



TOHOKU
UNIVERSITY

Cosmic Birefringence and Axion

June 24. 2021, seminar@KIAS

Fumi Takahashi (Tohoku)

Based on [2012.11576](#) with Wen Yin, [2103.08153](#) with Shota Nakagawa and Masaki Yamada

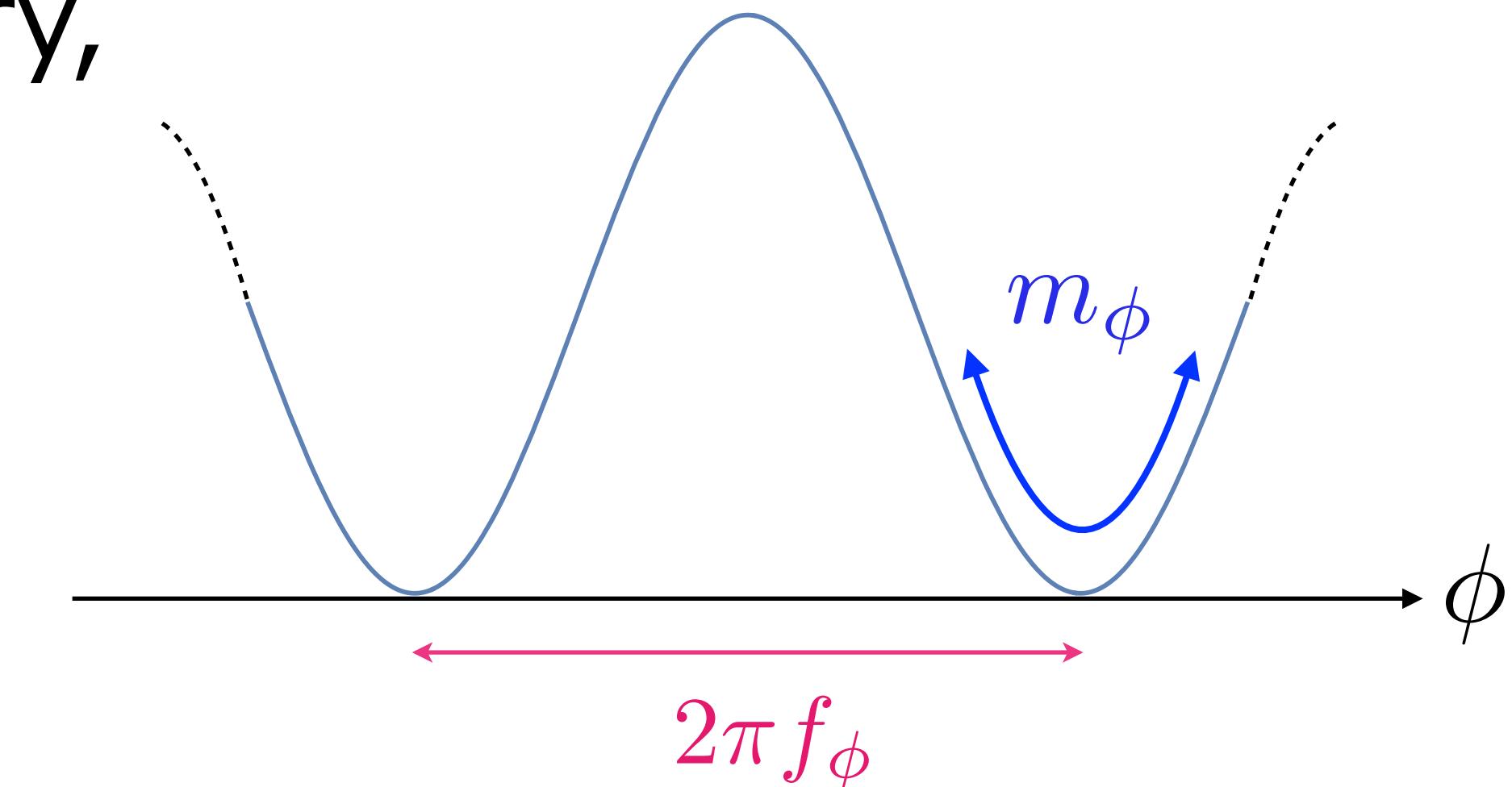
1. Introduction

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An axion enjoys a (discrete) shift symmetry,

$$\phi \rightarrow \phi + 2\pi f_\phi$$

which implies the existence of degenerate vacua.



The properties of the axion are characterized by **mass m_ϕ** and **decay constant f_ϕ** .

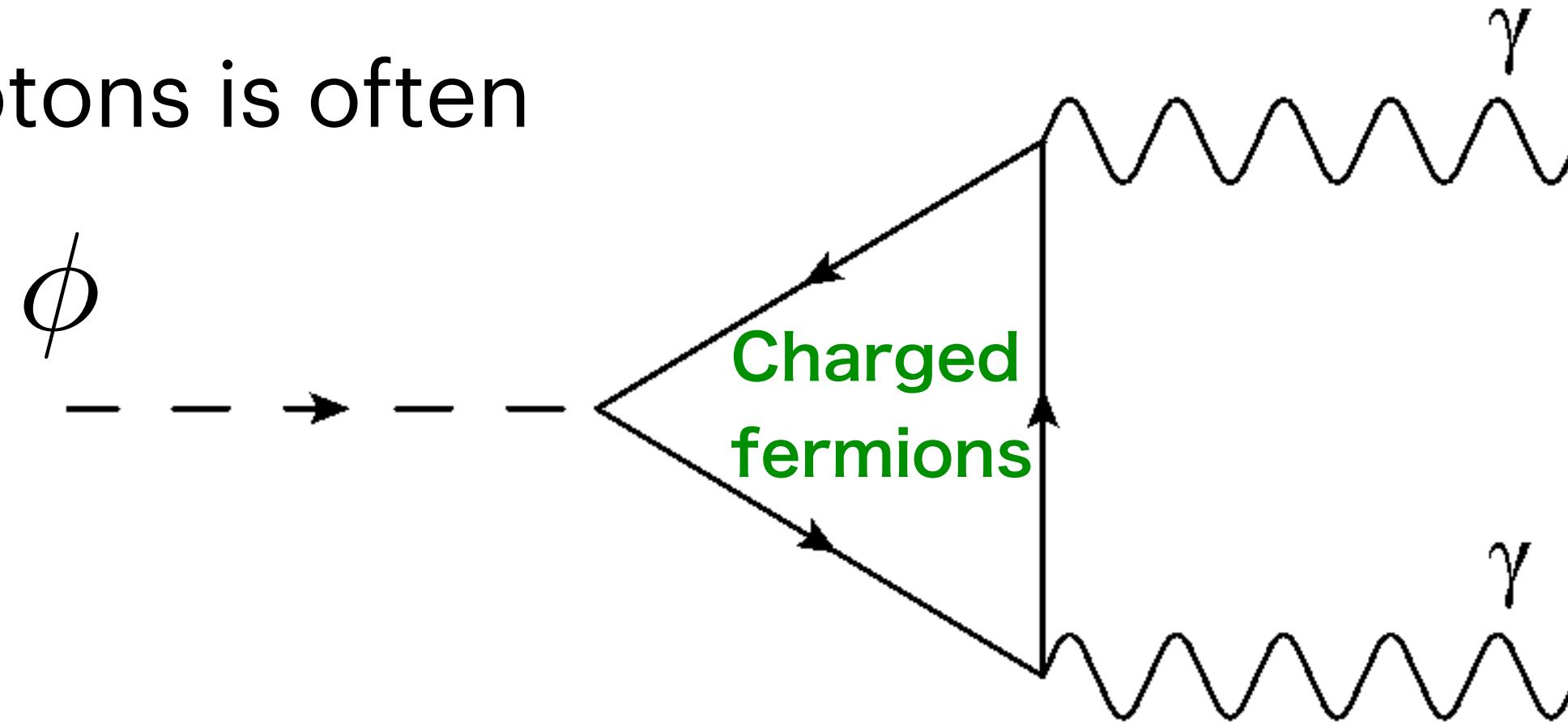
If the axion is very light, and if it has only feeble interactions, it may play an important role in cosmology (DM, DE, ⋯).

Axion couplings to the SM particles:

- **Photons**

$$\mathcal{L}_{\phi\gamma} = -c_\gamma \frac{\alpha}{4\pi} \frac{\phi}{f_\phi} F_{\mu\nu} \tilde{F}^{\mu\nu} = -\frac{1}{4} g_{\phi\gamma\gamma} \phi F_{\mu\nu} \tilde{F}^{\mu\nu},$$

Axion coupled to photons is often referred to as **ALP**.

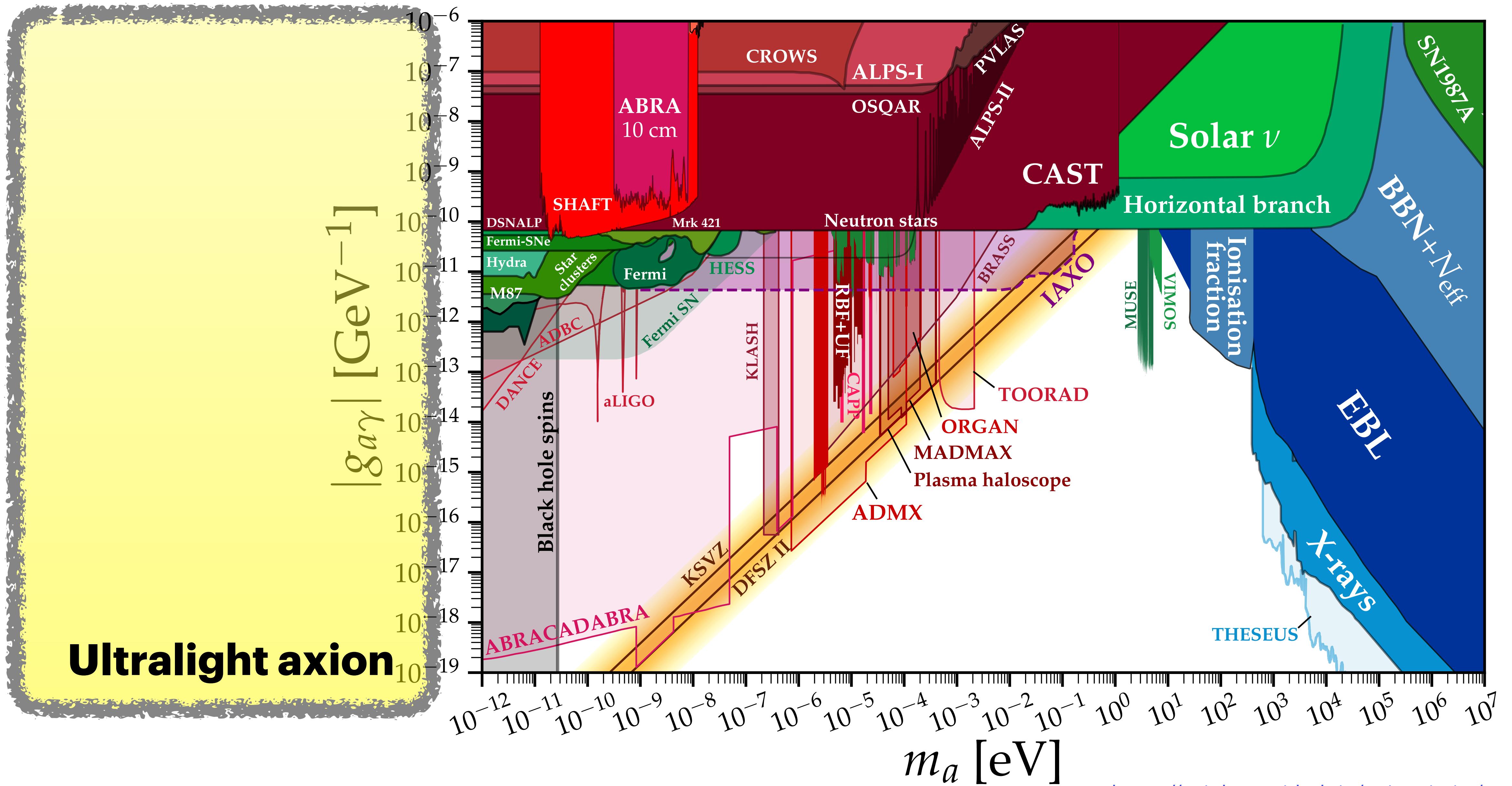


- Electrons $\mathcal{L}_{\phi e} = \frac{C_e}{2f_\phi} \partial_\mu \phi (\bar{\Psi}_e \gamma^\mu \gamma_5 \Psi_e) = -ig_{\phi ee} \phi (\bar{\Psi}_e \gamma_5 \Psi_e) + \dots$

- Nucleons $\mathcal{L}_{\phi N} = \sum_{N=p,n} \frac{C_N}{2f_\phi} \partial_\mu \phi (\bar{\Psi}_N \gamma^\mu \gamma_5 \Psi_N)$

$c_\gamma = O(1)$ in most models, but model-dependent.

Searching for axion/ALP



Cosmic birefringence (CB) due to ALP

Carrol, astro-ph/9806099

Lue, et al, astro-ph/9812088

The polarization plane of CMB gets rotated

if the ALP moves after the recombination (isotropic CB),
or if the ALP has fluctuations (anisotropic CB + isotropic CB).

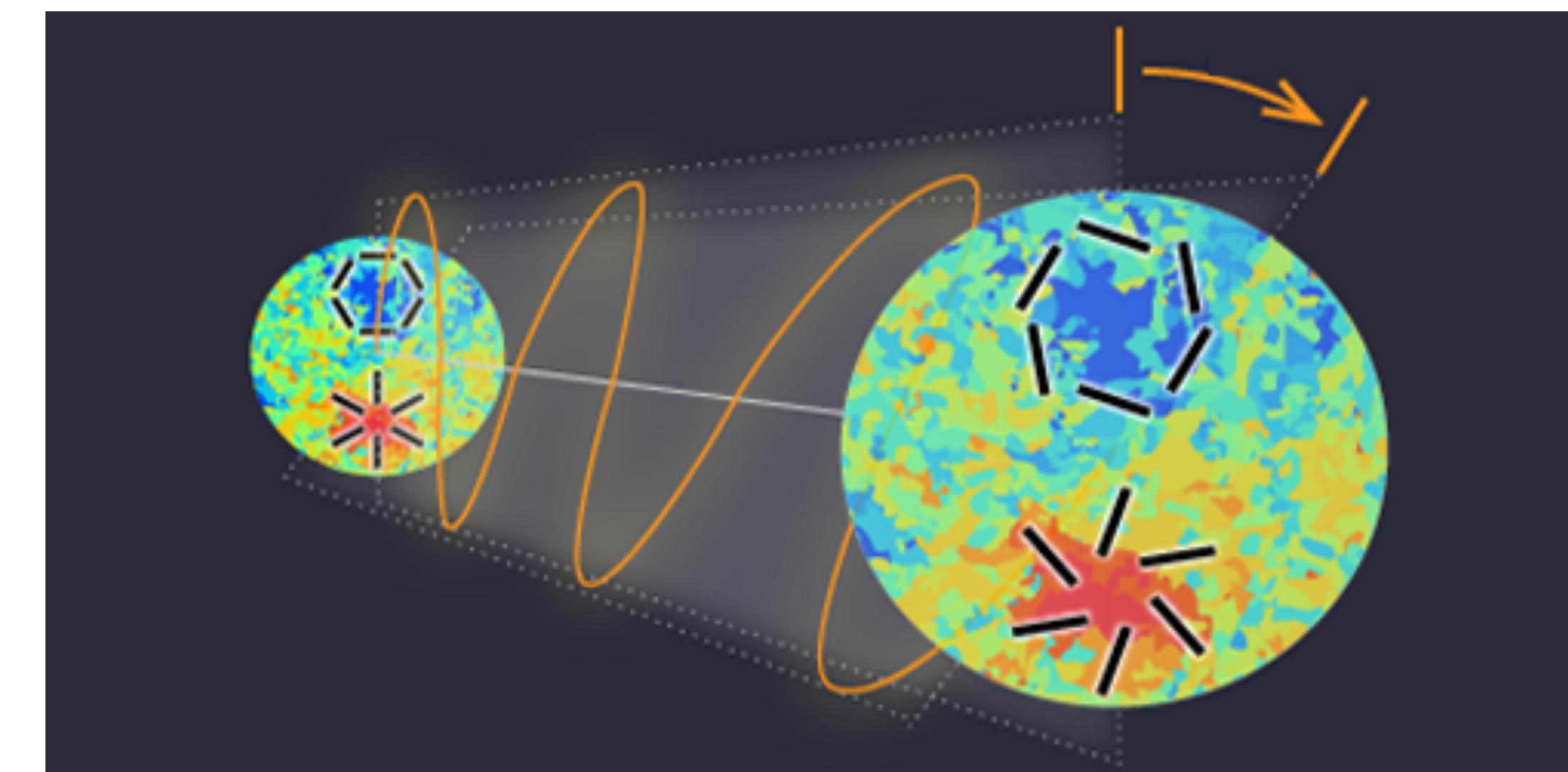
$$\Phi(\Omega) = 0.42 c_\gamma \left(\frac{\phi_{\text{today}} - \phi_{\text{LSS}}(\Omega)}{2\pi f_\phi} \right) \text{ deg}$$

Hint of isotropic CB?

$$\beta = \frac{1}{4\pi} \int d\Omega \Phi(\Omega) = 0.35 \pm 0.14 \text{ deg}$$

Minami, Komatsu, Phys. Rev. Lett. **125**, 221301

$$\mathcal{L}_{\phi\gamma} = -c_\gamma \frac{\alpha}{4\pi} \frac{\phi}{f_\phi} F_{\mu\nu} \tilde{F}^{\mu\nu} = -\frac{1}{4} g_{\phi\gamma\gamma} \phi F_{\mu\nu} \tilde{F}^{\mu\nu},$$

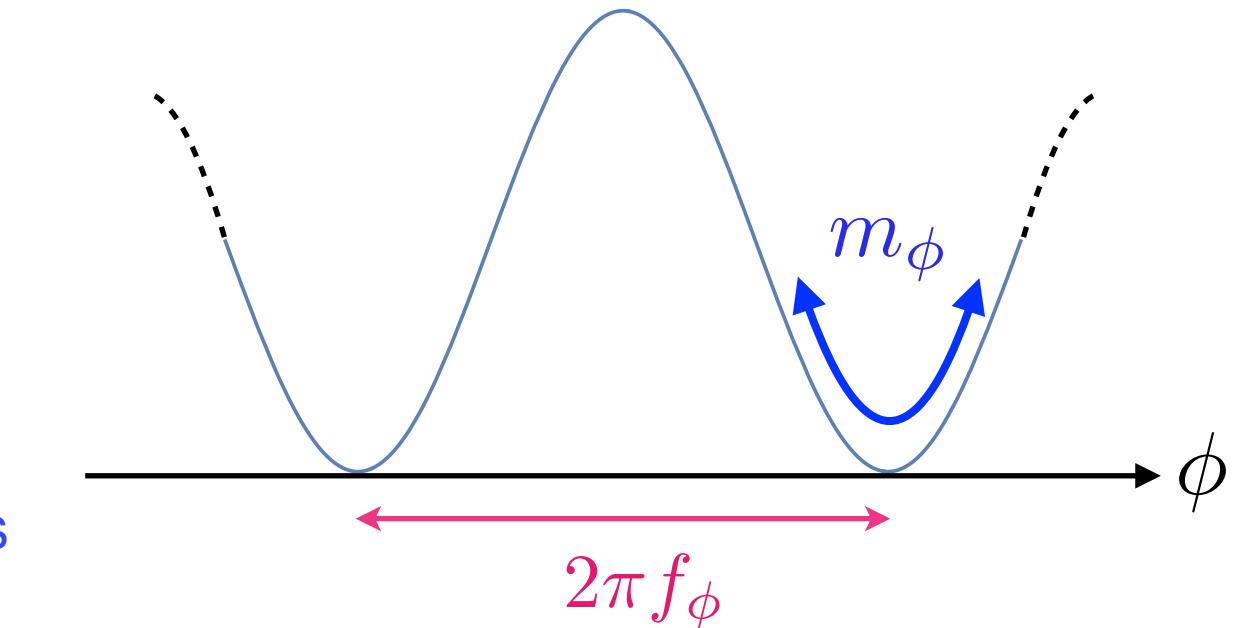


<https://physics.aps.org/articles/v13/s149>

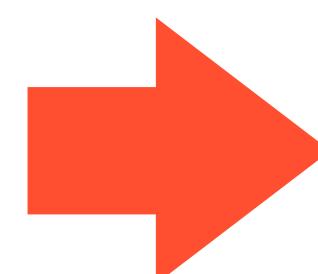
Implications of the hint for axion/ALP

Homogeneous ultralight axion with
mass $10^{-33}\text{eV} < m_\phi < 10^{-28}\text{eV}$?

cf. Carroll, astro-ph/9806099, Lue, et al astro-ph/9812088 for early works
[Fujita et al 2011.11894](#)



- Can it naturally explain the hinted isotropic CB?
- Why this particular masses?
- Is heavier or lighter axion possible?
- Any prediction for anisotropic CB?



(1) Axion domain walls

[2012.11576](#) with Wen Yin

(2) Axion coupled to DM

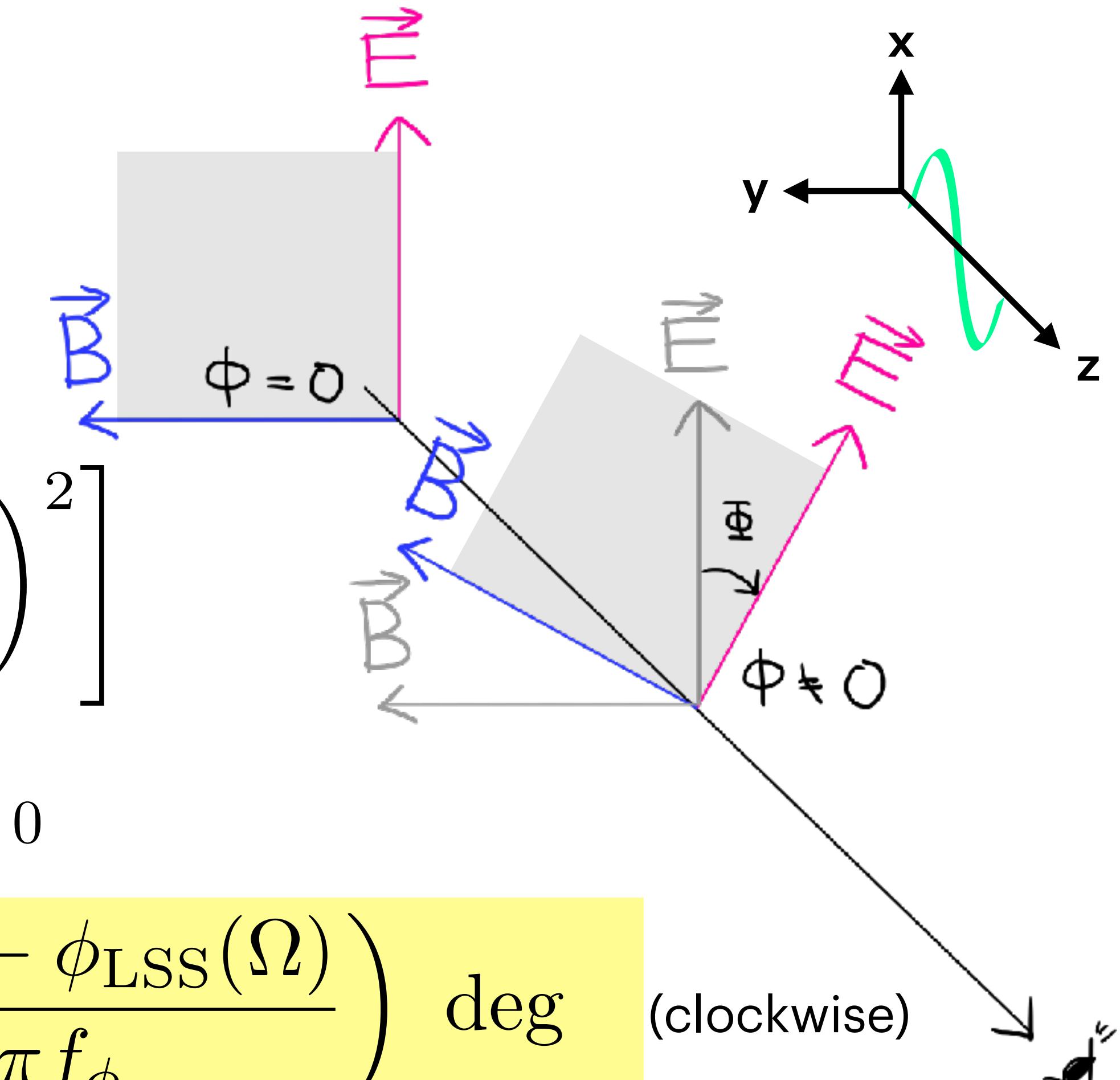
[2103.08153](#) with S.Nakagawa and M.Yamada

2. Cosmic birefringence

2. Cosmic birefringence

The axion dynamics rotates the polarization plane of linearly polarized light through the axion-photon coupling.

