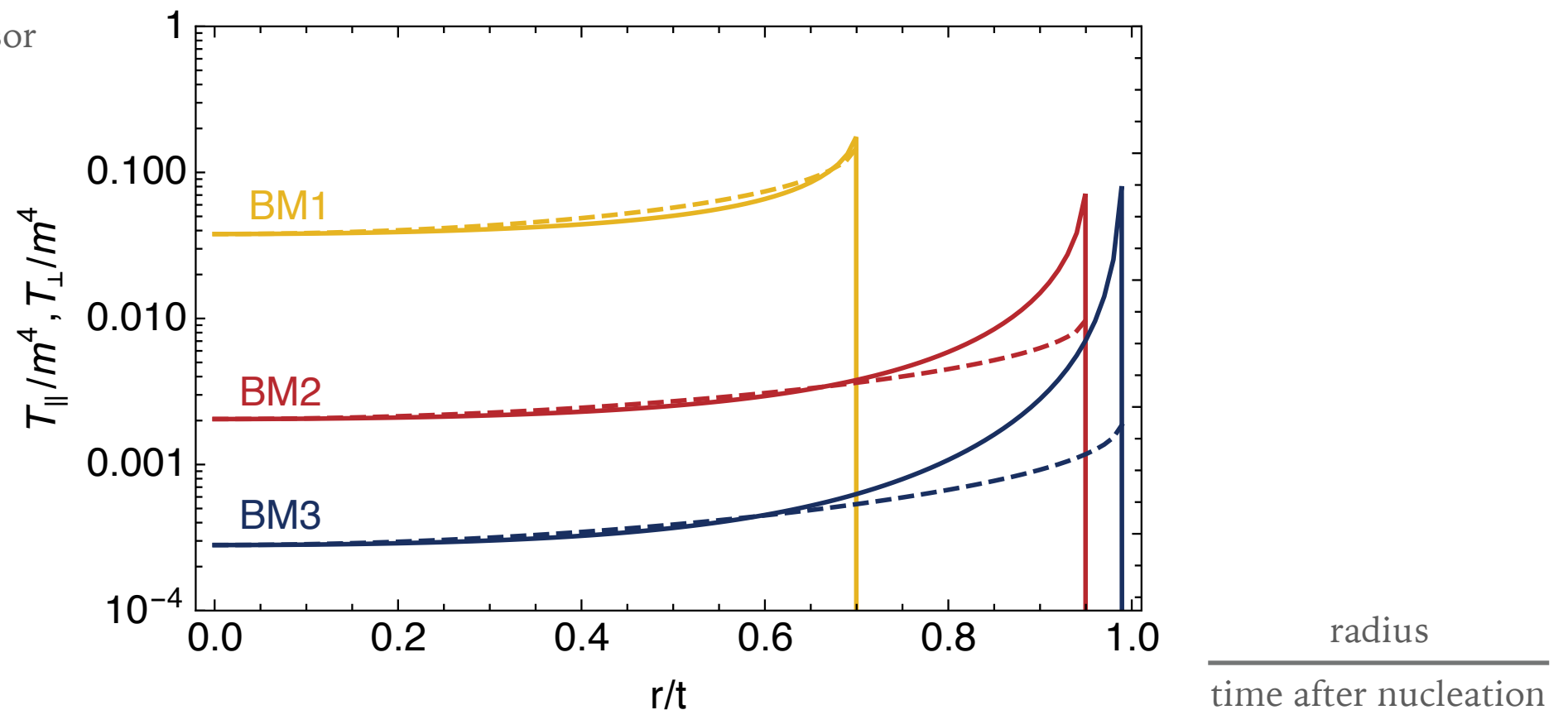
- Energy-momentum tensor of a single bubble before collision

We take 3 benchmark points: $\left\{ \begin{array}{ll} m/T = 1, \quad v_w = 0.7 & \text{(BM1)} \\ m/T = 2, \quad v_w = 0.95 & \text{(BM2)} \\ m/T = 3, \quad v_w = 0.99 & \text{(BM3)} \end{array} \right.$

Energy-momentum tensor

$$T_{\parallel} = T_{zz}$$

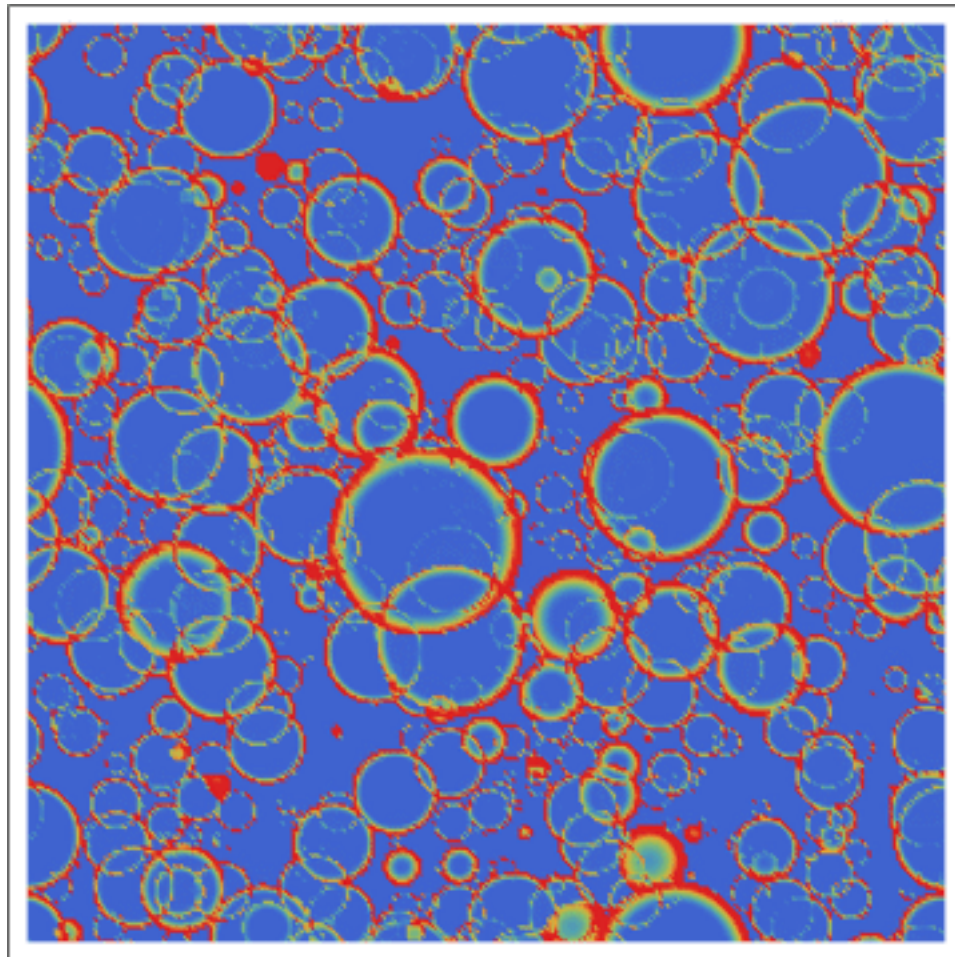
$$T_{\perp} = T_{xx} = T_{yy}$$



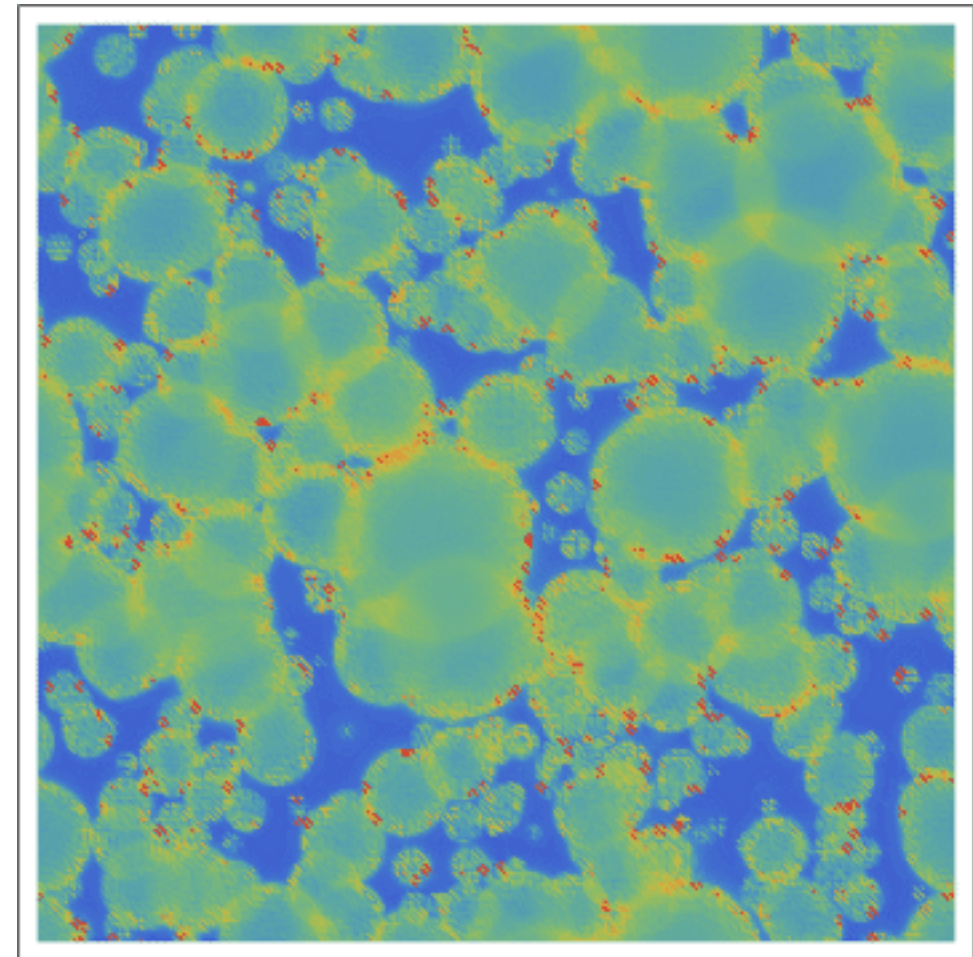
EVOLUTION OF BUBBLES WITH FEEBLY-INTERACTING PARTICLES

- Fluid vs. Feebly-interacting particles in a first-order phase transition