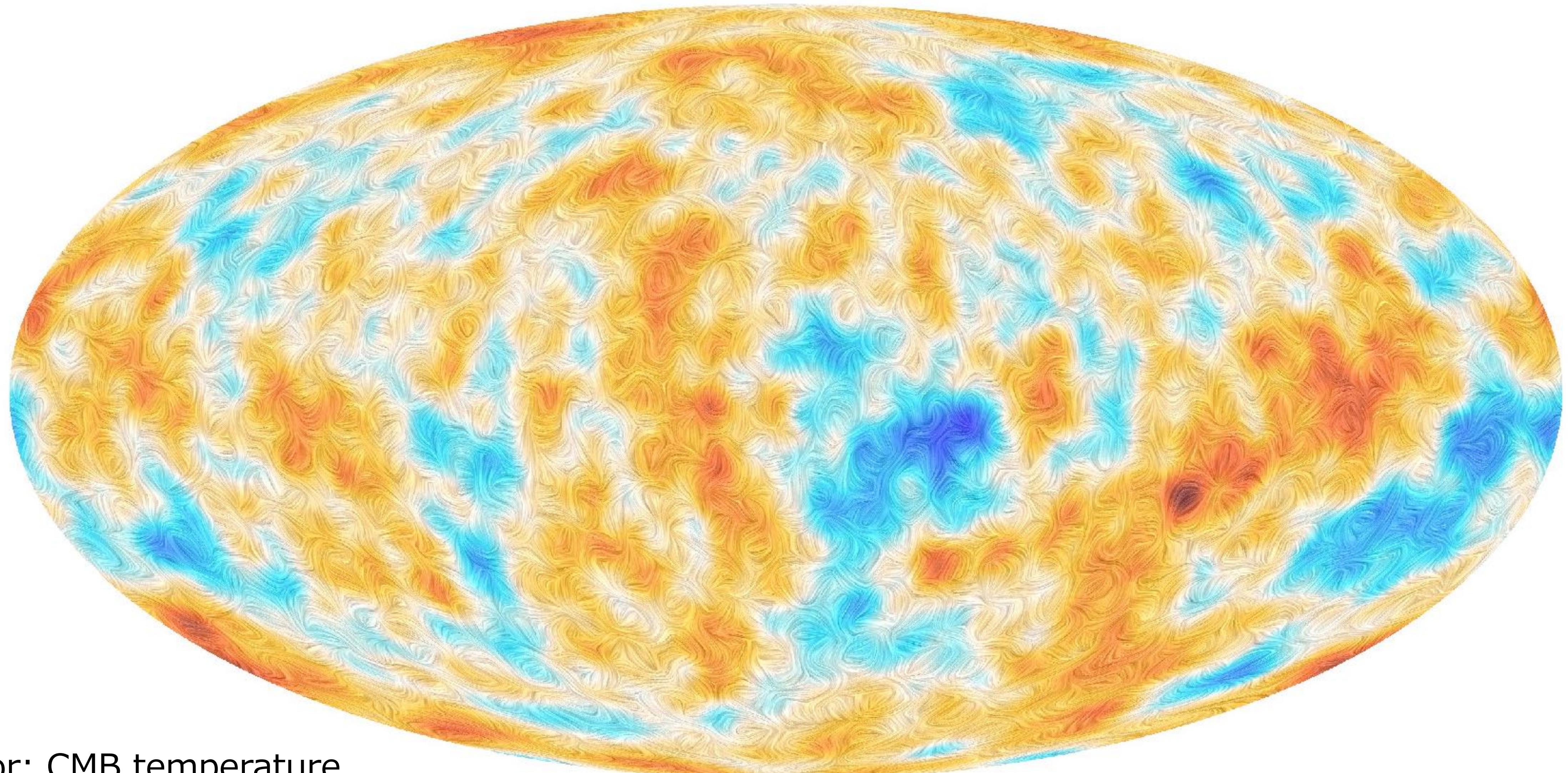
$$\begin{aligned}
 \mathcal{L} &= -\frac{1}{4}F_{\mu\nu}F^{\mu\nu} - \frac{1}{4}g_{\phi\gamma\gamma}\phi F_{\mu\nu}\tilde{F}^{\mu\nu}, \\
 &= \frac{1}{2}\left(\vec{E}^2 - \vec{B}^2\right) + g_{\phi\gamma\gamma}\phi\vec{E}\cdot\vec{B} \\
 &\approx \frac{1}{2}\left[\underbrace{\left(\vec{E} + \frac{g_{\phi\gamma\gamma}\phi}{2}\vec{B}\right)^2}_{\vec{E} \text{ when } \phi = 0} - \underbrace{\left(\vec{B} - \frac{g_{\phi\gamma\gamma}\phi}{2}\vec{E}\right)^2}_{\vec{B} \text{ when } \phi = 0}\right]
 \end{aligned}$$



Thus,

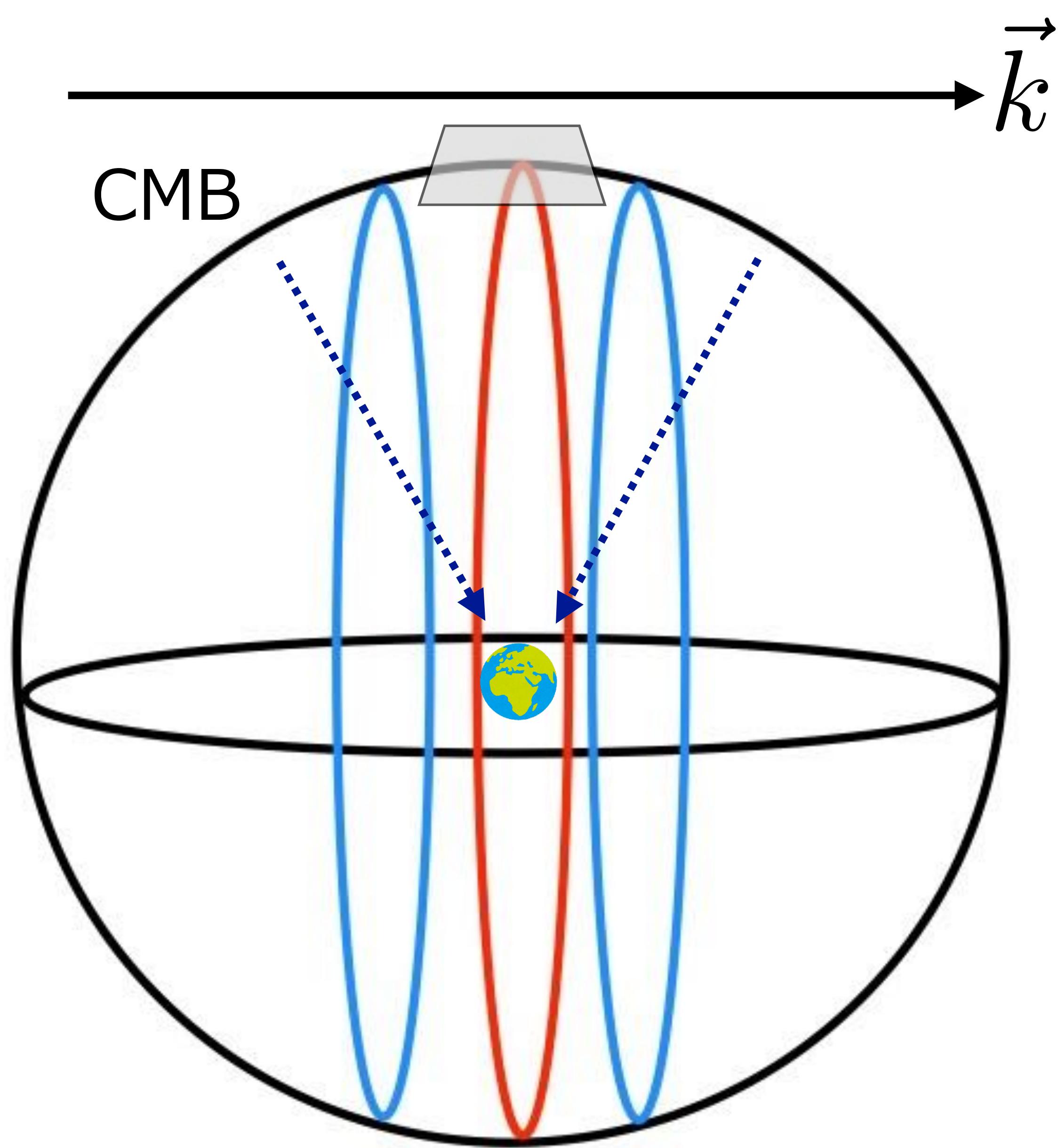
$$\Phi = \frac{g_{\phi\gamma\gamma}\Delta\phi}{2} \simeq 0.42c_\gamma \left(\frac{\phi_{\text{today}} - \phi_{\text{LSS}}(\Omega)}{2\pi f_\phi} \right) \text{ deg} \quad (\text{clockwise})$$

CMB photons are polarized (dominated by E-mode)

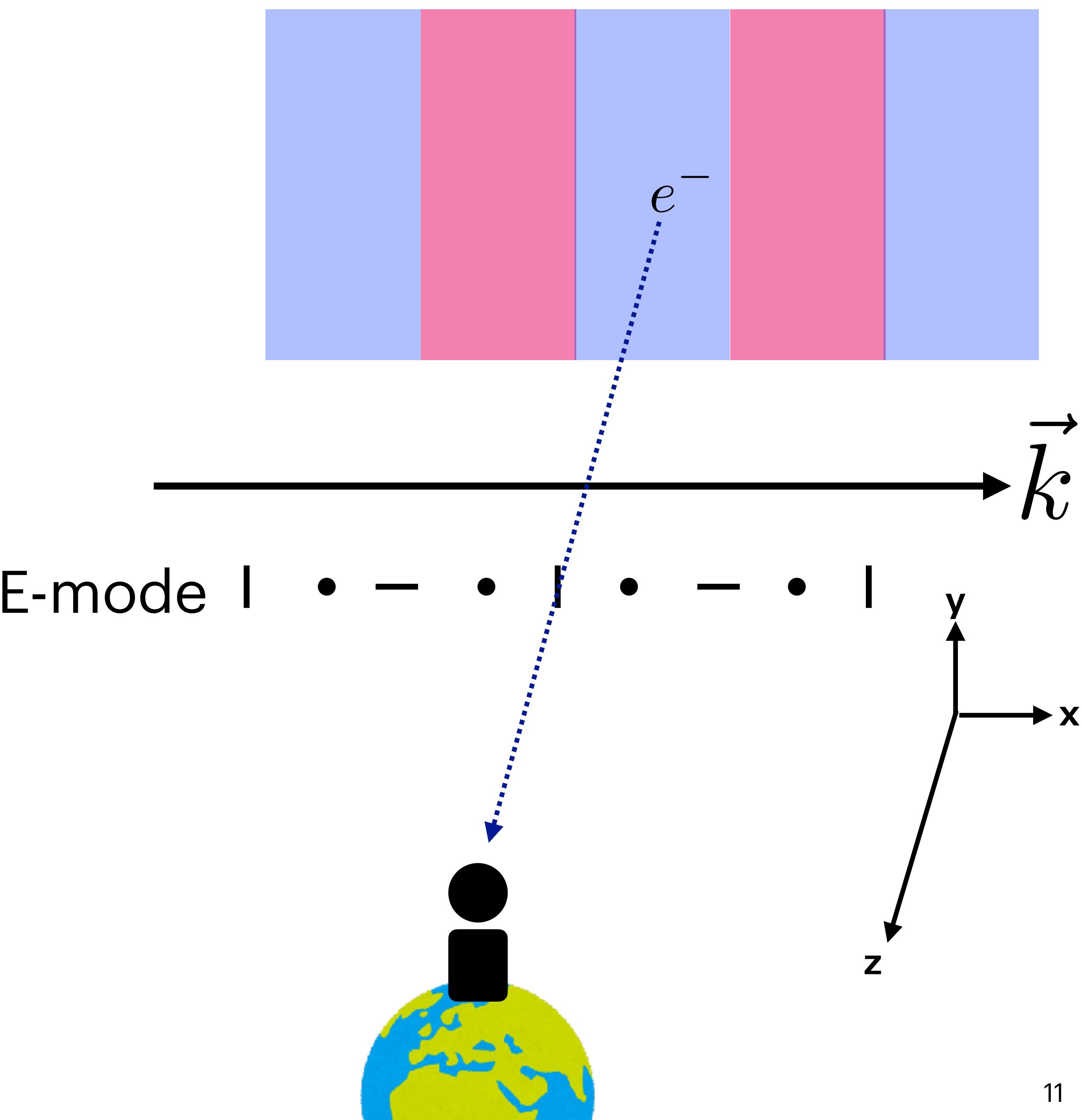


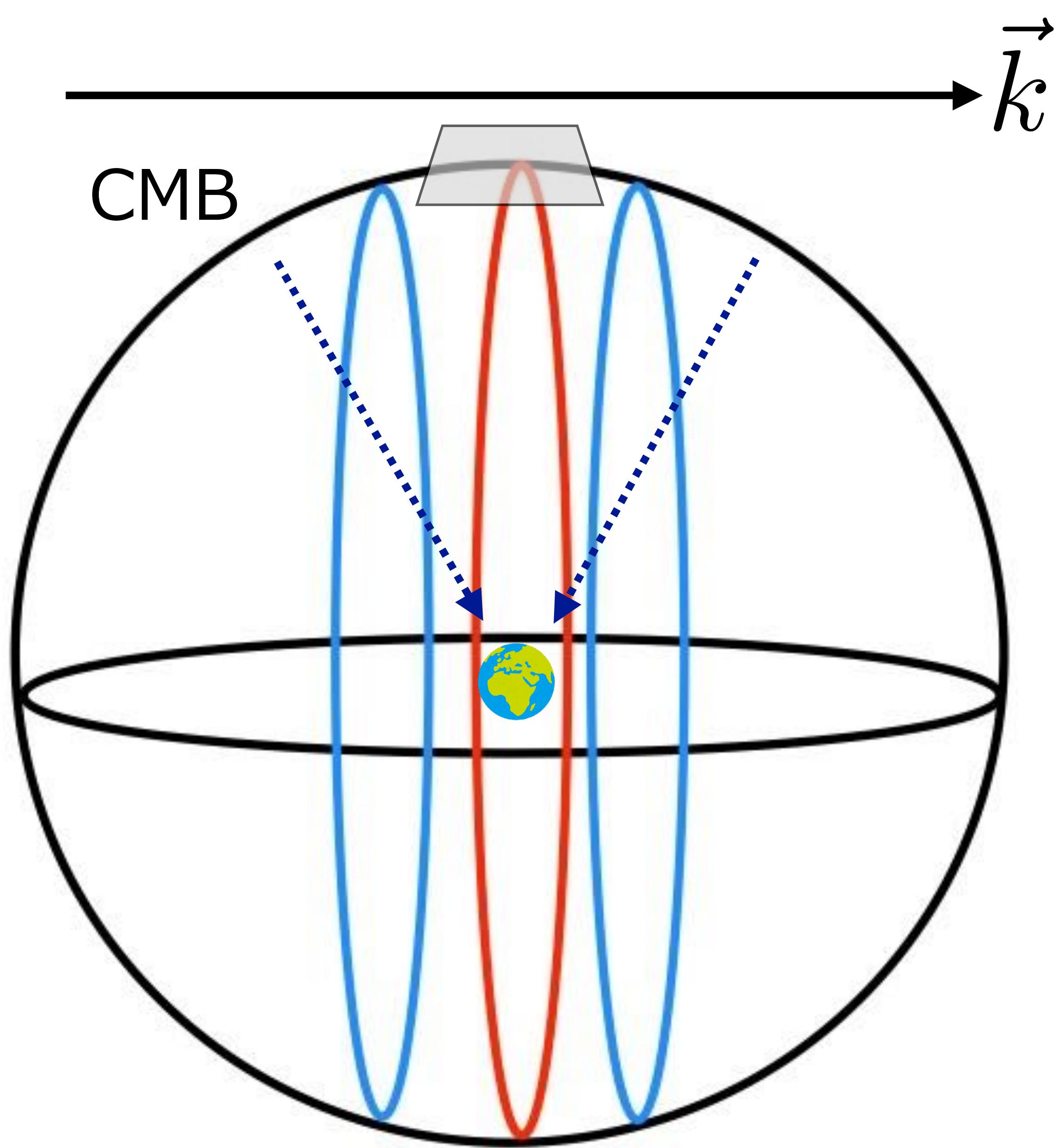
Color: CMB temperature

Texture: direction of polarization

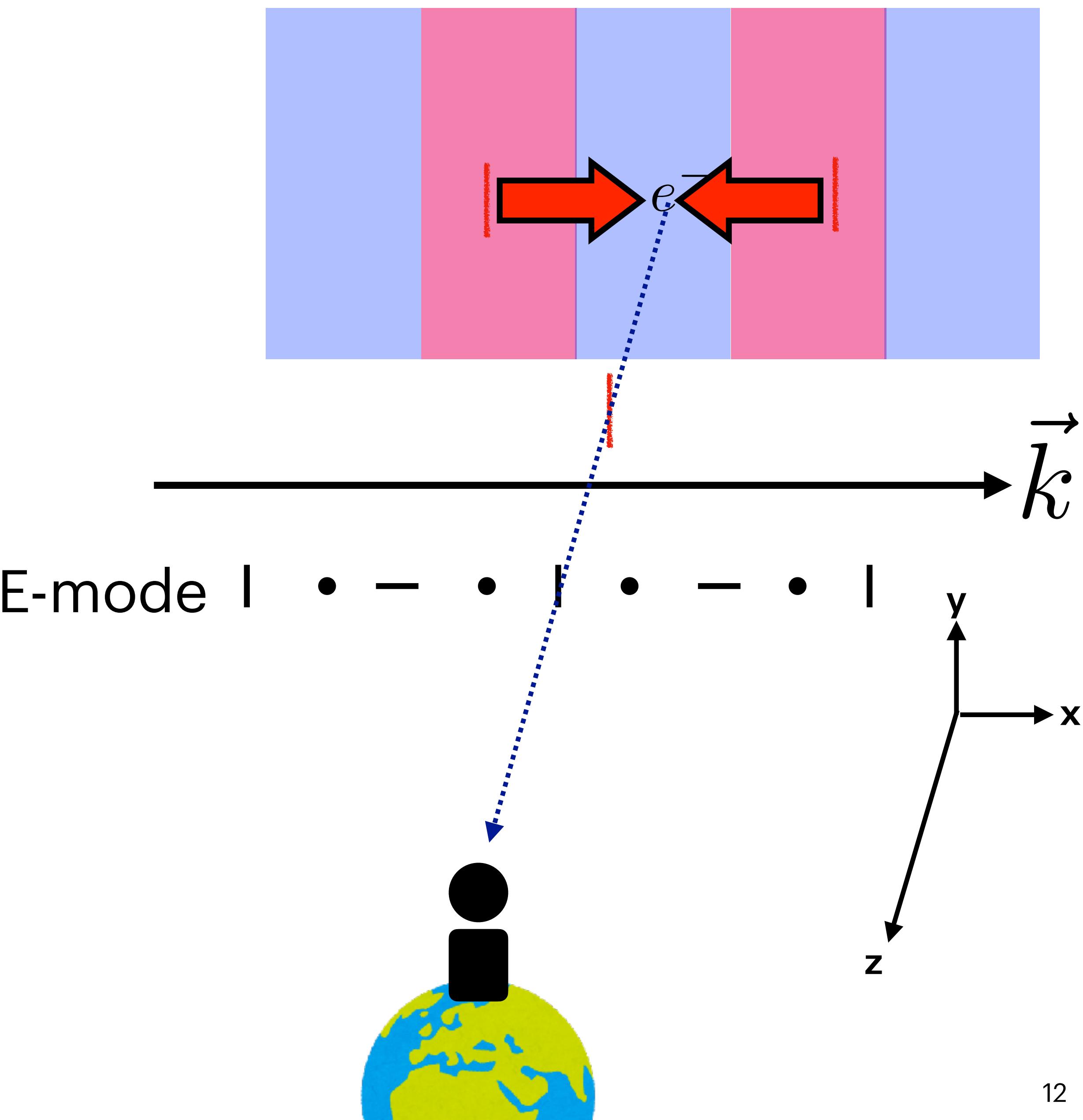


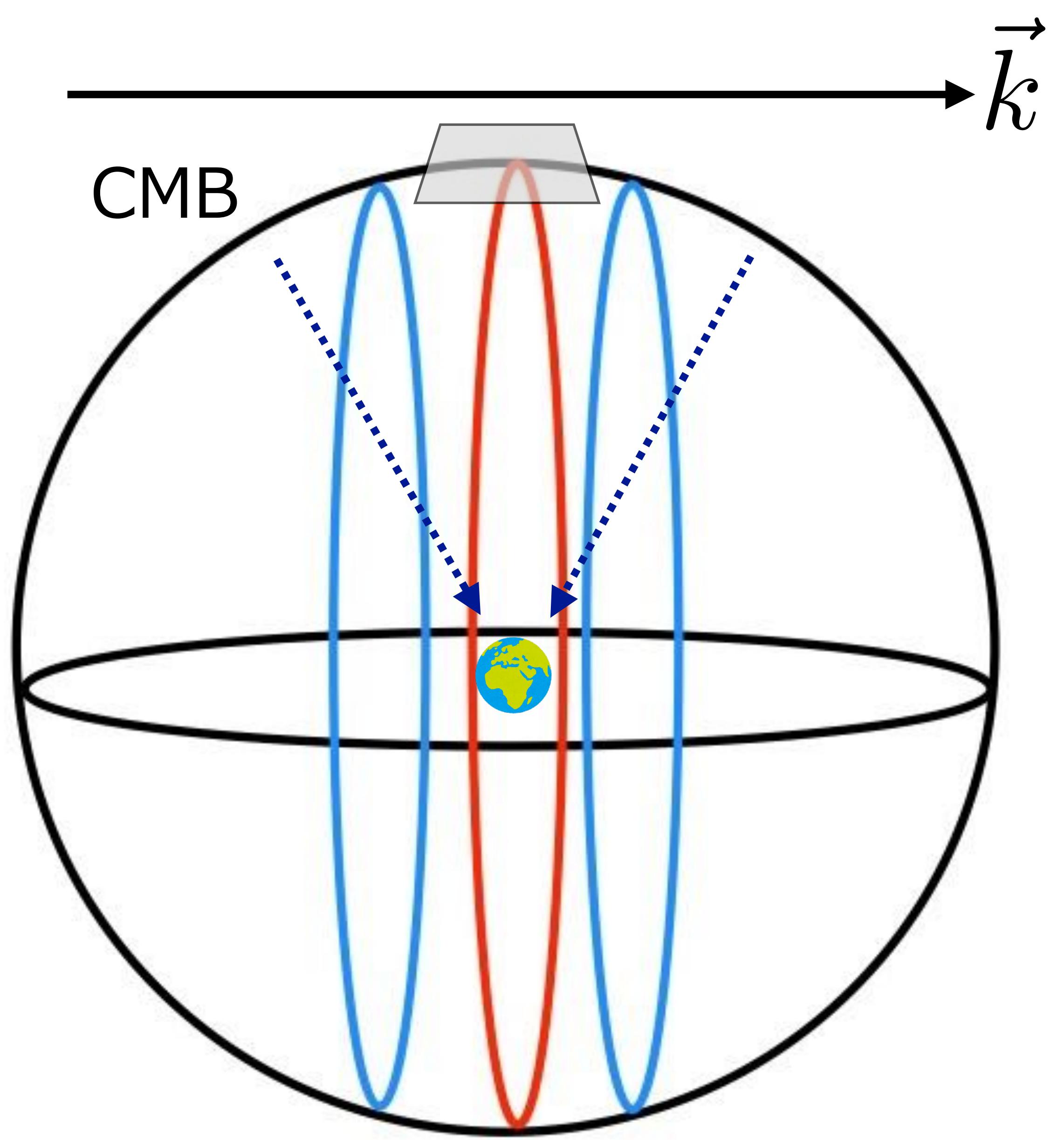
Last scattering surface (LSS)