Fluid

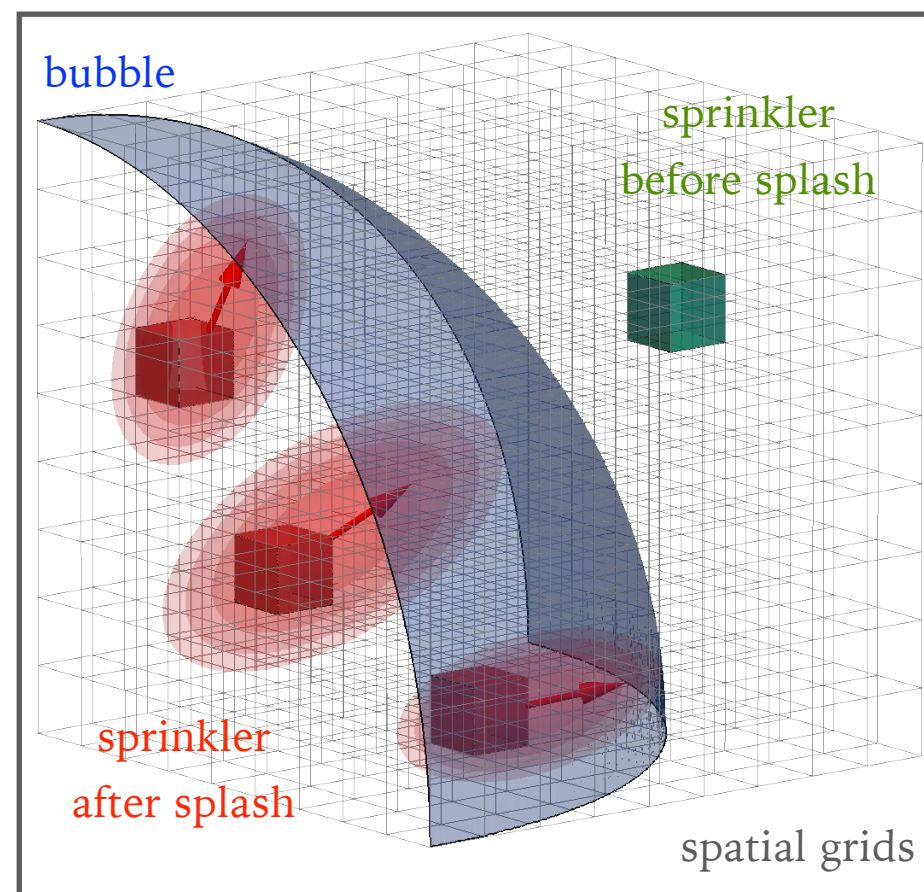


Feebly-interacting



HOW TO CALCULATE THE GW SPECTRUM

- To calculate the GW spectrum, we don't use the time evolution shown in the animation in the previous slides
- We instead propose a new calculation scheme – "sprinkler picture"