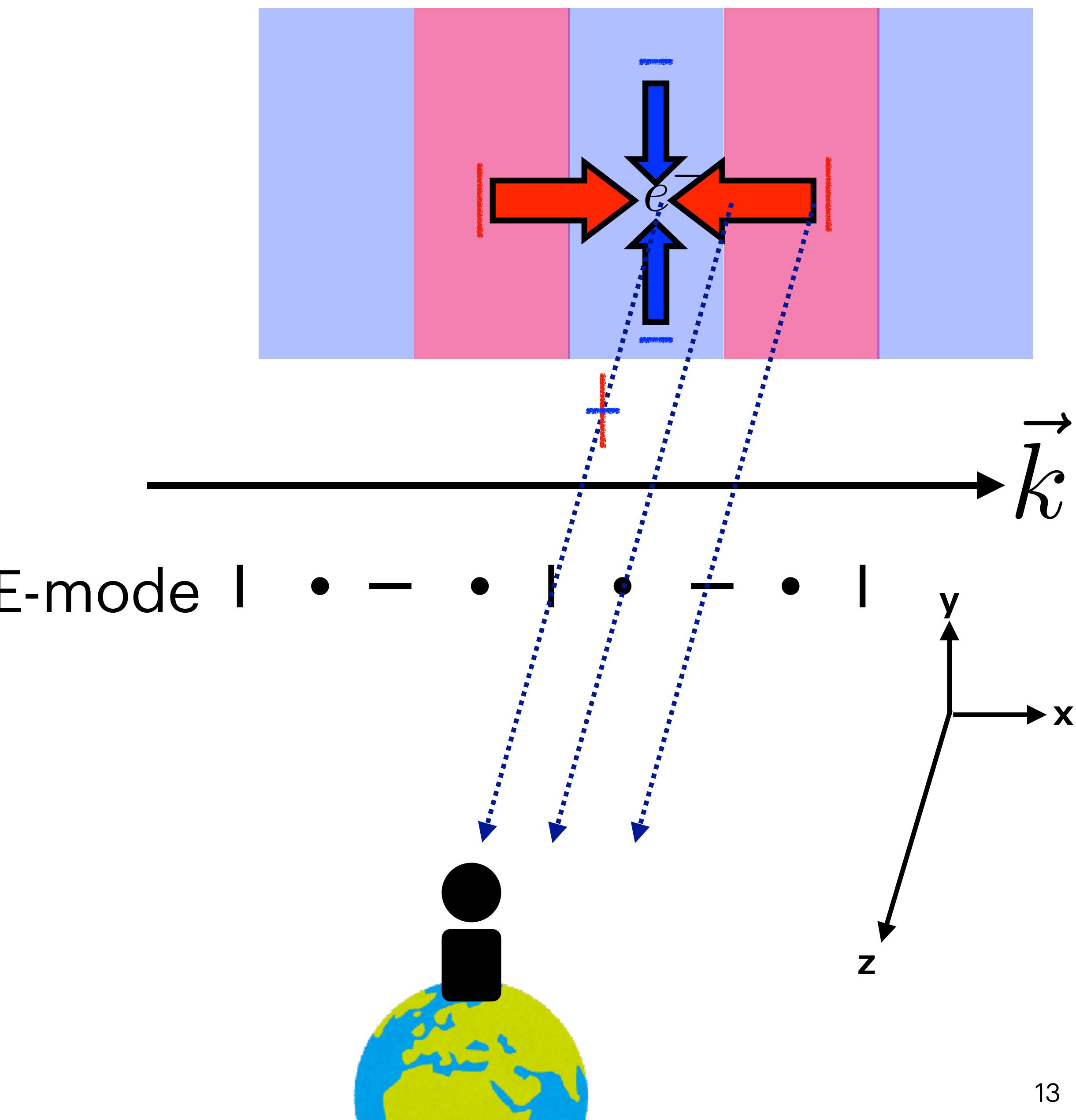


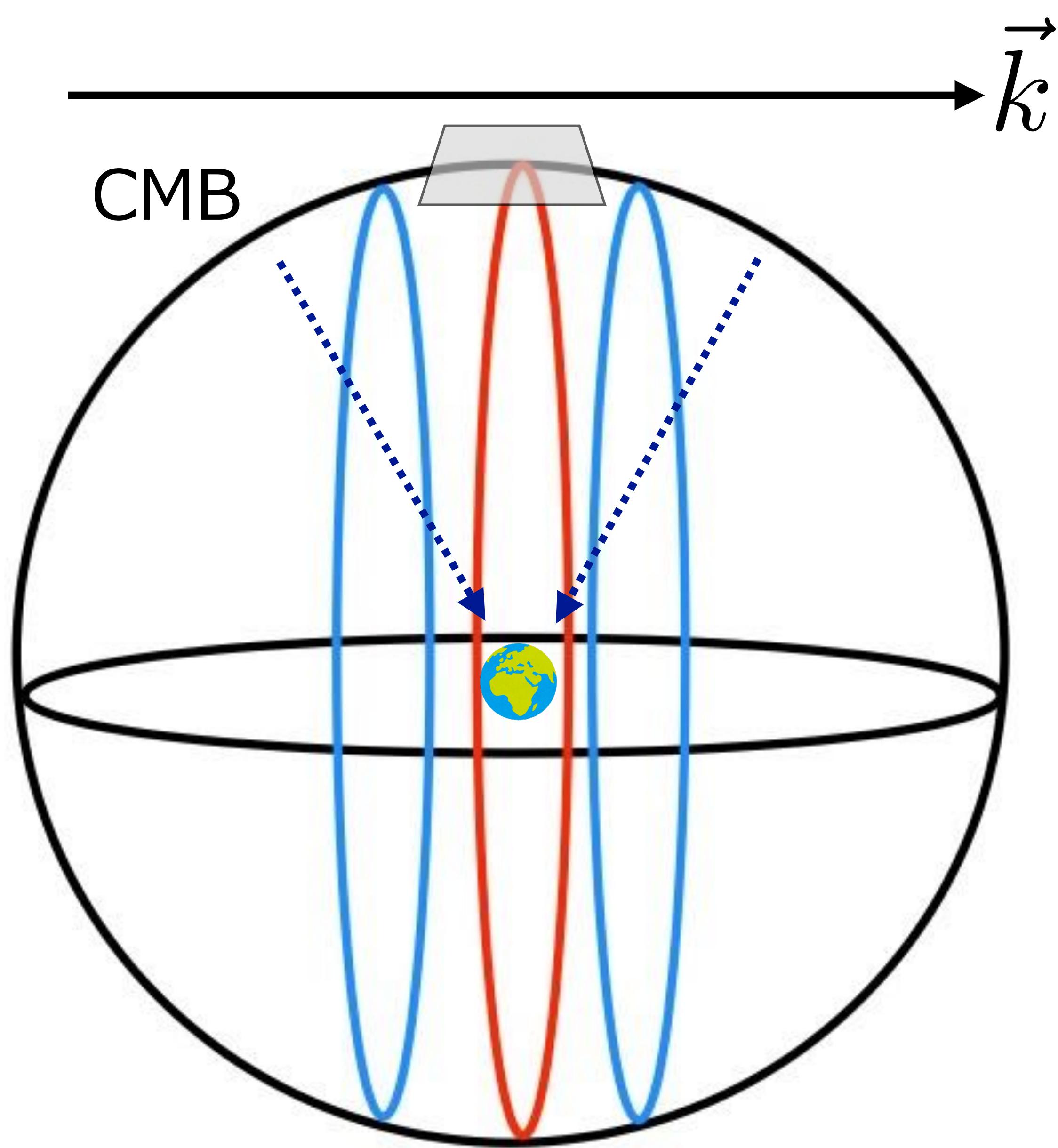
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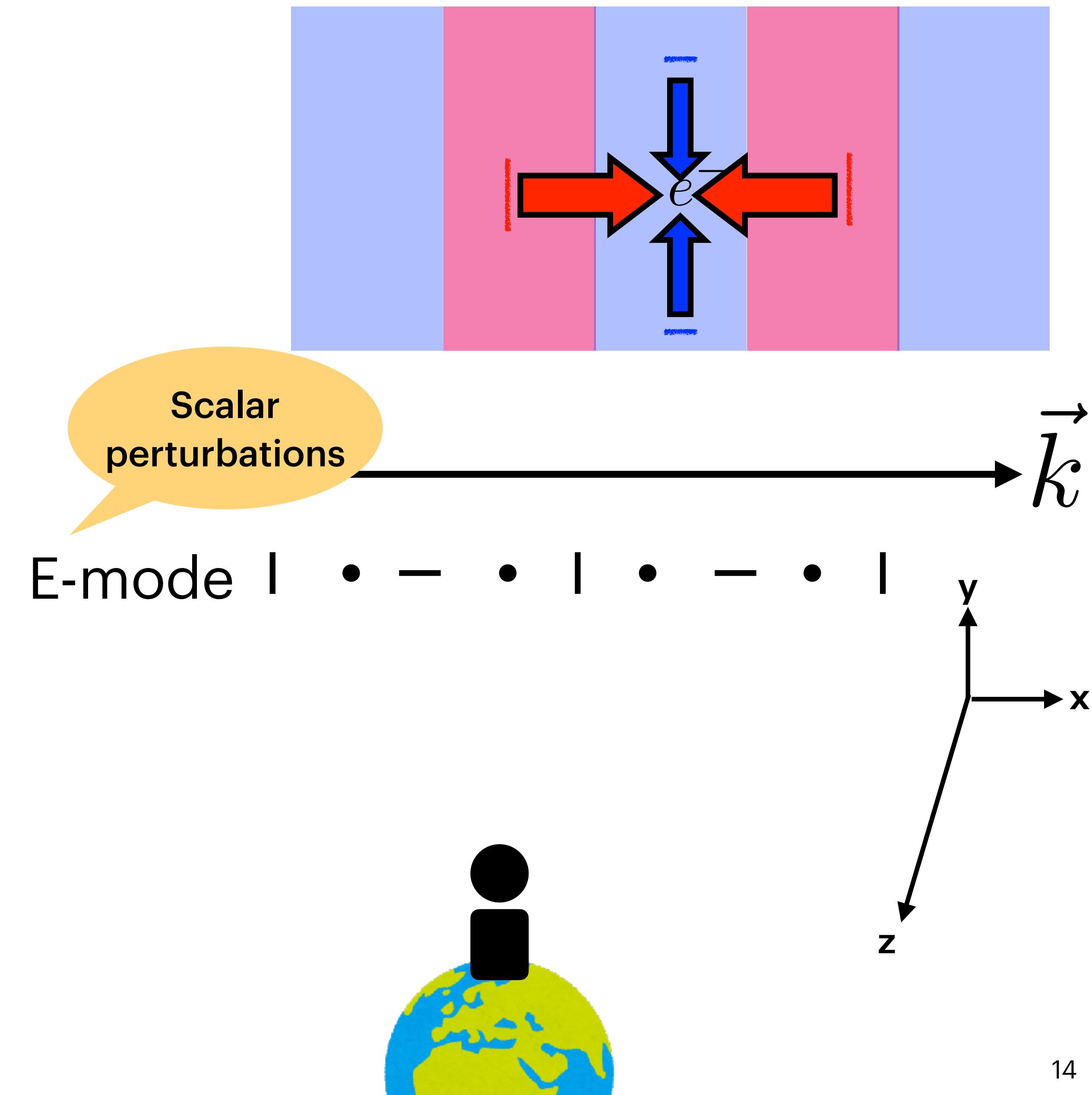


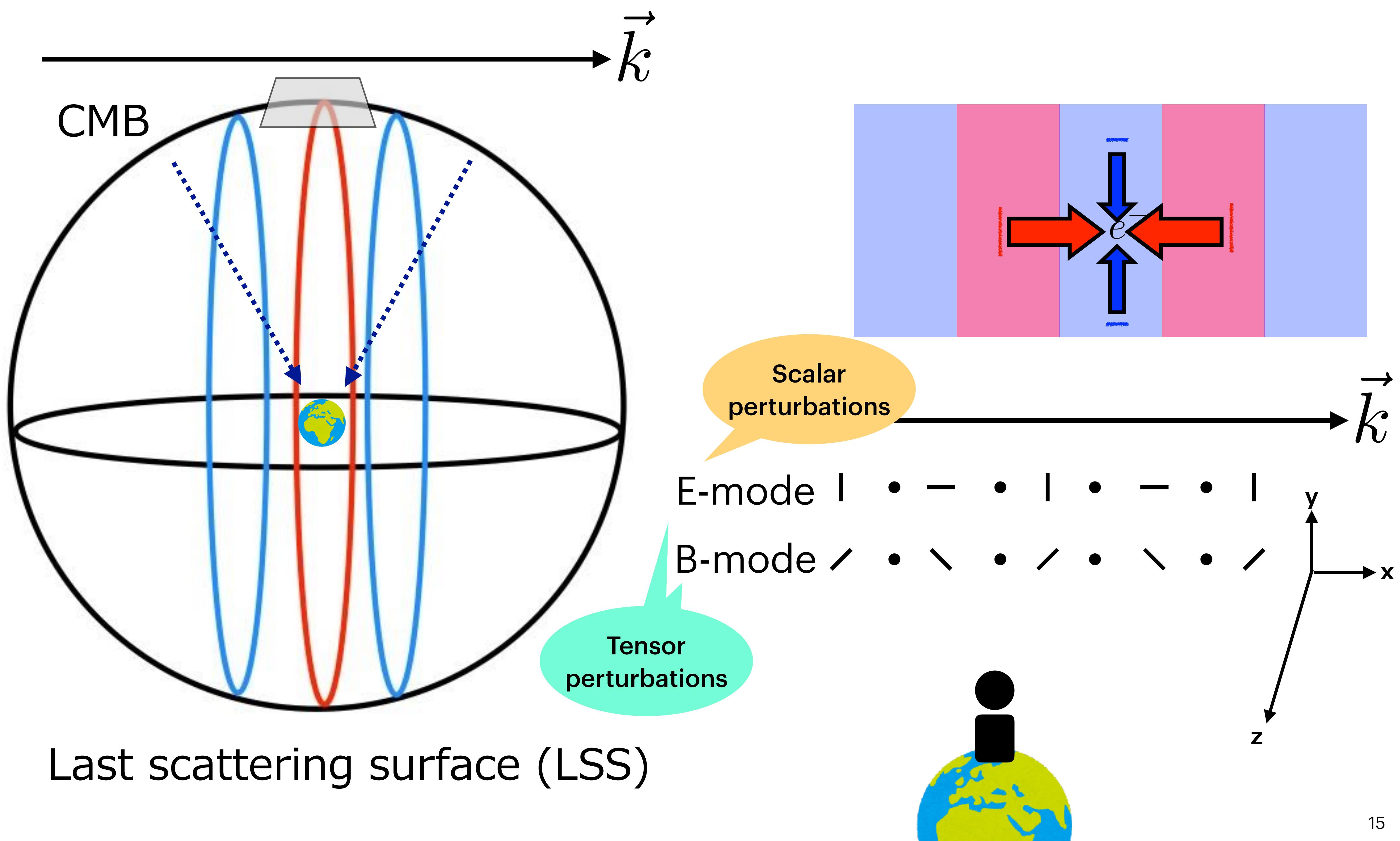
Last scattering surface (LSS)





Last scattering surface (LSS)



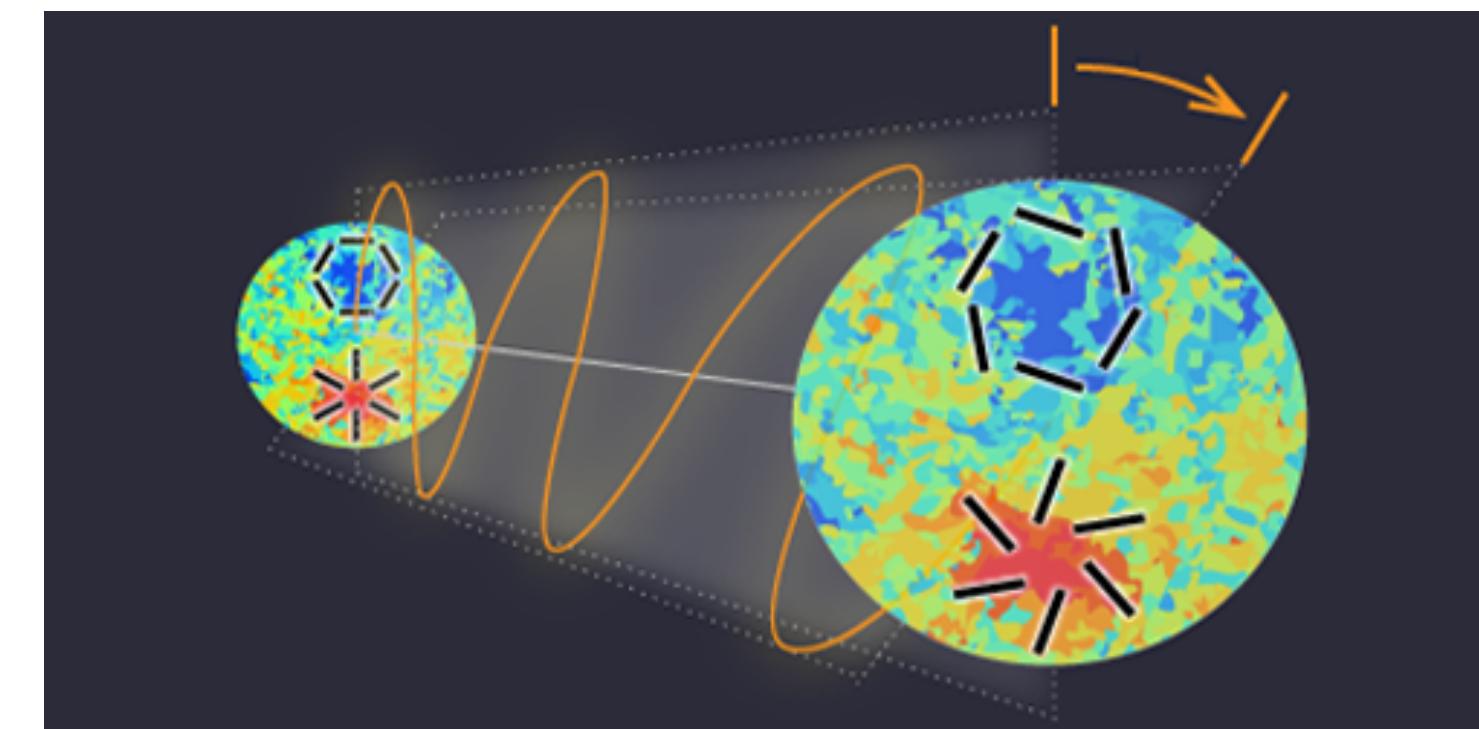


CMB constraints on the CB

Isotropic CB

$$\beta = \frac{1}{4\pi} \int d\Omega \Phi(\Omega) = 0.35 \pm 0.14 \text{ deg}$$

from Planck 18 pol. data



<https://physics.aps.org/articles/v13/s149>

Minami, Komatsu, Phys. Rev. Lett. **125**, 221301

based on a new method that uses both the CMB and Galactic foreground to distinguish between CB (β) and detector orientation miscalibration (α).

Minami et al, PTEP 2019 083E02 , Minami PTEP 2020 063E01, Minami and Komatsu PTEP 2020 103E02

cf. The reported isotropic CB in the past:

$$\alpha + \beta = \begin{cases} -0.36 \pm 1.24 \text{ deg} & \text{WMAP} \\ 0.31 \pm 0.05 \text{ deg} & \text{Planck} \\ -0.61 \pm 0.22 \text{ deg} & \text{POLARBEAR} \\ 0.63 \pm 0.04 \text{ deg} & \text{SPTpol} \\ 0.12 \pm 0.06 \text{ deg} & \text{ACT} \\ 0.09 \pm 0.09 \text{ deg} & \text{ACT} \end{cases}$$

$$\sigma_{\text{syst}}(\alpha) = \begin{cases} 1.5 \text{ deg} & \text{WMAP} \\ 0.28 \text{ deg} & \text{Planck} \end{cases}$$

CMB constraints on the CB

Anisotropic CB

$$\sqrt{\frac{L(L+1)C_L}{2\pi}} = \frac{g_{\phi\gamma\gamma}}{2} \frac{H_{\text{inf}}}{2\pi} < 0.18 \text{ deg} \quad (95\% \text{ CL})$$

for a scale-invariant CB; e.g. the axion fluctuation

$$\delta\phi = \frac{H_{\text{inf}}}{2\pi}$$

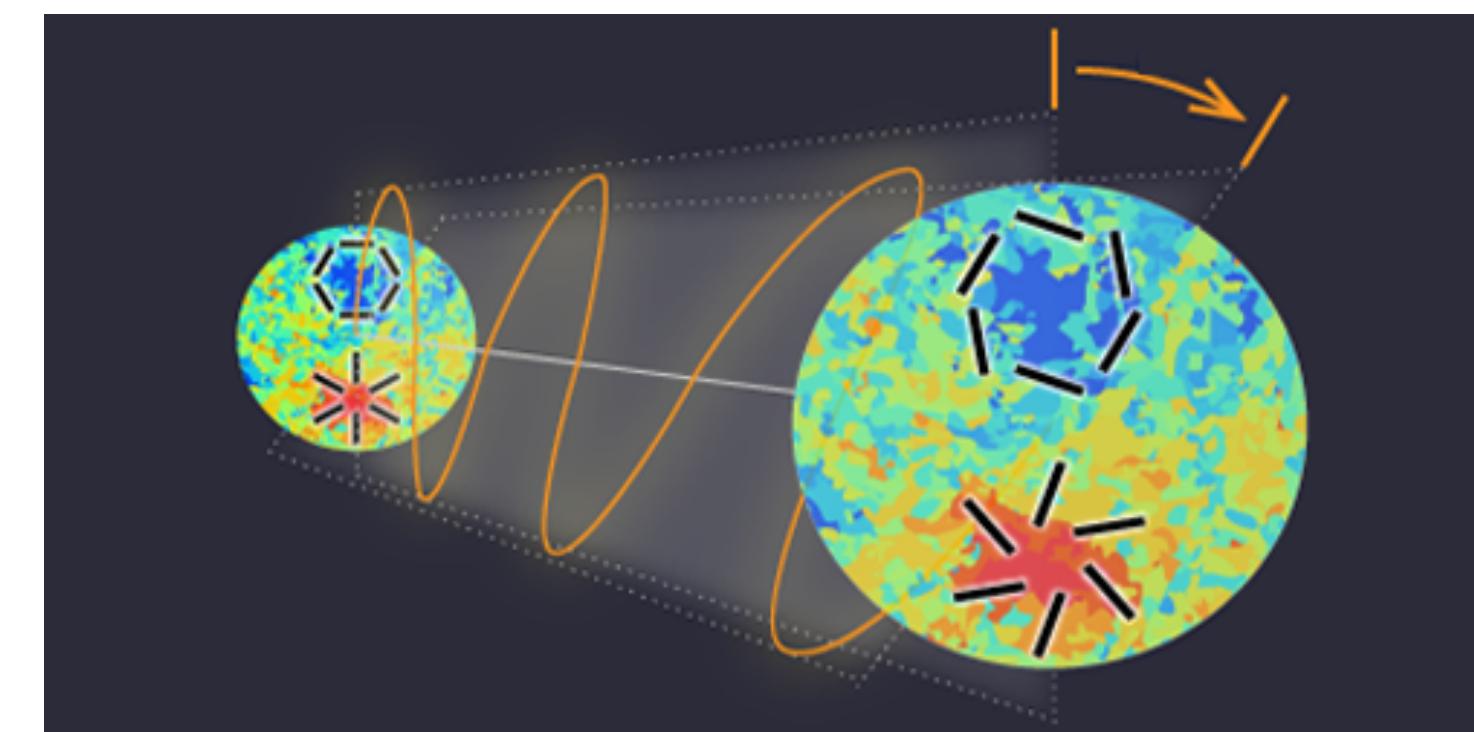
generated during inflation.

$$(\text{Recall } \Phi = \frac{g_{\phi\gamma\gamma}\Delta\phi}{2})$$

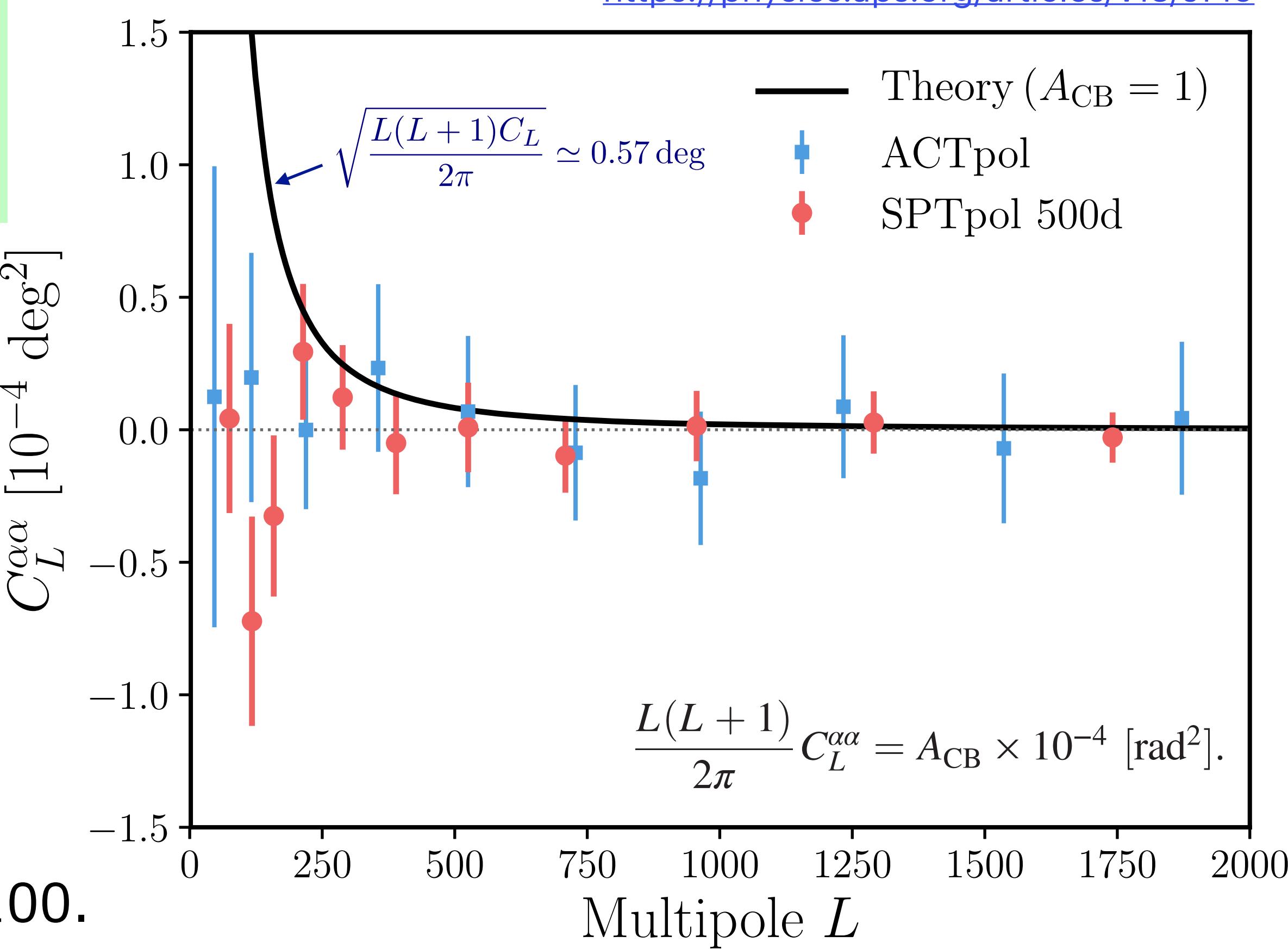
N.B. The limit mainly comes from low multipole $L < 100$.

The sensitivity will be improved by a factor of ~ 30 in the future CMB-S4

Pogosian et al, PRD 100, 023507 (2019)



<https://physics.aps.org/articles/v13/s149>



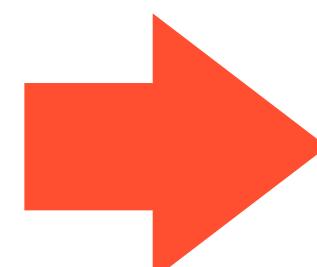
$$\frac{L(L+1)}{2\pi} C_L^{\alpha\alpha} = A_{\text{CB}} \times 10^{-4} [\text{rad}^2].$$

SPTpol, Phys.Rev.D 102 (2020) 8, 083504 (arXiv:2006.08061)

Implications for ALP

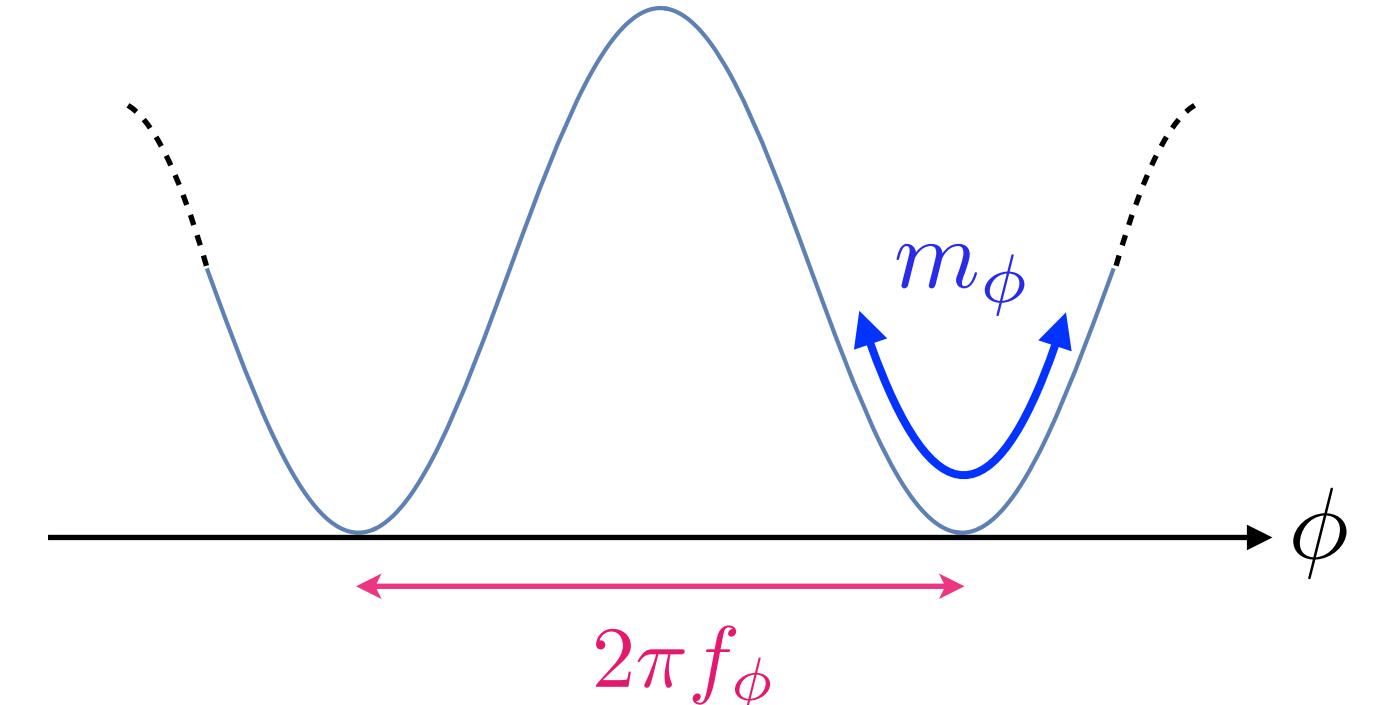
$$\mathcal{L}_{\phi\gamma} = -c_\gamma \frac{\alpha}{4\pi} \frac{\phi}{f_\phi} F_{\mu\nu} \tilde{F}^{\mu\nu} = -\frac{1}{4} g_{\phi\gamma\gamma} \phi F_{\mu\nu} \tilde{F}^{\mu\nu},$$

- The hint of the isotropic CB: $\beta = \frac{1}{4\pi} \int d\Omega \Phi(\Omega) = 0.35 \pm 0.14$ deg
- The ALP prediction: $\Phi(\Omega) \simeq 0.42 c_\gamma \left(\frac{\phi_{\text{today}} - \phi_{\text{LSS}}(\Omega)}{2\pi f_\phi} \right)$ deg



The ALP must have moved by $\Delta\phi = \mathcal{O}(\pi f_\phi)$ for $c_\gamma = O(1)$ after recombination

The interpretation in terms of a homogeneous ALP was studied in e.g. Fujita et al 2011.11894



Case of a homogeneous ALP

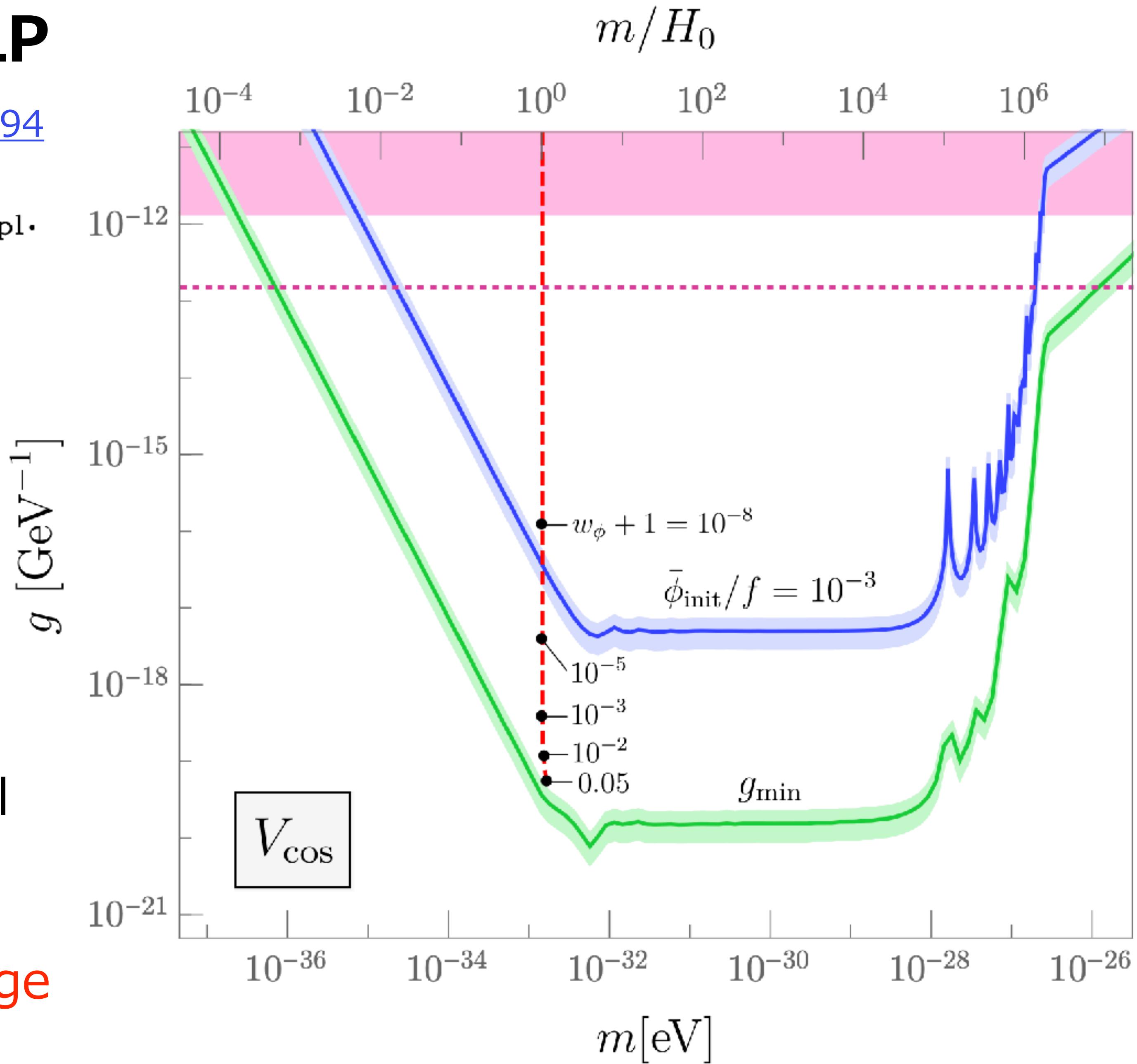
[Fujita et al 2011.11894](#)

$$V_{\cos}(\phi) = m^2 f^2 [1 - \cos(\phi/f)] \text{ with } f = M_{\text{pl}}.$$

In their setup, there are four free parameters:

- (1) mass m
- (2) decay constant $f \rightarrow$ fixed to be the Planck mass in the right figure.
- (3) axion-photon coupling g (or c_γ)
- (4) The ALP abundance Ω_ϕ (or initial misalignment angle)

Note that the interesting mass range is $10^{-33} \sim 10^{-28}$ eV.



3. Scenario 1: Axion Domain Walls

ALP domain walls without strings

Let us consider the axion potential

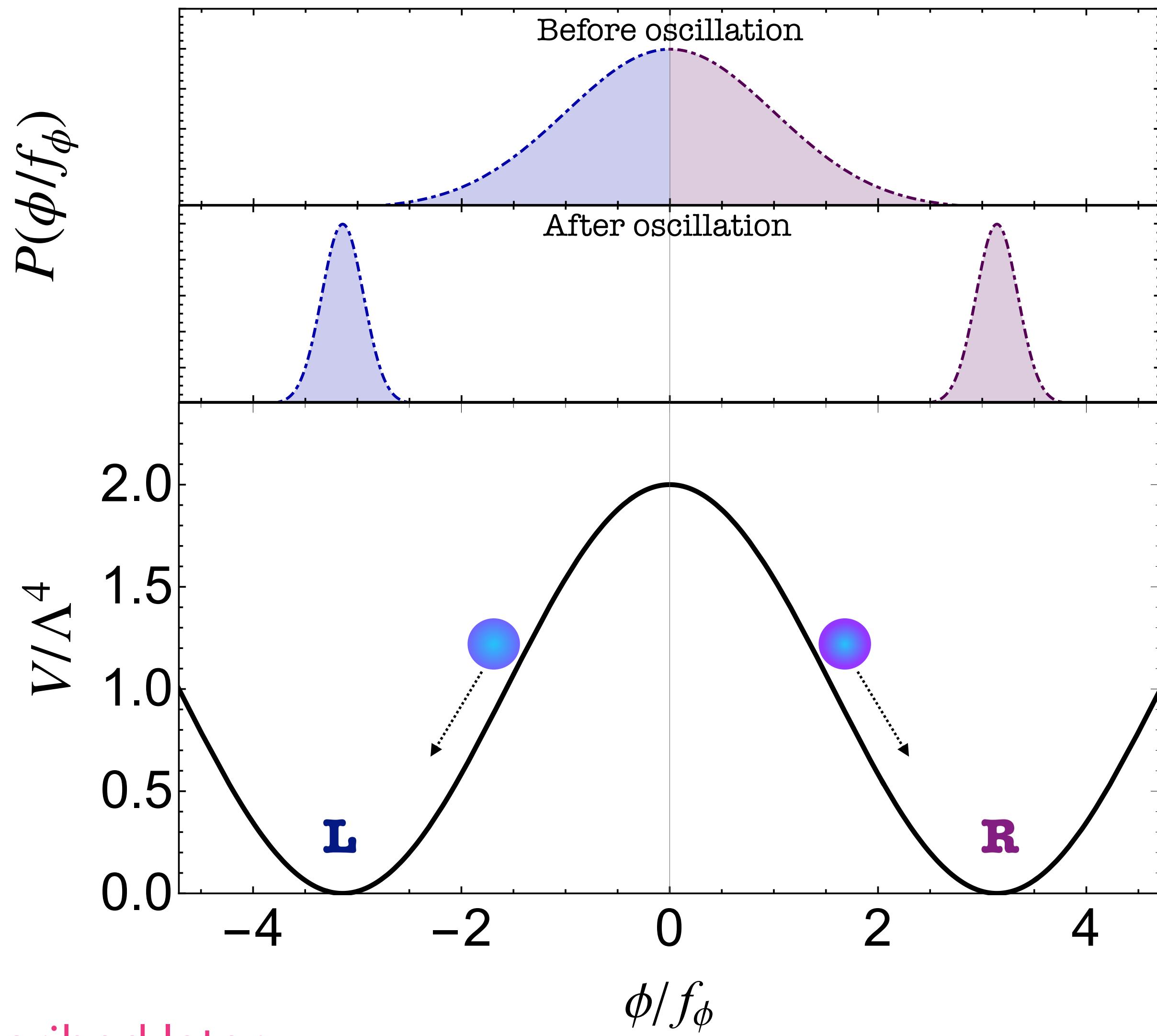
$$V(\phi) = m_\phi^2 f_\phi^2 \left(1 + \cos \frac{\phi}{f_\phi}\right)$$

and focus on the adjacent minima,

$$\phi_L = -\pi f_\phi \text{ and } \phi_R = +\pi f_\phi.$$

If both vacua are populated in the early Universe with $0.3 \lesssim p_L \lesssim 0.7$, infinite domain wall (w/o strings) will appear when $H \sim m_\phi \gtrsim H_{\text{LSS}}$.

Specific scenarios to obtain $\delta\theta = O(1)$ will be described later.



ALP domain walls without strings

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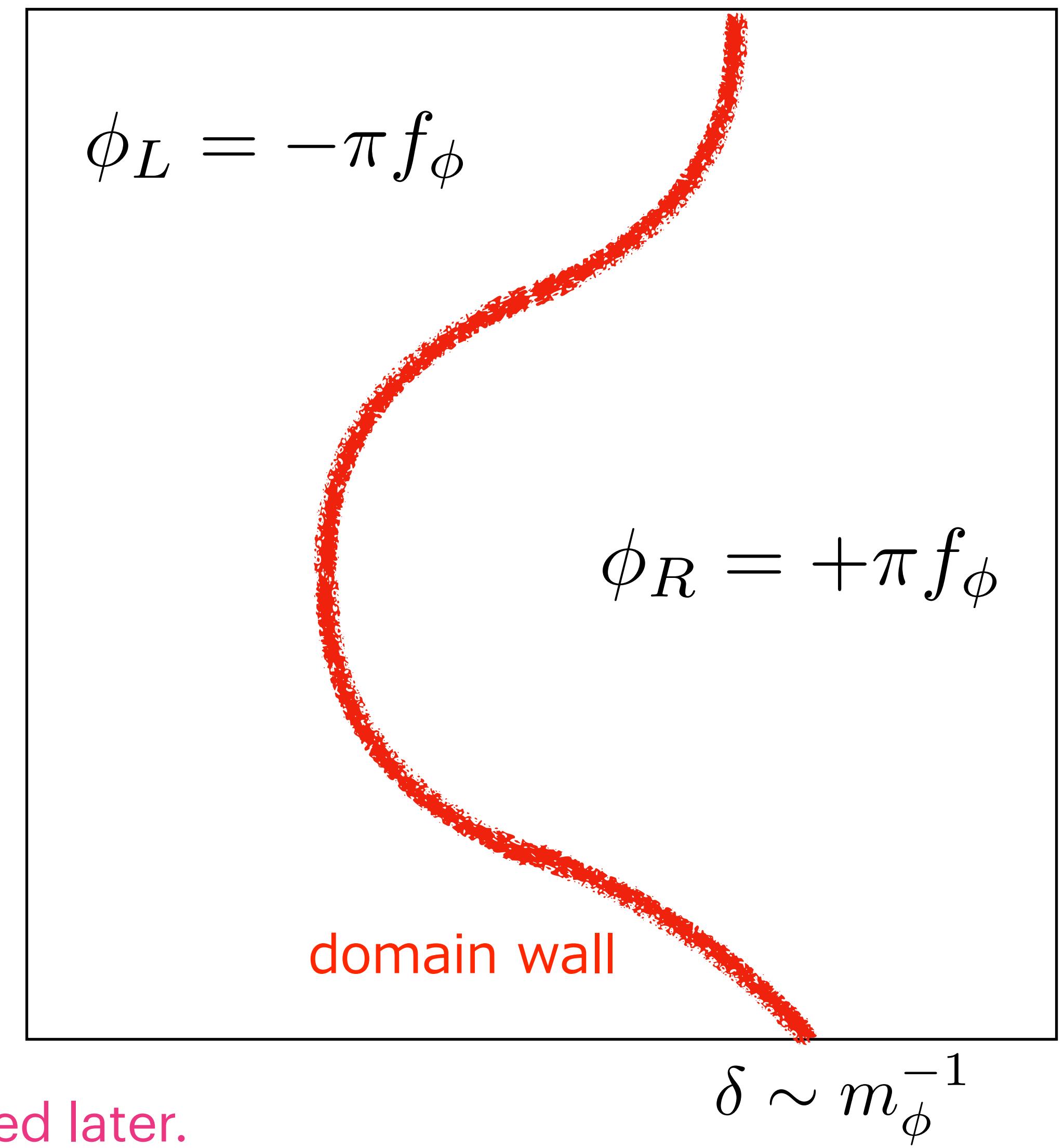
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Scaling solution of domain walls