SPRINKLER PICTURE FOR GW CALCULATION

➤ How the "sprinkler picture" works

① Imagine **each grid point has a sprinkler** that splashes free-streaming particles when hit by the wall

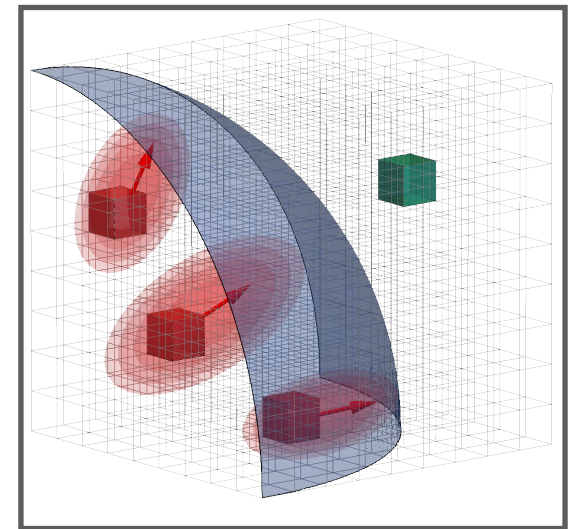
② **The sprinklers are universal:**

their only difference is when and in which direction they are hit

③ GW production from one sprinkler is easily calculable.

Contributions from different sprinklers (= grids) are linearly superposed.