Press, Ryden, Spergel '89

The scaling solution is such that the Hubble horizon contains on average about one wall:

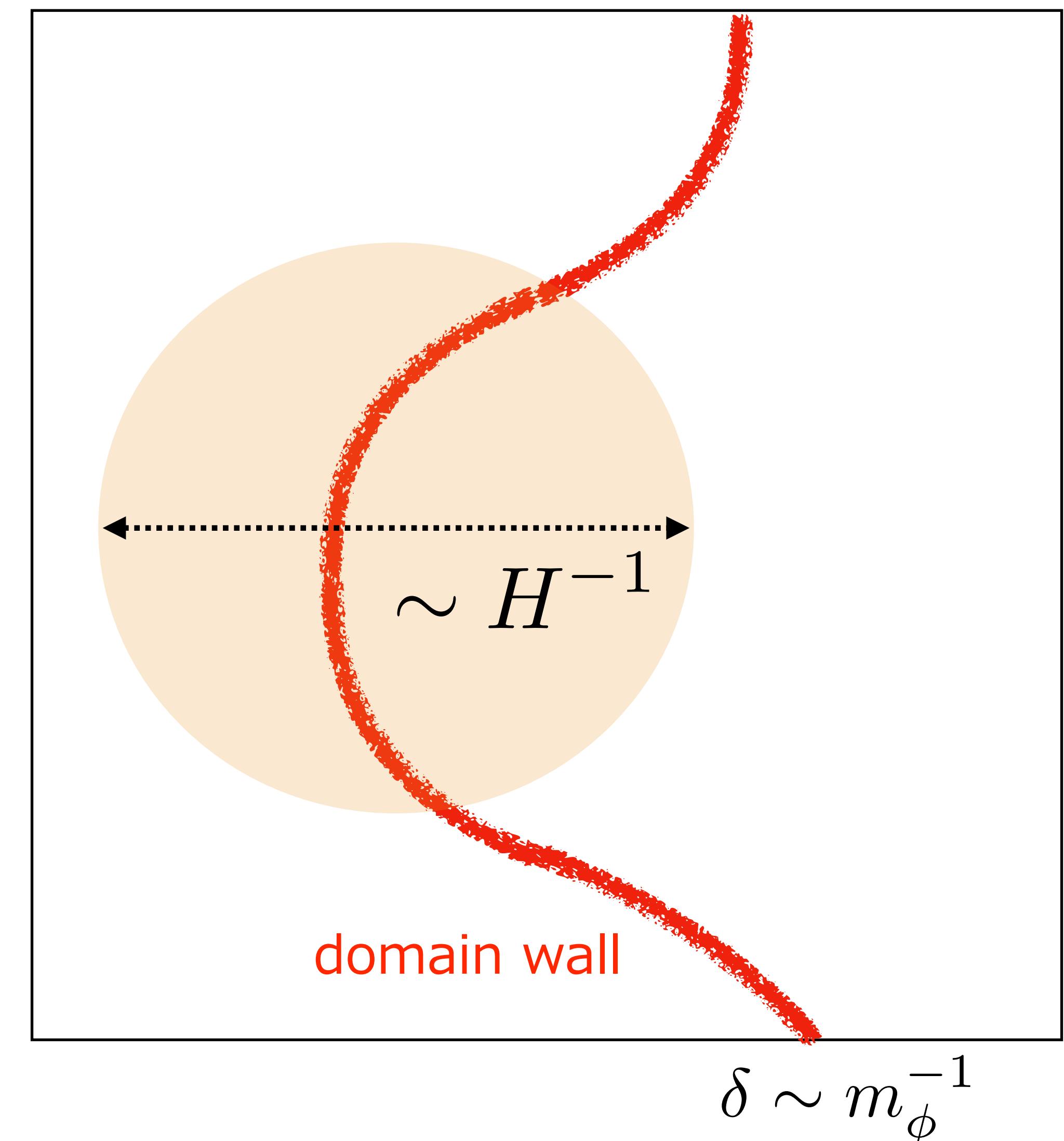
$$\rho_{\text{DW}} \sim \frac{\sigma_{\text{DW}} H^{-2}}{H^{-3}} \sim m_\phi f_\phi^2 H$$

$$\sigma_{\text{DW}} \simeq 8m_\phi f_\phi^2$$

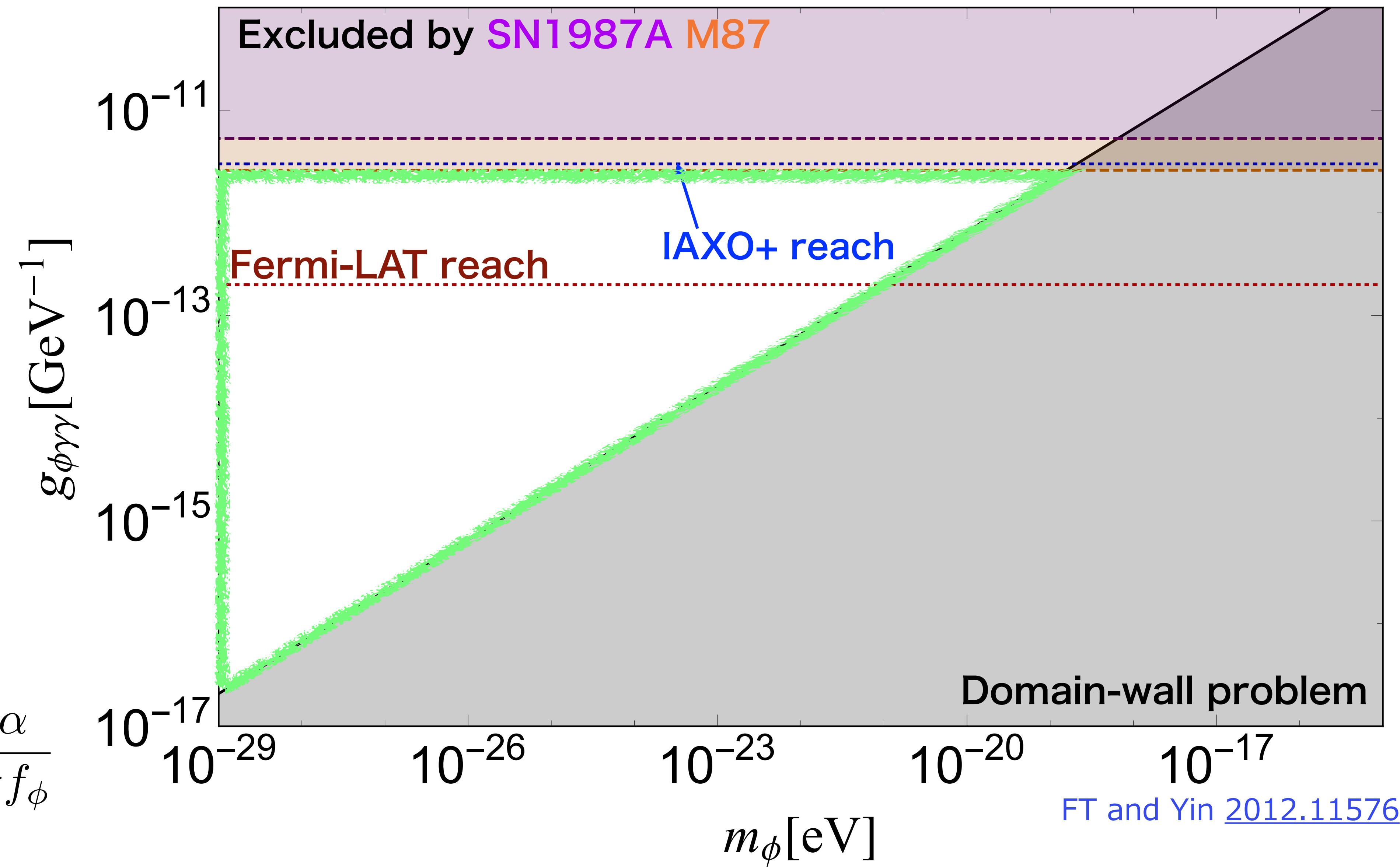
tension of DW for the cosine potential

which decreases more slowly than matter, and there is a CMB bound on stable domain walls,