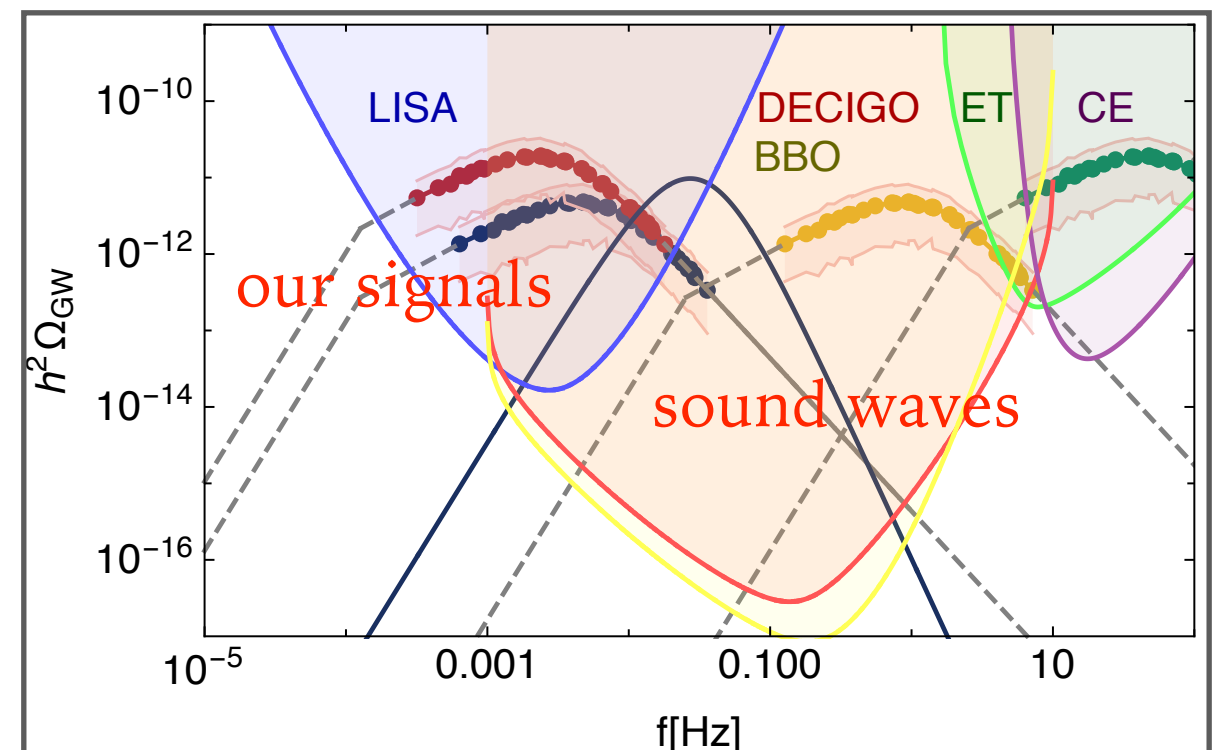
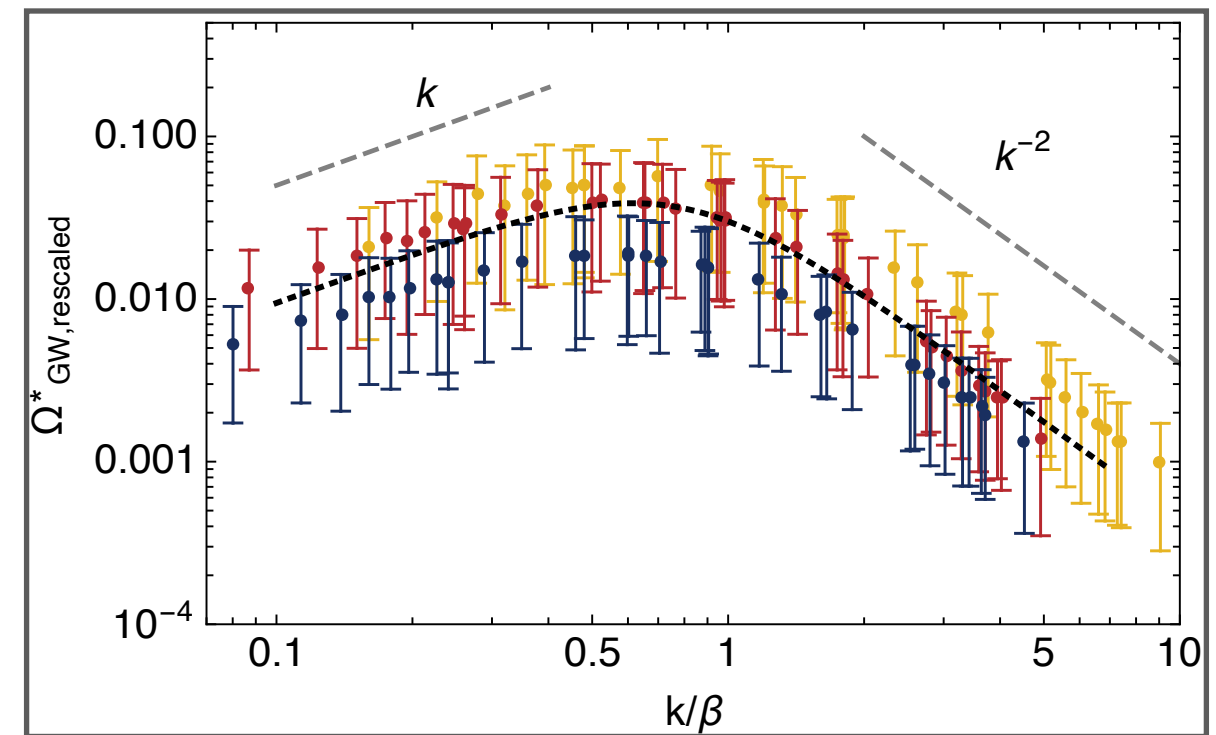
➤ This method is possible because GW production is linear in each sprinkler in the present system



$$\square h_{ij} \sim T_{ij} \sim \sum_{\text{sprinkler } p} T_{ij}^{(p)}$$

GW SPECTRUM

- GW spectral shape is universal for different benchmark points (after normalizing by some factor)
- GW spectral shape is clearly different from sound-wave sources: it stretches over wider frequencies



DISCUSSION

► What is the essential difference?

- Sound waves: it is fluid velocity \vec{v} that superposes linearly

$$\vec{v} = \sum_{I : \text{bubbles}} \vec{v}^{(I)} \longrightarrow T_{ij} \sim w v_i v_j \neq \sum_{I : \text{bubbles}} T_{ij}^{(I)}$$

- Free-streaming particles: it is T_{ij} that superposes linearly

$$T_{ij} = \sum_{I : \text{bubbles}} T_{ij}^{(I)}$$



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Introduction

2
GWs from
sound waves
in FOPT

3
GWs from
FIPs
in FOPT

4
Summary

SUMMARY

- We point out a missing possibility for GW sources in FOPT:

feebly-interacting particles

- We propose a novel GW calculation scheme ("sprinkler picture")
that makes use of the linearity of GW production in each sprinkler
- Feebly-interacting particles are found to leave characteristic imprint
on the GW spectrum

Backup

IR BEHAVIOR OF THE SPECTRUM

[RJ, Takimoto '19, Appendix E]