$$\sigma_{\text{DW}} \lesssim (1 \text{ MeV})^3$$

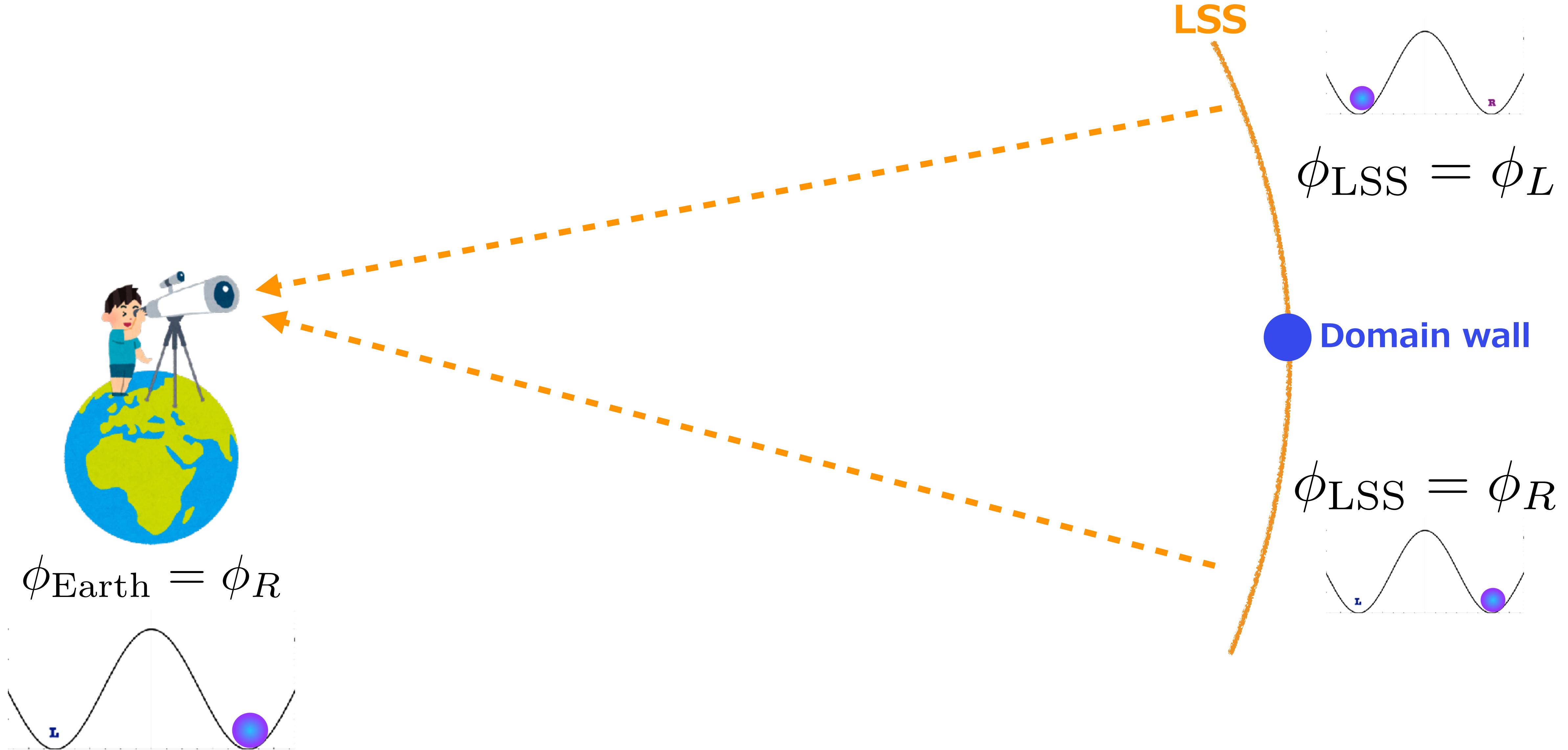


Various bounds and future sensitivity reach

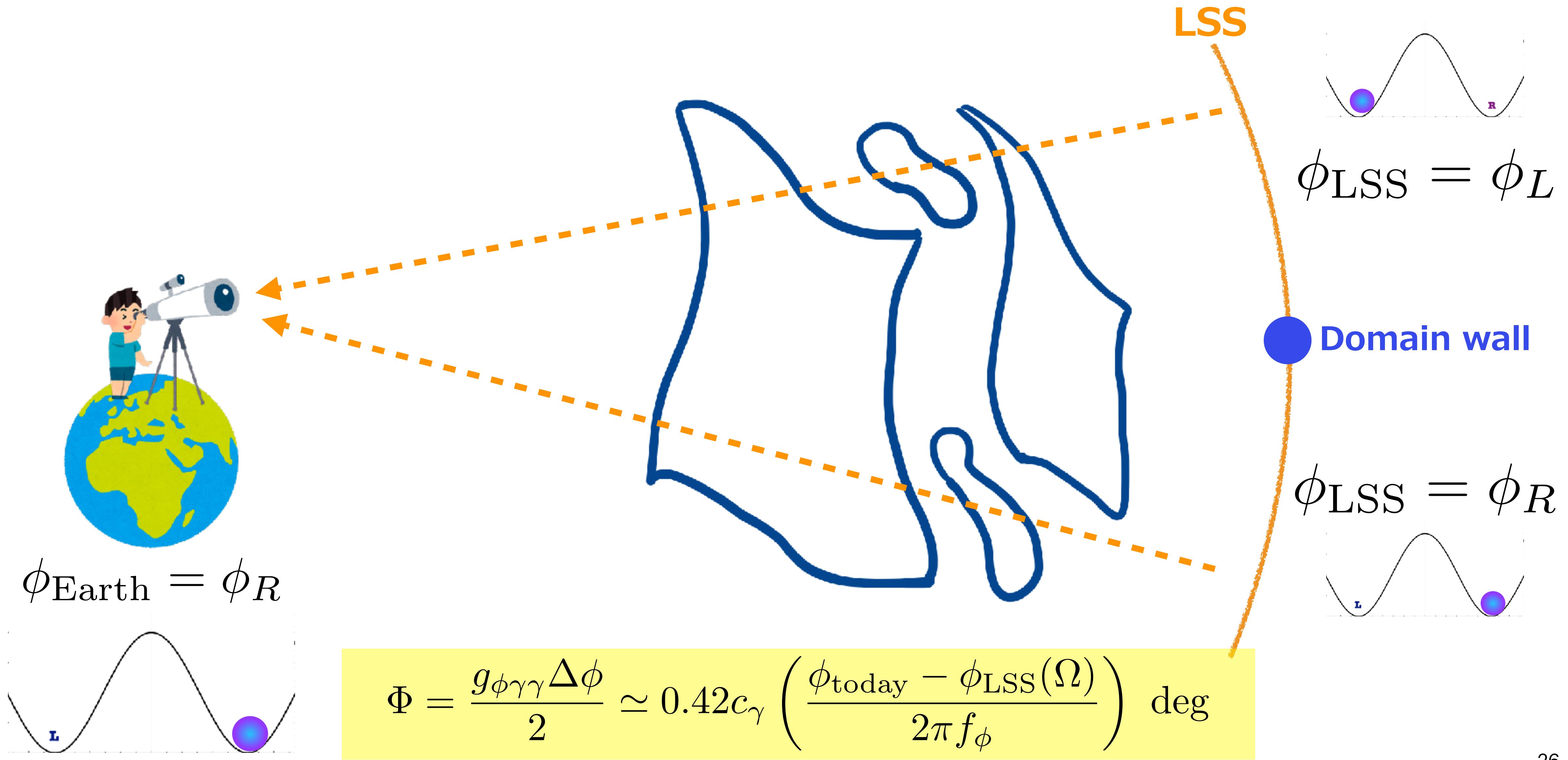


Note that the mass is heavier than $\sim 10^{-29}$ eV $\simeq H_{\text{LSS}}$ 24

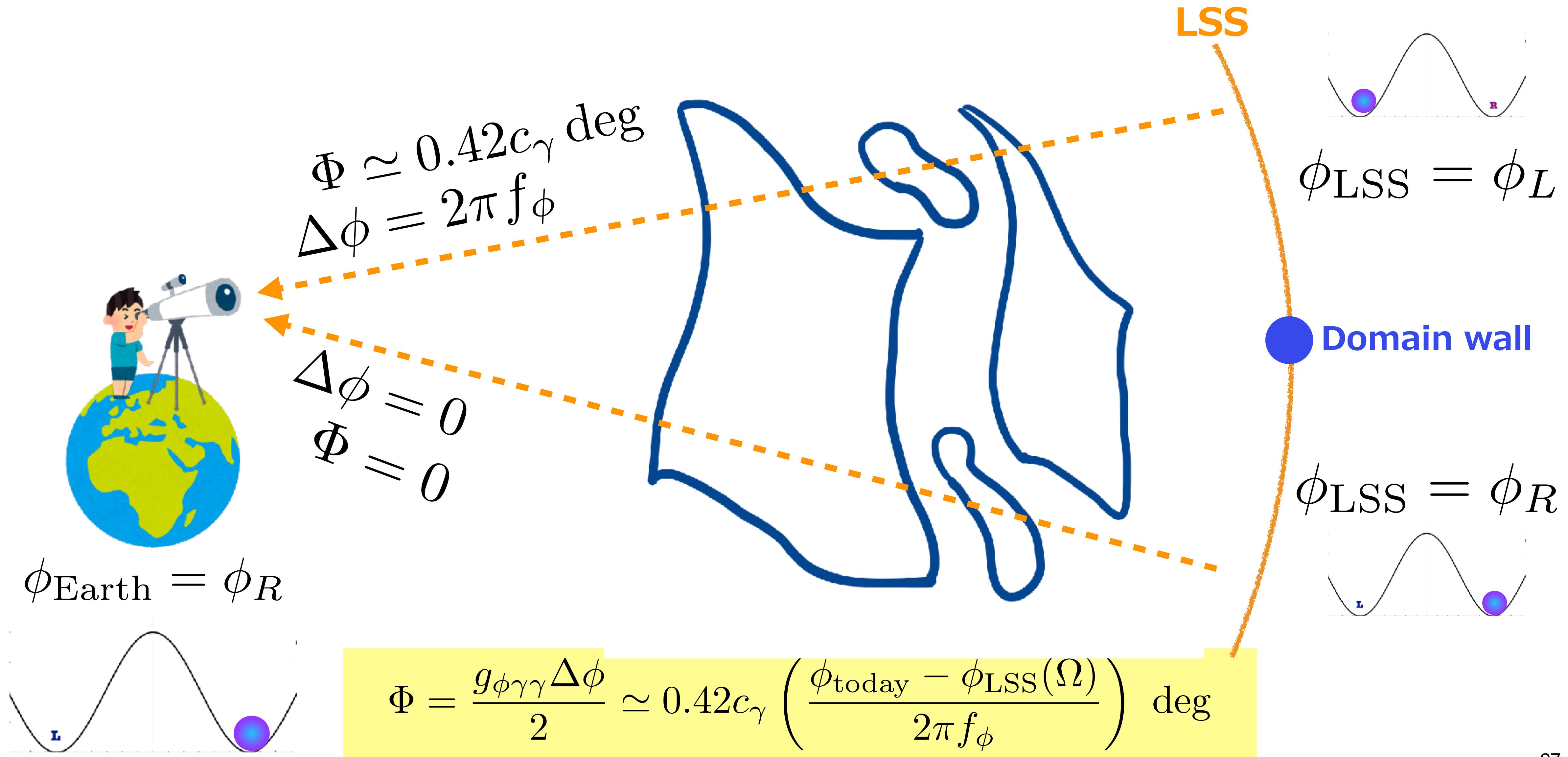
KiloByte CB from ALP domain walls



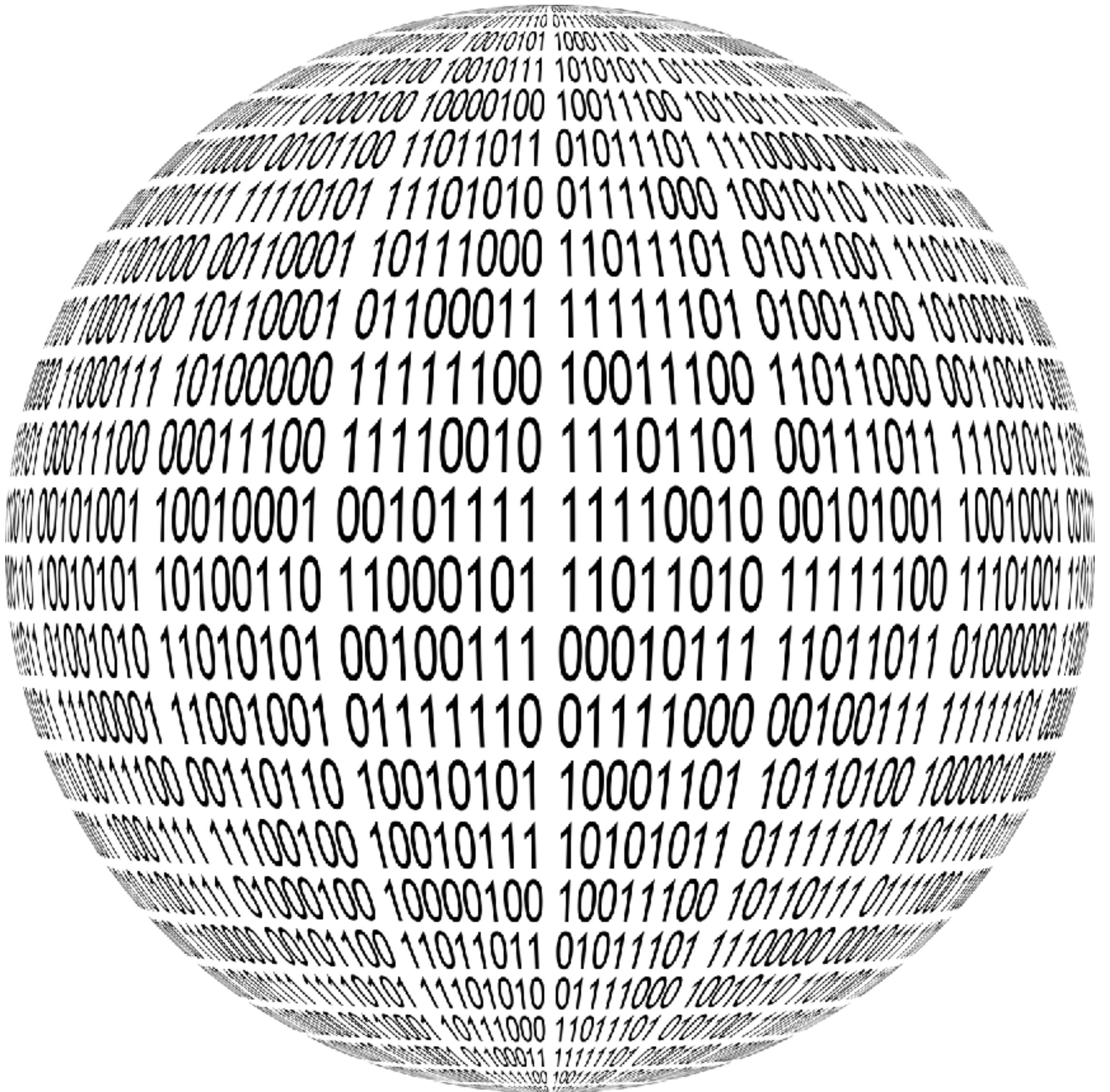
KiloByte CB from ALP domain walls



KiloByte CB from ALP domain walls



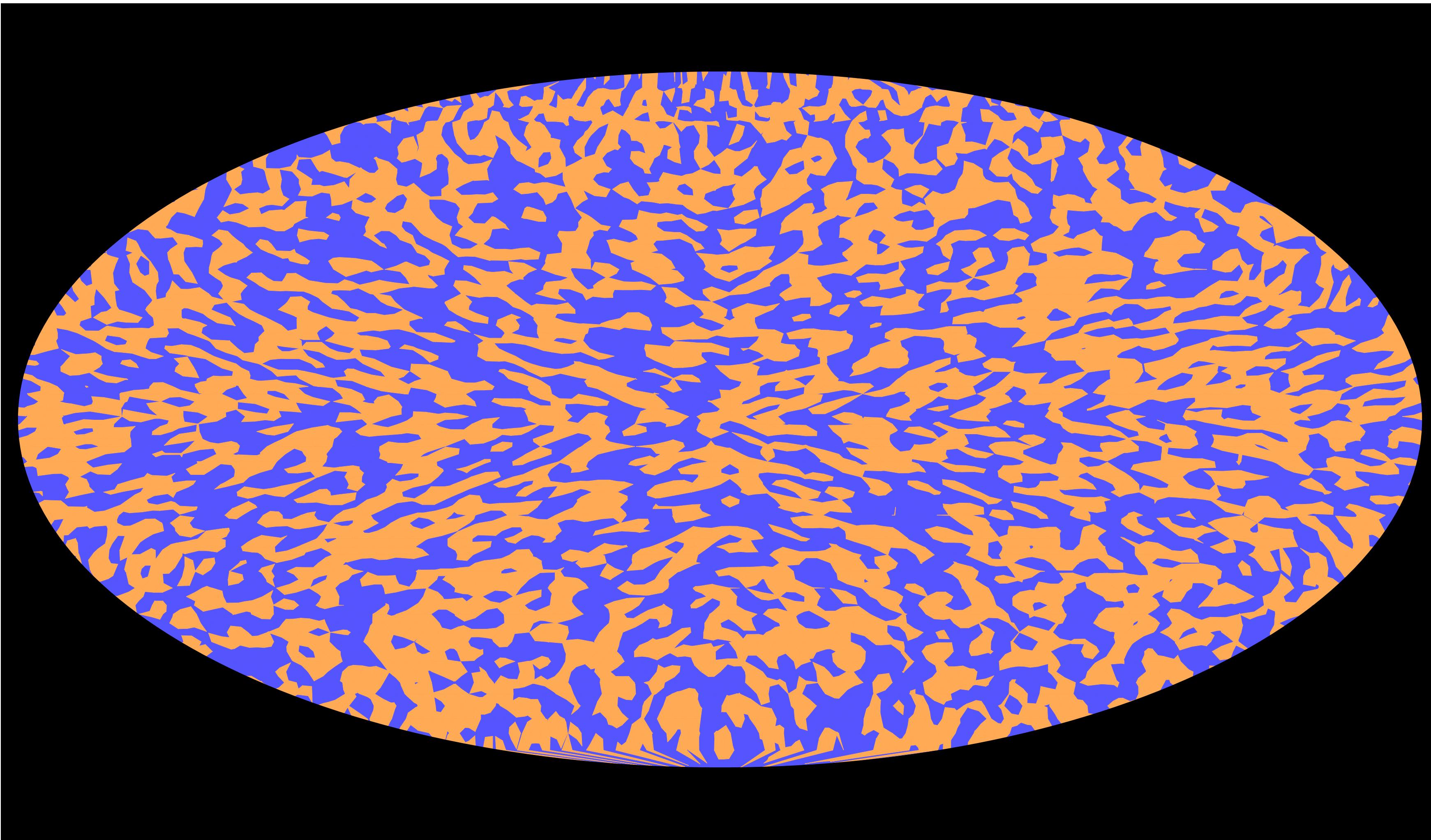
There will be $O(10^{3-4})$ domains on the LSS, and the CMB polarization from each domain is either not rotated at all or rotated by a fixed angle, $\Phi \simeq 0.42c_\gamma$ deg.



$$= 2^N, \quad N = O(10^{3-4})$$

**“KiloByte Cosmic Birefringence”
(KBCB)**

KBCB from ALP domain walls



Blue: $\Phi = 0$

Orange: $\Phi \simeq 0.42c_\gamma$ deg

N.B. This figure is NOT a result of numerical simulations, but just a mock sample.

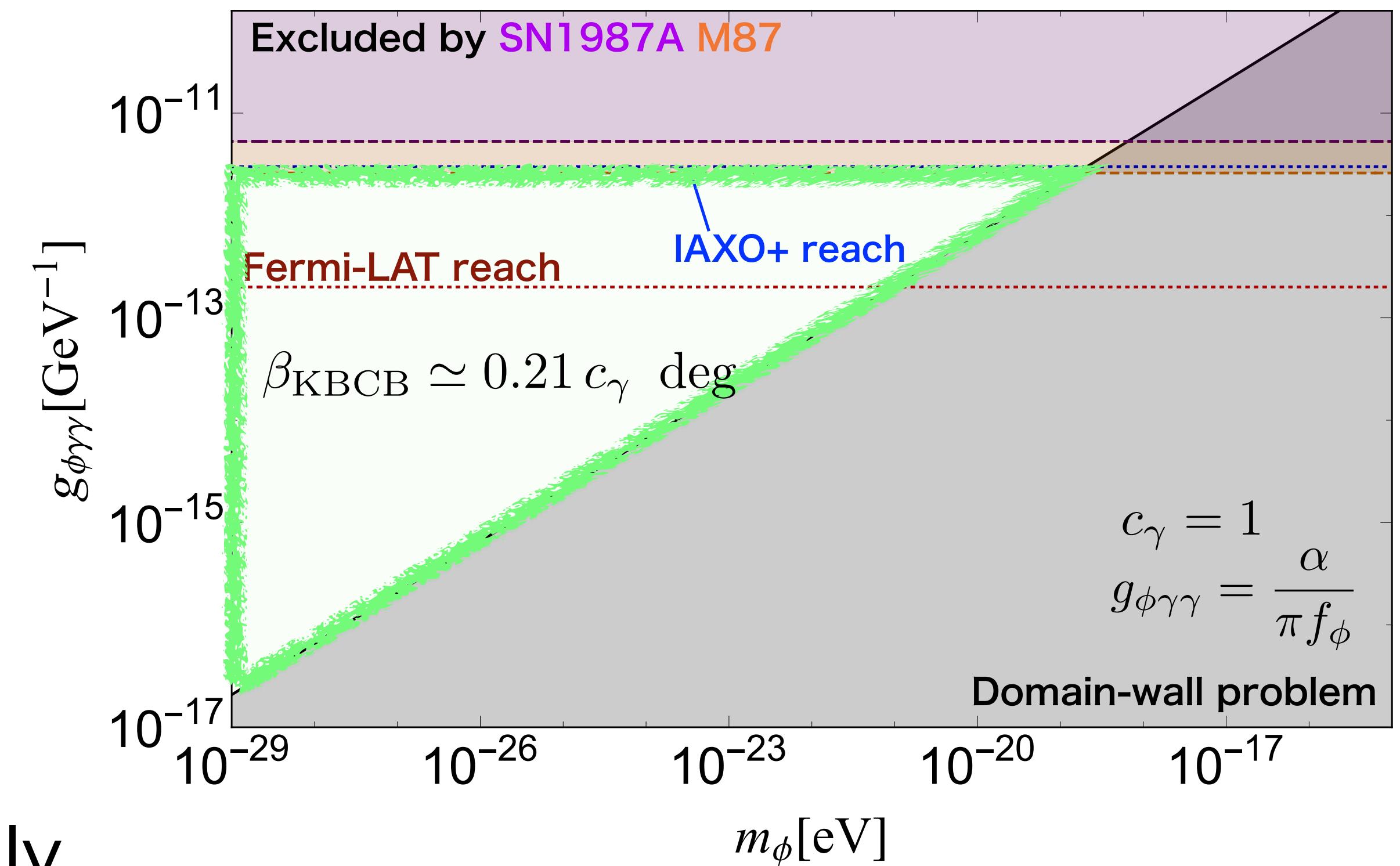
Predictions of KBCB

Isotropic CB

$$\beta = \frac{1}{4\pi} \int d\Omega \Phi(\Omega) = \frac{1}{2} c_\gamma \alpha \simeq 0.21 c_\gamma \text{ deg} .$$

independent of m_ϕ and f_ϕ .

$\beta_{\text{obs}} = 0.35 \pm 0.14 \text{ deg}$. can be naturally explained for $c_\gamma = O(1)$.



The predicted isotropic CB is the same over the viable parameter space (green triangle).

Predictions of KBCB

Anisotropic CB

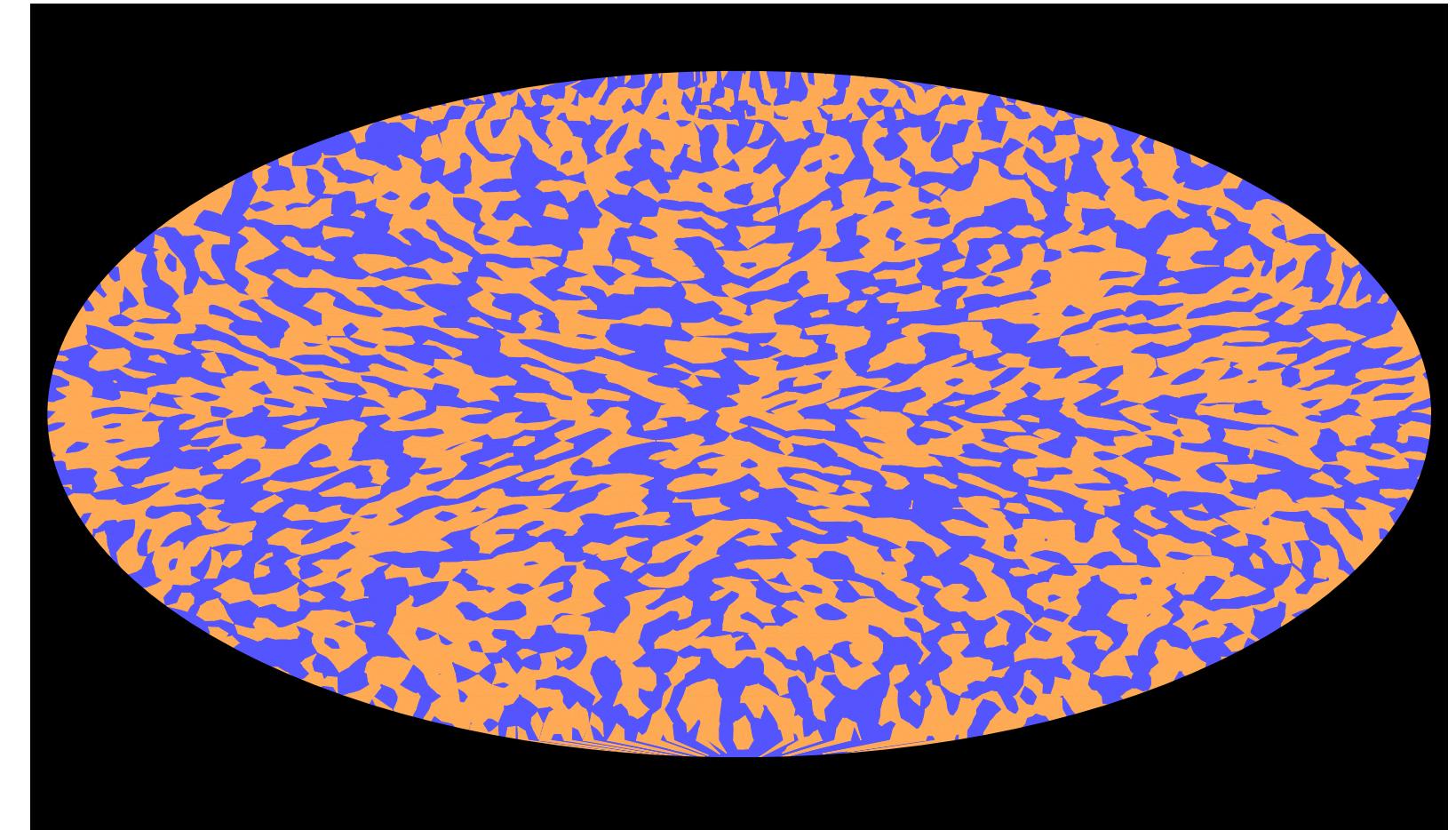
$$\Delta\Phi(\Omega) \equiv \Phi(\Omega) - \beta$$

$$\begin{aligned} \Delta\Phi(\Omega) &= \pm \beta \\ &= \sum_{\ell,m} a_{\ell m} Y_{\ell m}(\Omega) \quad \text{i.e.} \quad a_{\ell m} = \int d\Omega \Delta\Phi(\Omega) Y_{\ell m}^*(\Omega). \end{aligned}$$

The angular power spectrum:

$$C_\ell^\Phi \equiv \frac{1}{2\ell + 1} \sum_m a_{\ell m}^* a_{\ell m} = 2\pi \int d\cos\theta \Delta\Phi(0,0) \Delta\Phi(\theta,0) P_\ell(\cos\theta)$$

$$\text{Then, } \int d\Omega (\Delta\Phi(\Omega))^2 = \sum_\ell (2\ell + 1) C_\ell^\Phi = 4\pi\beta^2$$



Predictions of KBCB

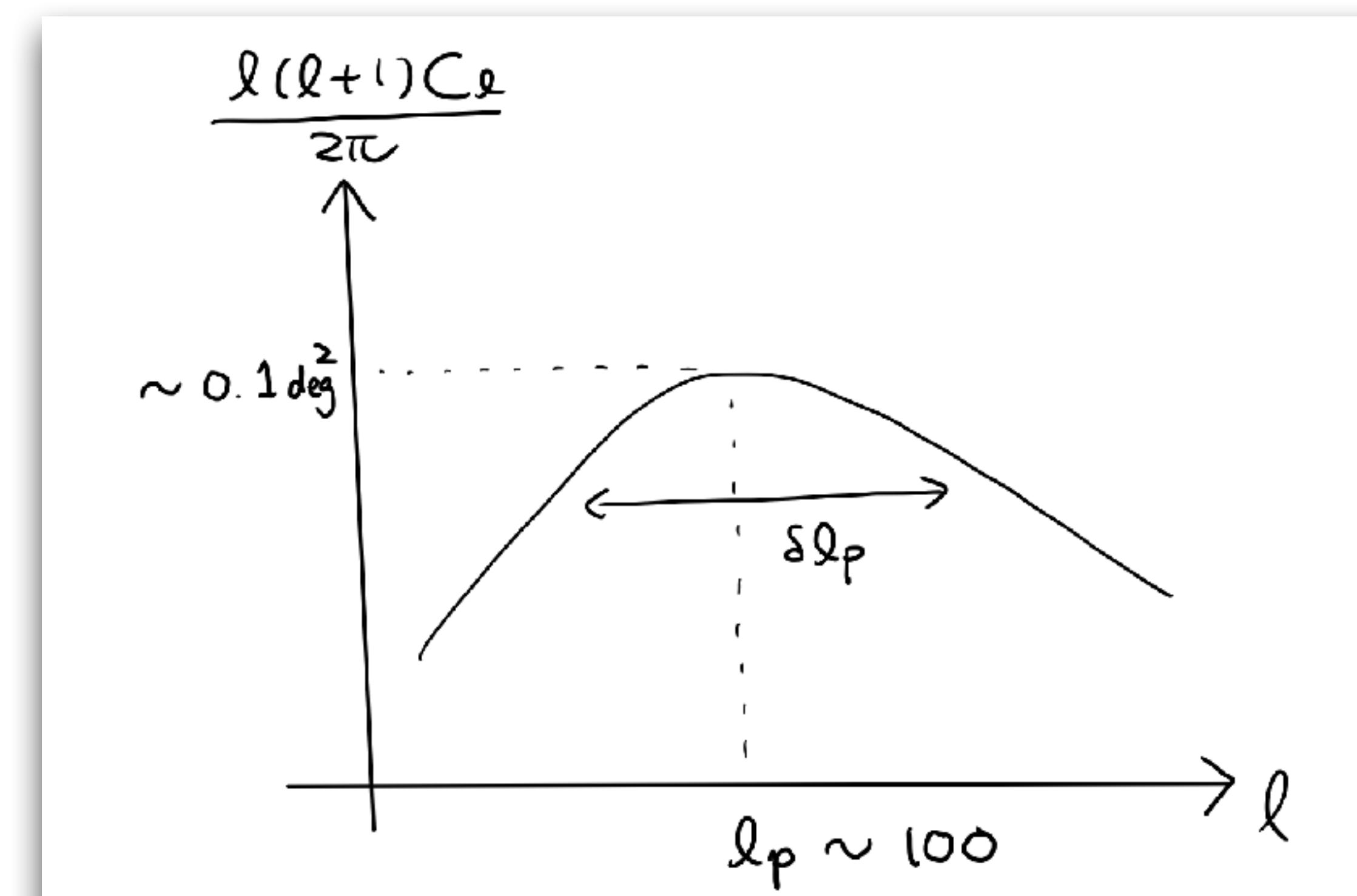
Anisotropic CB

$$\int d\Omega (\Delta\Phi(\Omega))^2 = \sum_{\ell} (2\ell + 1) C_{\ell}^{\Phi} = 4\pi\beta^2$$

If the peak is broad, $\ell_p \sim \delta\ell_p$

$$\frac{\ell_p(\ell_p + 1)C_{\ell_p}^{\Phi}}{2\pi} \lesssim 0.1 \left(\frac{\beta}{0.35 \text{ deg}} \right)^2 \text{ deg}^2$$

The peak location corresponds to the Hubble horizon at the LSS.



A simple model of the domain-wall network

Let $\mathcal{D}_{\text{DW}} = r_{\text{DW}}^{-1}$ be the DW density along a straight line, where r_{DW} is the average distance b/w walls.

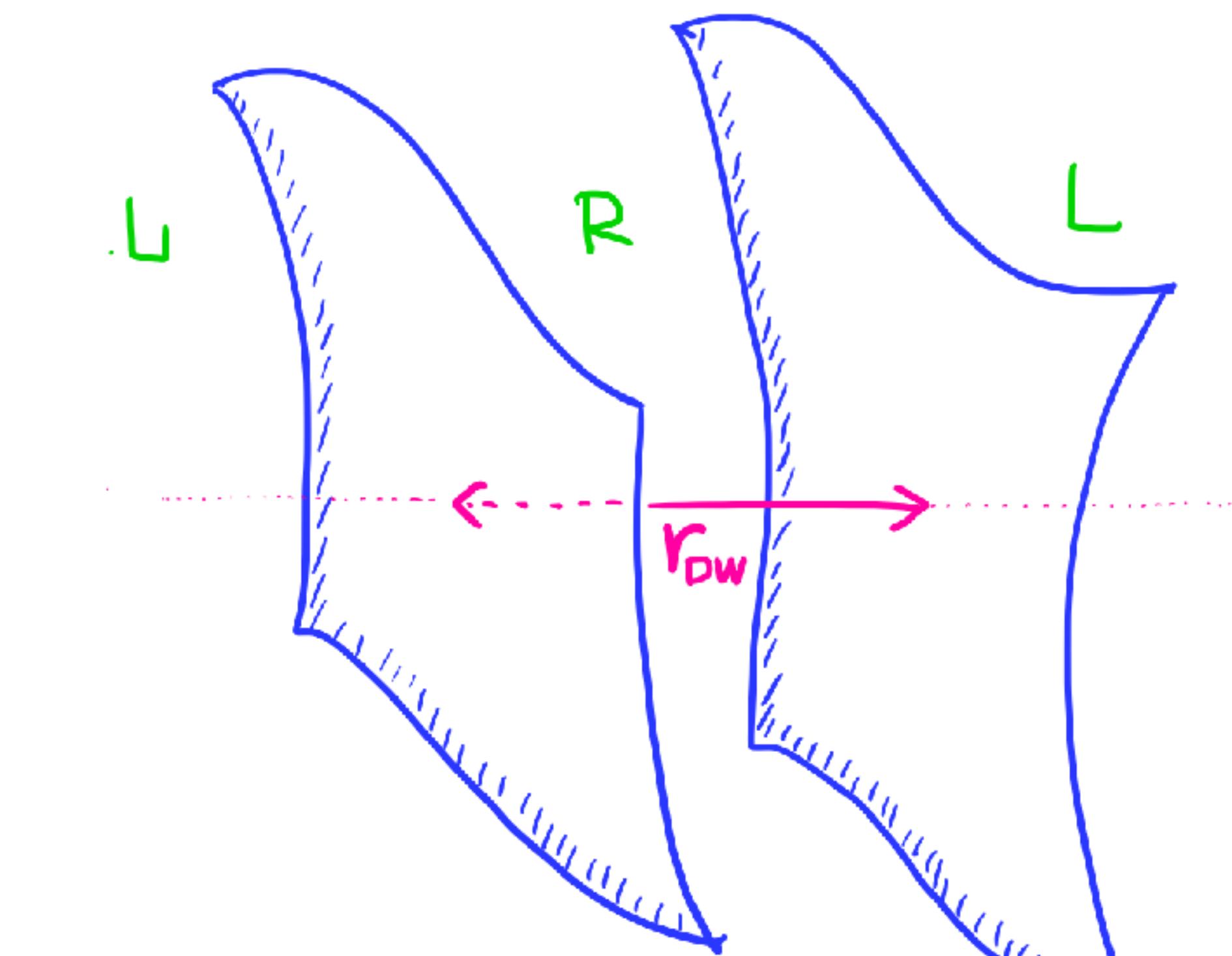
For a scaling solution, we have

$$\mathcal{D}_{\text{DW}} = \kappa_{\text{DW}} H \quad \text{with} \quad \kappa_{\text{DW}} = \mathcal{O}(1)$$

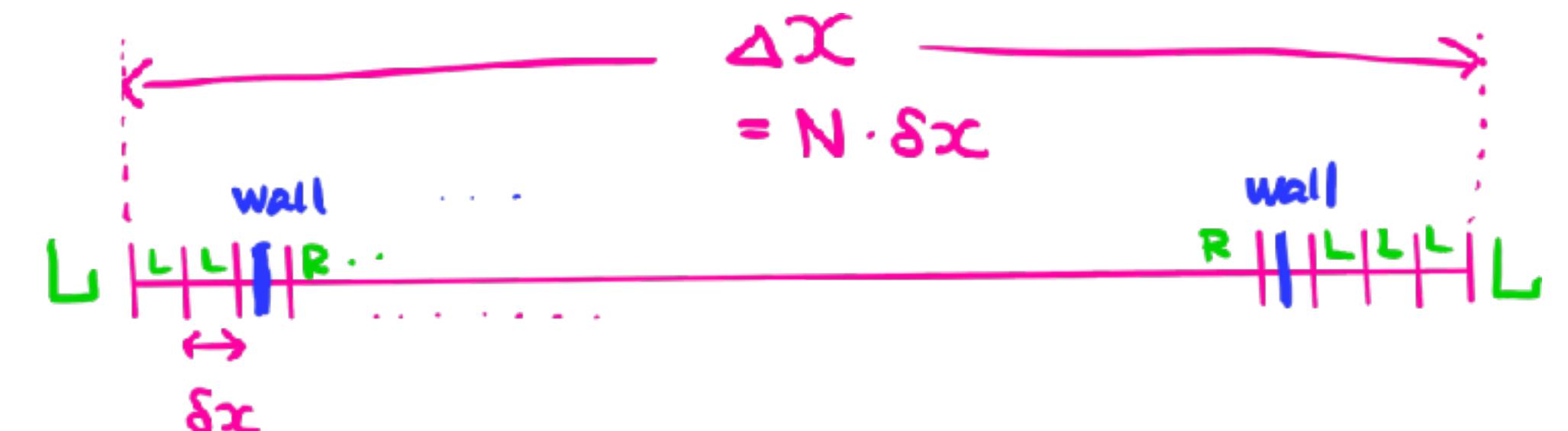
Then the probability of being in the same vacuum at a point Δx apart is

$$P_{\text{match}}[\Delta x] = \sum_{N/2 \geq m=0} {}_N C_{2m} (\mathcal{D}_{\text{DW}} \delta x)^{2m} (1 - \mathcal{D}_{\text{DW}} \delta x)^{N-2m}$$

$$\rightarrow \frac{1}{2} (1 + e^{-2\mathcal{D}_{\text{DW}} \Delta x})$$



$$r_{\text{DW}} \sim H^{-1} \text{ for a scaling solution}$$



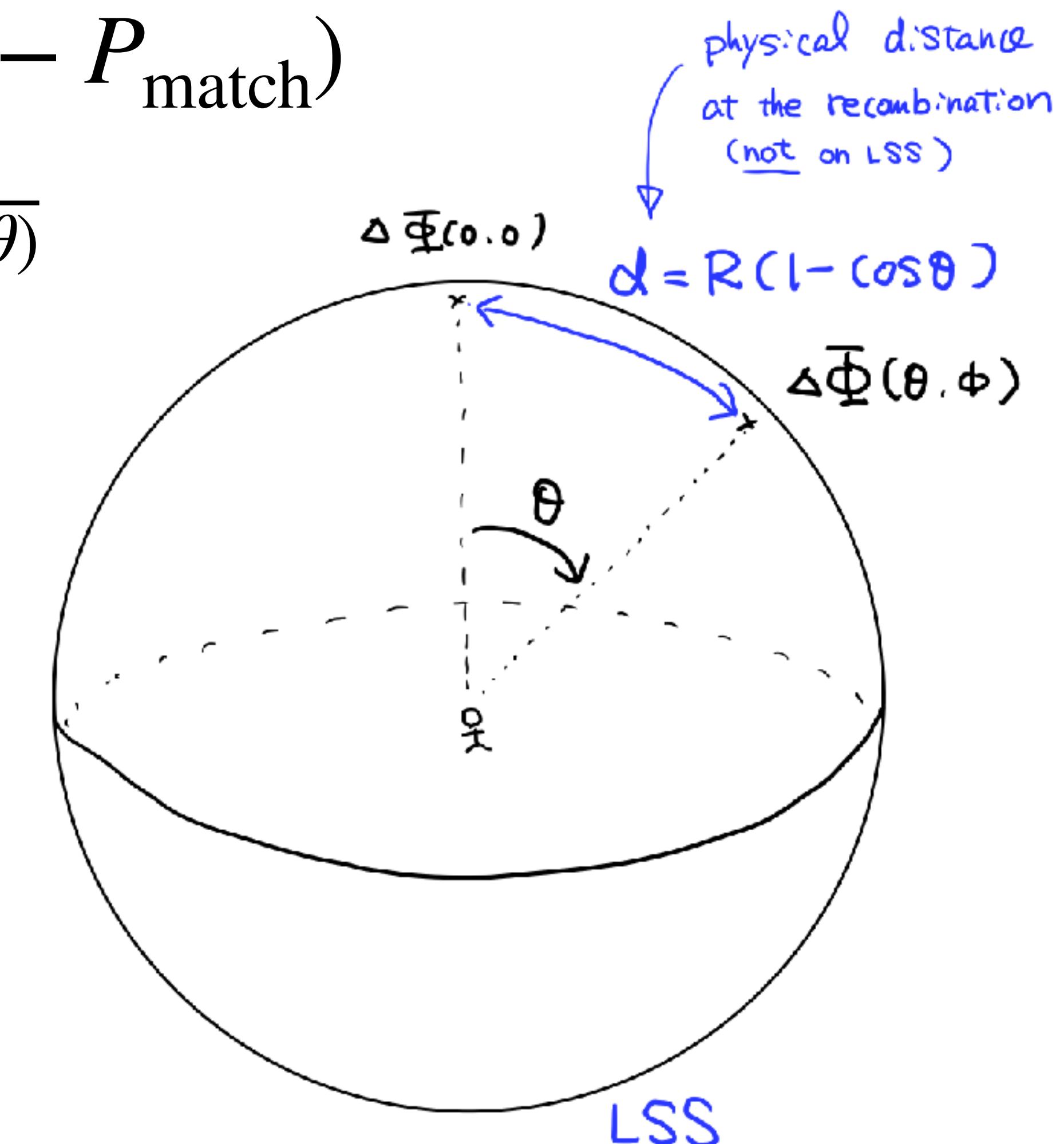
$2m$: the number of domain walls in $\Delta x = N\delta x$ 33

A simple model of the domain-wall network

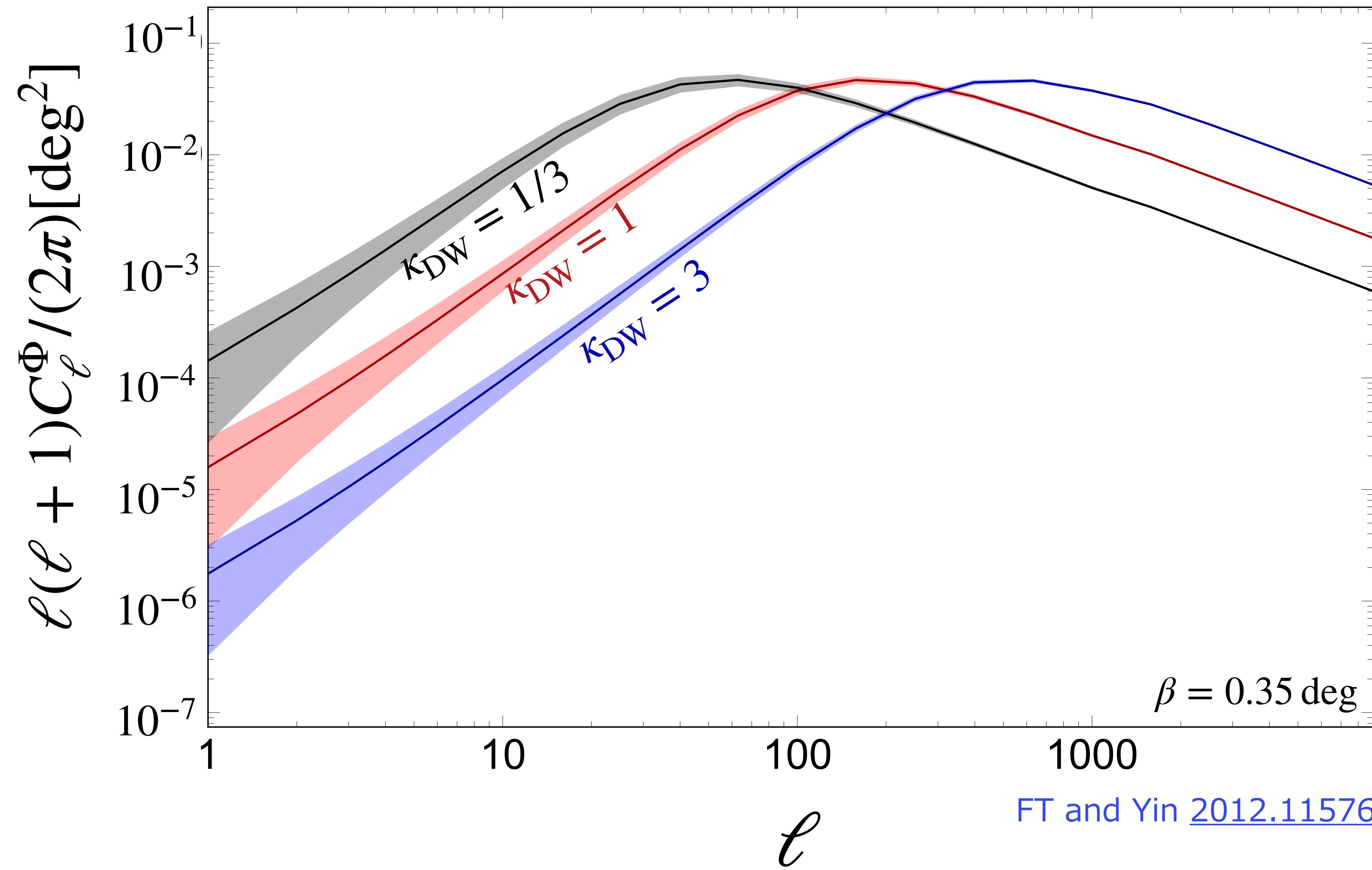
$$\begin{aligned}\langle \Delta\Phi(0,0)\Delta\Phi(\theta,\phi) \rangle &\simeq \beta^2 P_{\text{match}} + \beta(-\beta)(1 - P_{\text{match}}) \\ &= \beta^2 e^{-2\mathcal{D}_{\text{DW}}R\sqrt{2(1 - \cos\theta)}}\end{aligned}$$

Then, we can estimate the angular power spectrum (with the ensemble average) by substituting the above into

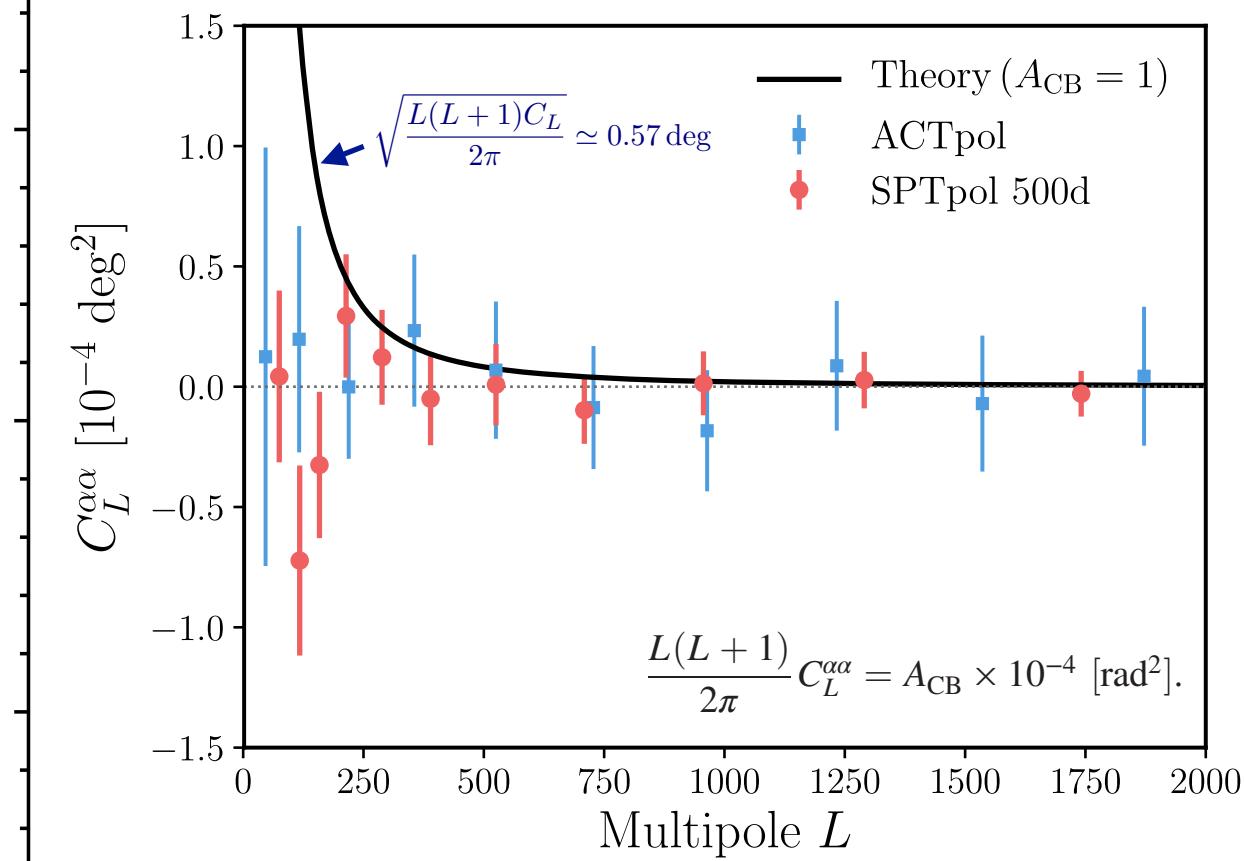
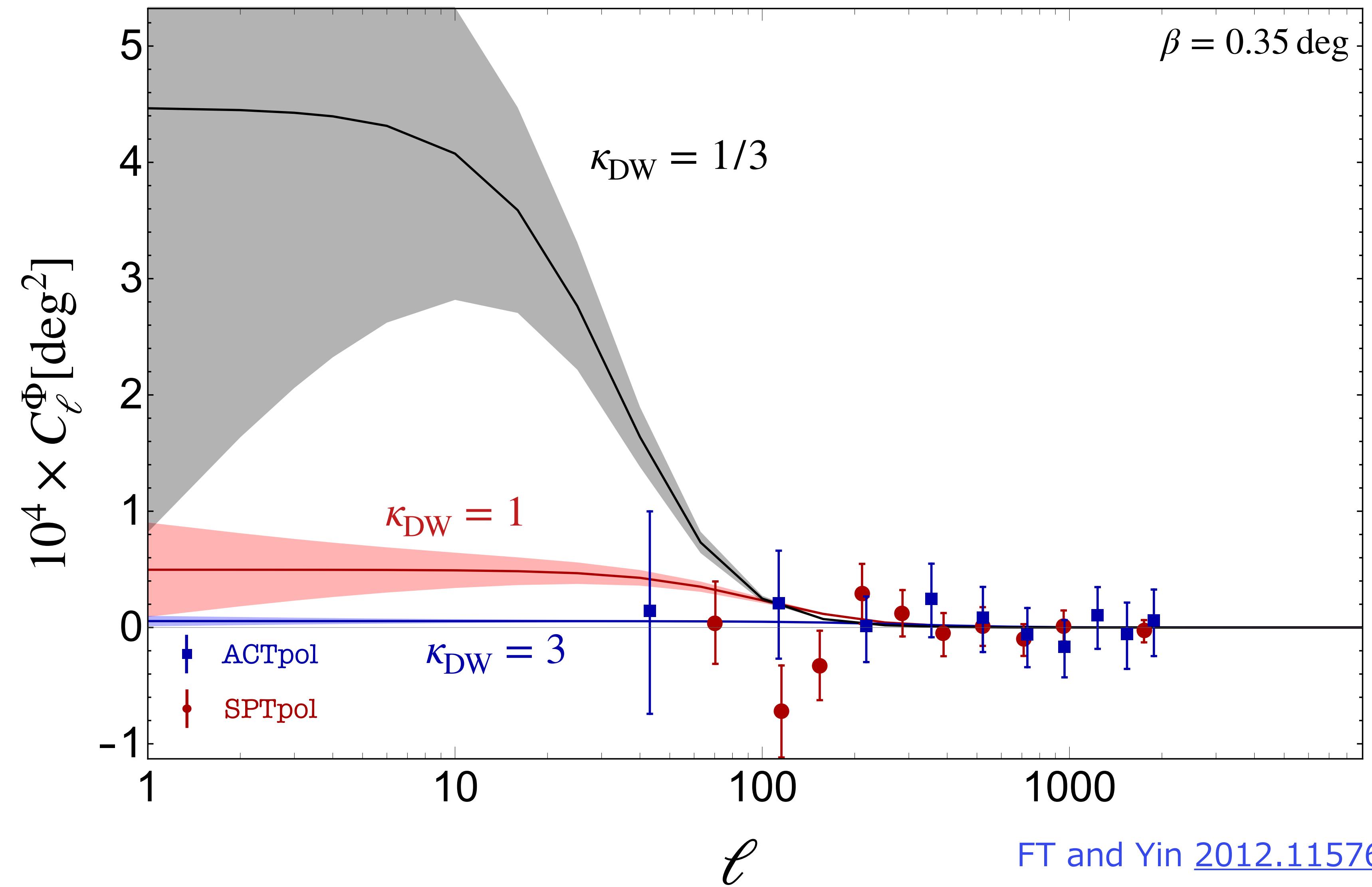
$$C_\ell^\Phi = 2\pi \int d\cos\theta \langle \Delta\Phi(0,0)\Delta\Phi(\theta,0) \rangle P_\ell(\cos\theta)$$



Anisotropic CB of ALP domain walls



Anisotropic CB of ALP domain walls

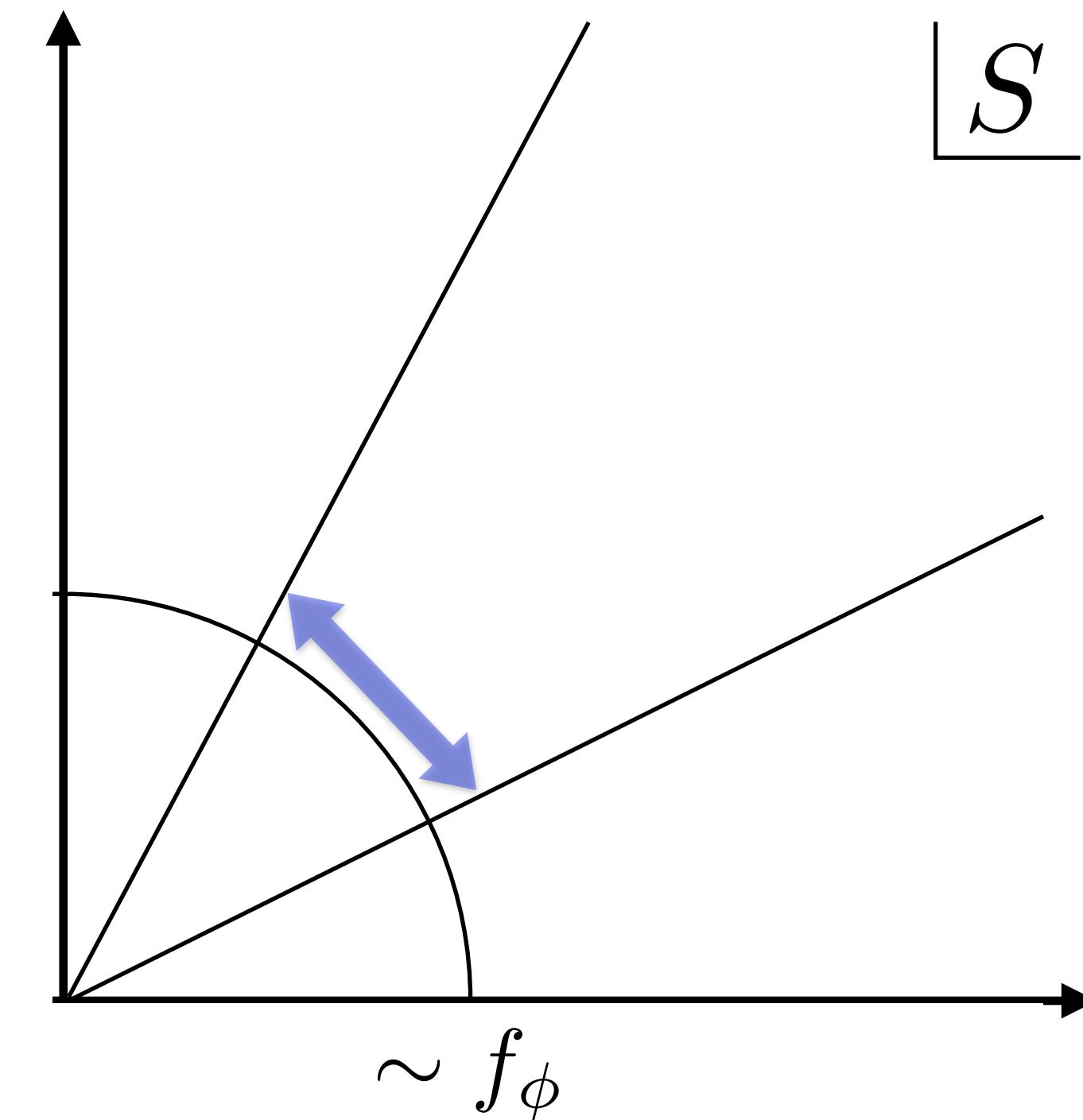


A model with a negative Hubble mass

Suppose that the PQ symmetry is linearly realized as

$$S = \frac{f_\phi}{\sqrt{2}} e^{i \frac{\phi}{f_\phi}}$$

$$V(S) = -m_S^2 |S|^2 + \frac{\lambda}{4} |S|^4$$



A model with a negative Hubble mass

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$$S = \frac{f_\phi}{\sqrt{2}} e^{i \frac{\phi}{f_\phi}}$$

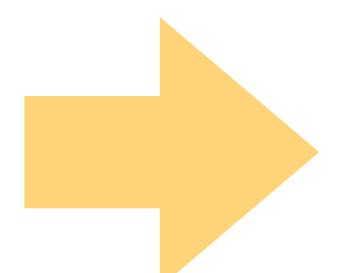


$$S \sim H_{\text{inf}} e^{i \frac{\phi}{H_{\text{inf}}}}$$

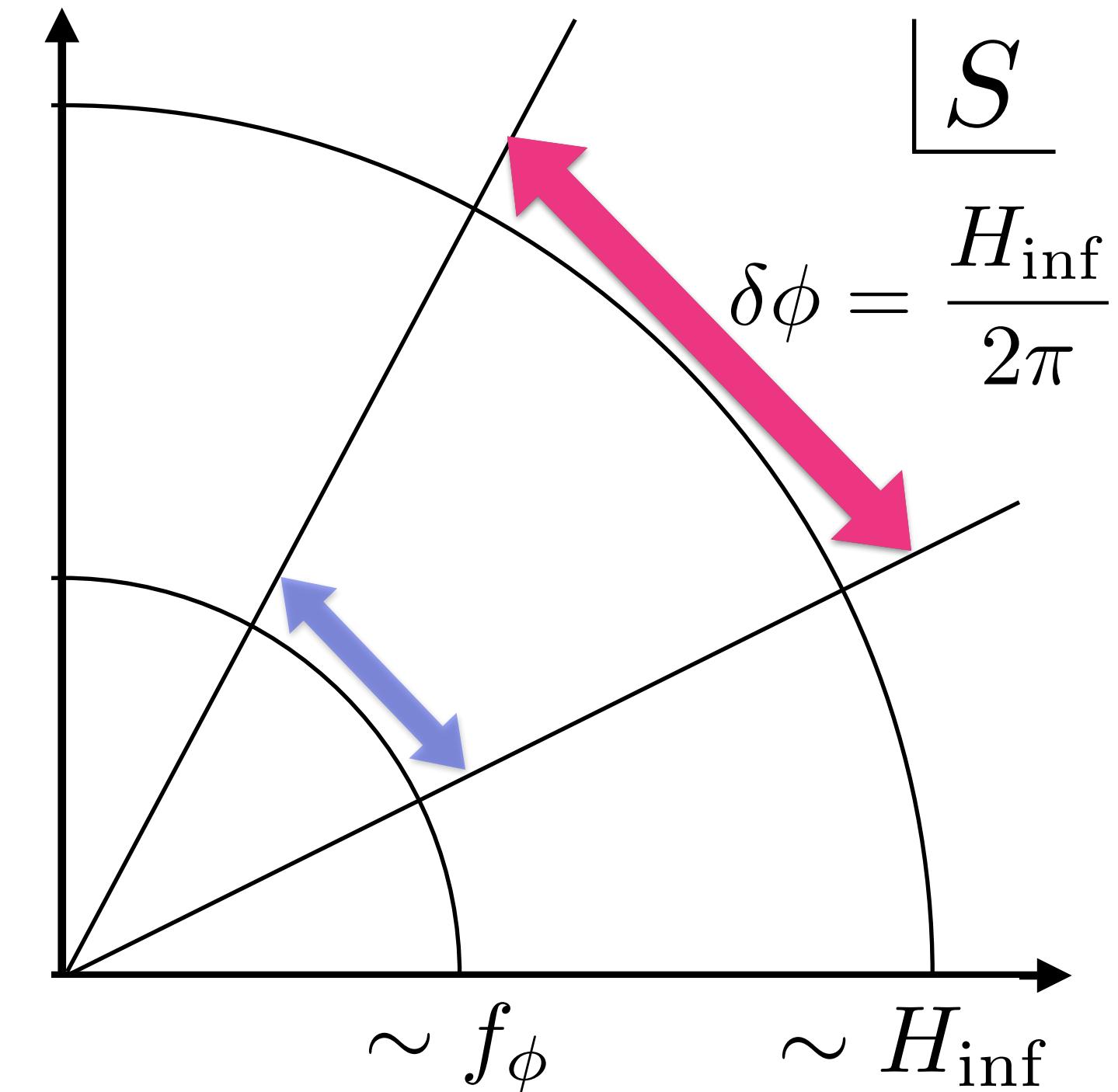
(during inflation)

$$V(S) = -m_S^2 |S|^2 + \frac{\lambda}{4} |S|^4 - H_{\text{inf}}^2 |S|^2$$

During inflation, the effective decay constant can be as large as H_{inf} , and the axion acquires quantum fluctuations of $\mathcal{O}(H_{\text{inf}})$.



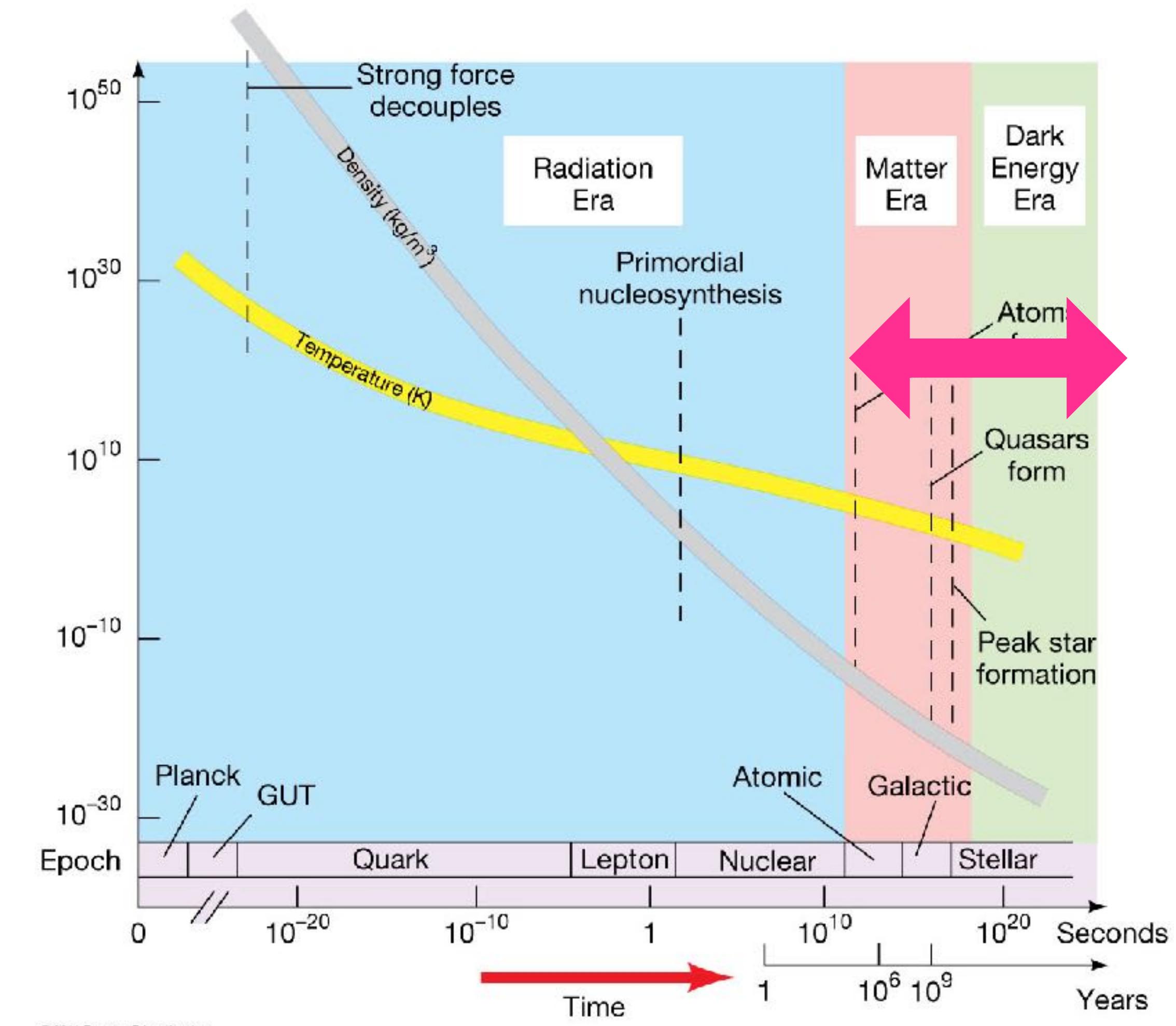
$$\delta\theta = \mathcal{O}(1)$$



4. Scenario 2: Axion coupled to DM

Why does the ALP starts to move at such a special timing i.e. between the recombination and the present?

A (mild) coincidence problem ?

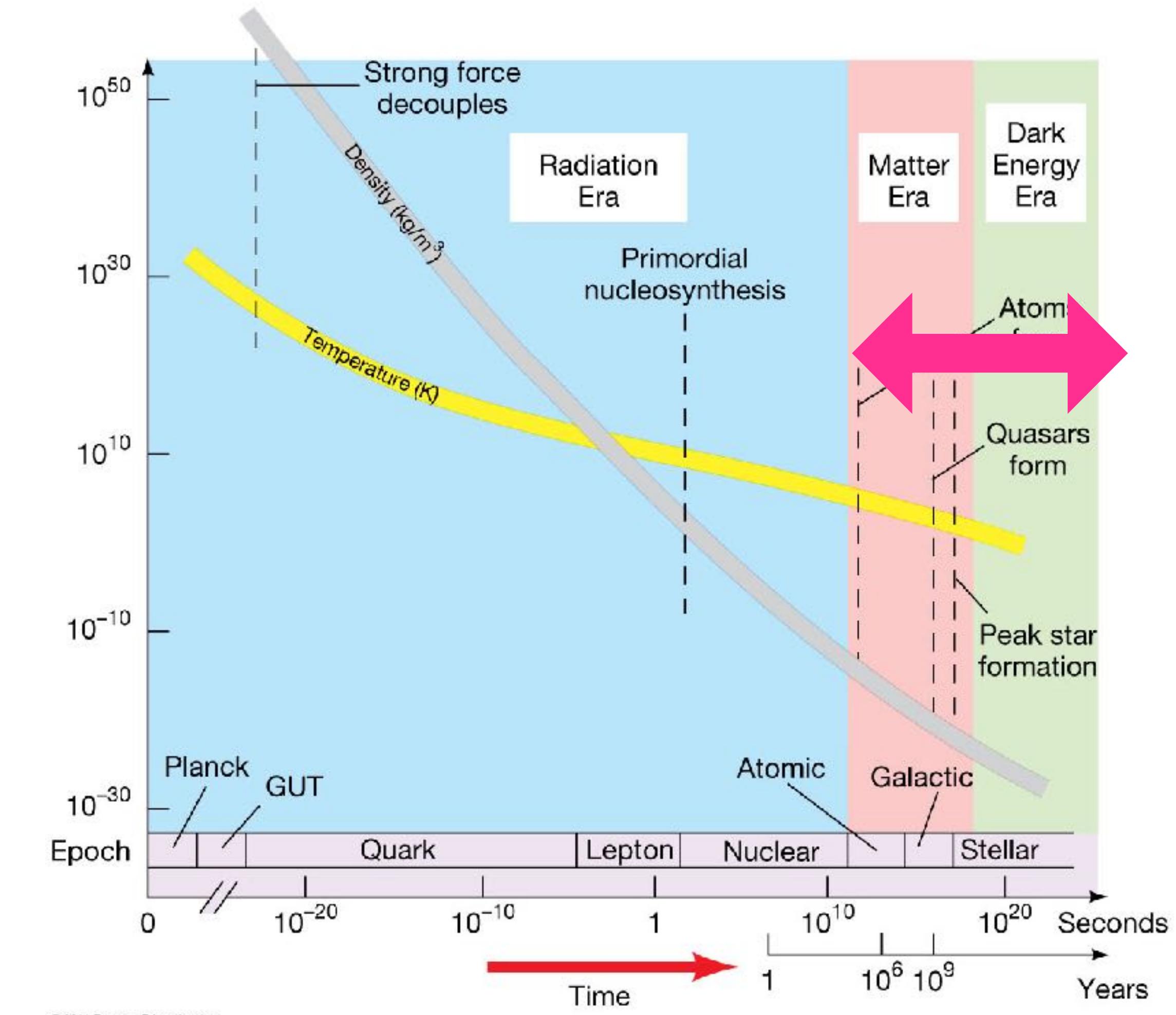


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Why does the ALP starts to move at such a special timing i.e. between the recombination and the present?

A (mild) coincidence problem ?

- Maybe natural in string axiverse?
 - Number of axions?
 - Coupling to photons?



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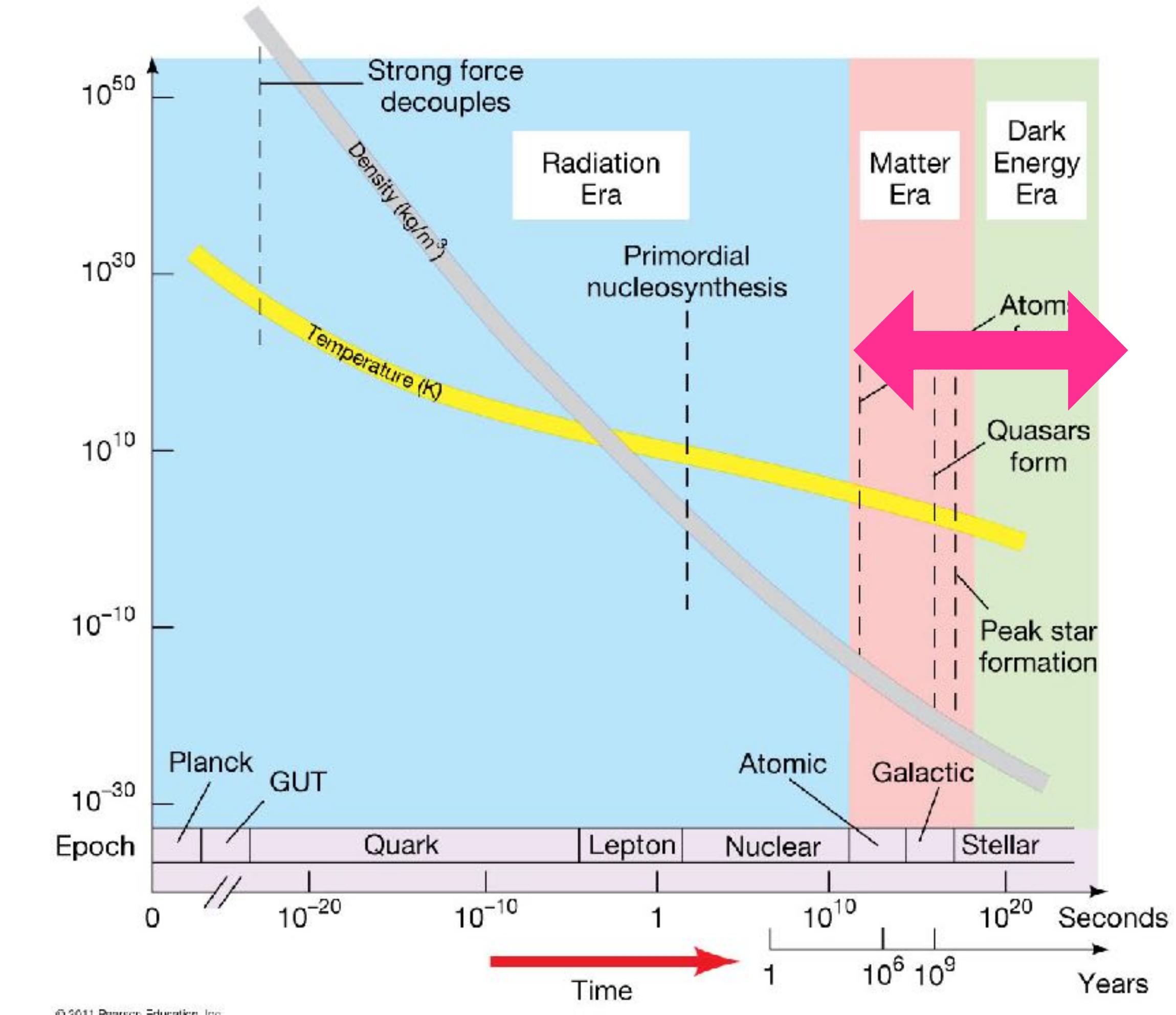
Why does the ALP starts to move at such a special timing i.e. between the recombination and the present?

A (mild) coincidence problem ?

- Maybe natural in string axiverse?
 - Number of axions?
 - Coupling to photons?

If the ALP is coupled to DM, it may acquire an effective mass which becomes relevant only after matter-radiation equality (~ recombination).

$$V(\phi) \sim \frac{\rho_{\text{DM}}}{M_p^2} \phi^2$$



CB triggered by DM domination



Consider a “massless” ALP with

$$V(\phi) = \frac{1}{2} c_H H_{\text{DM}}^2 \phi^2 \quad \text{with} \quad H_{\text{DM}}^2 \equiv \frac{\rho_{\text{DM}}}{3M_p^2}$$

cf. Hidden monopole DM (Witten effect)

$$\mathcal{L} \supset -\frac{1}{4} X_{\mu\nu} X^{\mu\nu} - \frac{\alpha_H}{8\pi f_\phi} \phi X_{\mu\nu} \tilde{X}^{\mu\nu} \rightarrow c_H = 3 \left(\frac{\rho_{\text{monopole}}}{\rho_{\text{DM}}} \right) \left(\frac{\alpha_H M_p}{4\pi f_\phi} \right)^2$$

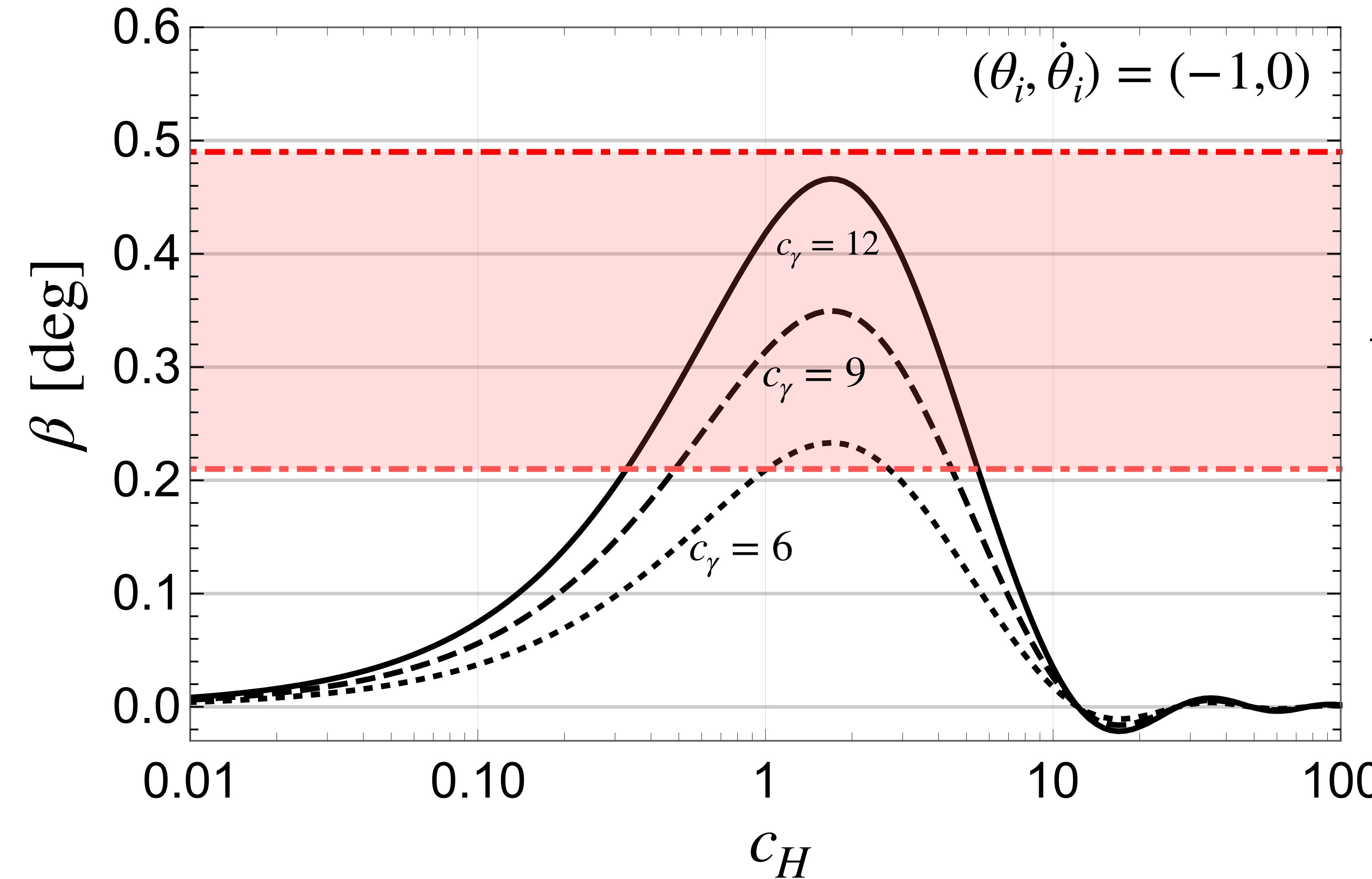
$c_H \sim 1$ for $\rho_{\text{monopole}} \sim \rho_{\text{DM}}$, $\alpha_H \sim 0.01$, $f_\phi \sim 10^{15} \text{ GeV}$

The ALP starts to move after the matter-radiation equality if $c_H = O(1)$.

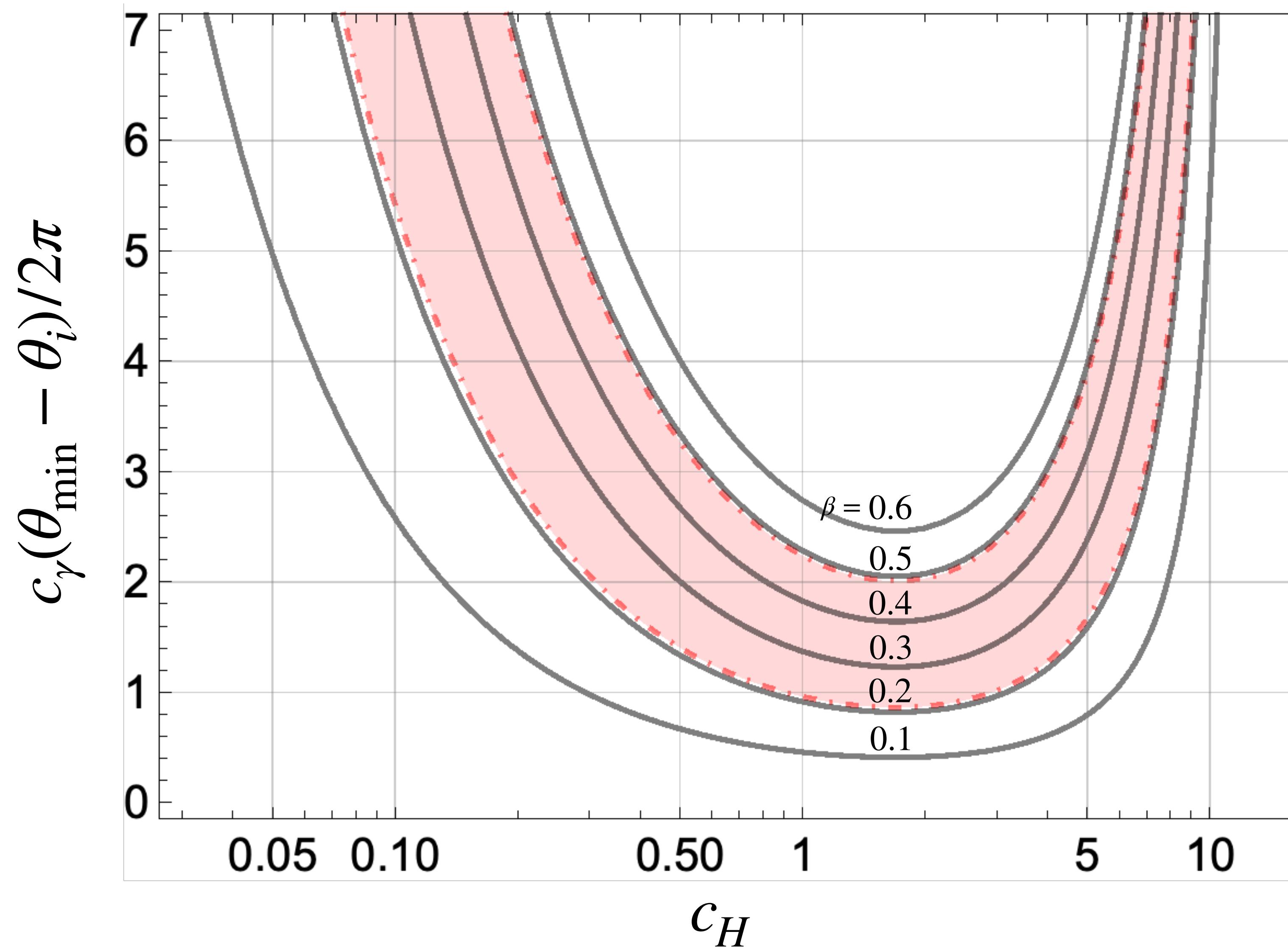
$$\ddot{\phi} + 3H\dot{\phi} + c_H H_{\text{DM}}^2 \phi = 0$$

$$H^2 = H_0^2 \left(\Omega_{\text{rad}} a^{-4} + \Omega_{\text{mat}} a^{-3} + \Omega_\Lambda \right)$$

CB triggered by DM domination



CB triggered by DM domination



No fine-tuning of the initial angle is needed for $c_H \sim c_\gamma = O(1)$.

5. Summary

- Recent hint for the isotropic CB may be due to ultralight ALP.

$$\beta_{\text{obs}} = 0.35 \pm 0.14 \text{ deg}$$

- **ALP domain walls** naturally explains the isotropic CB over a wide range of the axion mass and axion-photon coupling.

$$\beta_{\text{KBCB}} \simeq 0.21 c_\gamma \text{ deg independent of } m_\phi \text{ and } f_\phi.$$

Also predicts a peculiar anisotropic CB, which may be checked by future CMB observations.

- **ALP coupled to DM** works even for a massless ALP;
e.g. the ALP coupled to hidden monopole DM with $f_\phi \sim 10^{15} \text{ GeV.}$